

A New Electro-Optic Detection Scheme for Recording Electron Bunch Shapes With High Resolution and Record Recording Length

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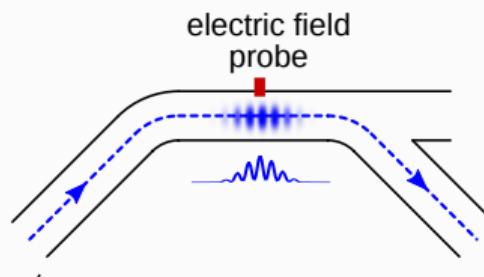
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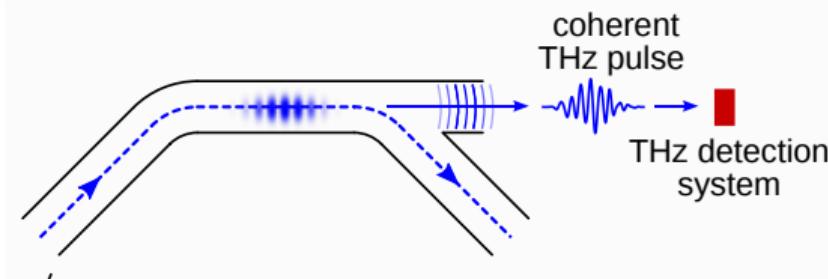
How to record the electron bunch temporal profile and/or THz radiation ?

→ probe its electric field...

... in the near-field (NF)



... or in the far-field (FF)



😊/😢 crystal near the e- bunch

😊 "very direct" measurement, access to the whole e-field

😊 intense electric field

😊 detection far from the e- bunch

😊/😢 "high-pass" filter, only access to fast-evolving component

😢 less intense field (V-kV/cm)

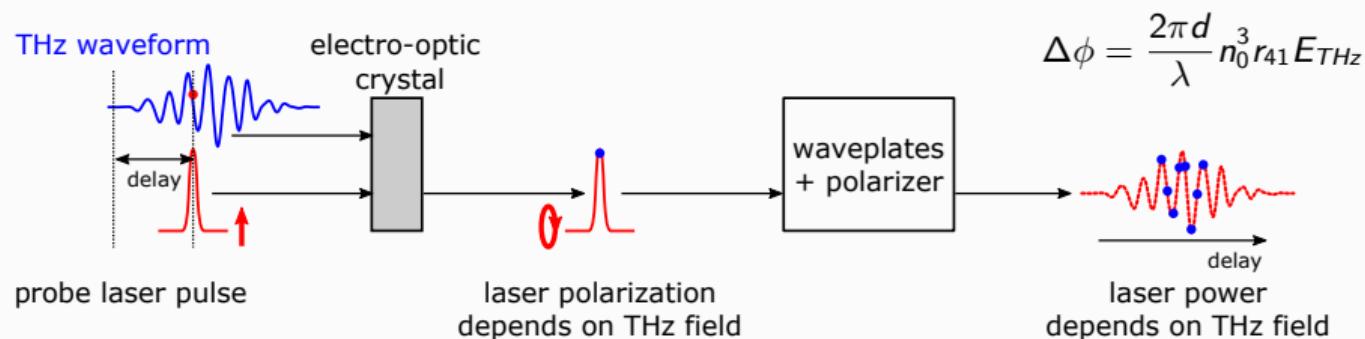
In both cases, need for:

- (1) 100's fs resolution; (2) single-shot; (3) MHz+ acquisition rate

Electro-optic sampling of electric field: principle

Simple cross-correlation of the THz and optical pulses based on the **Pockels effect**:

- An external electric field modifies the refractive indexes of a birefringent crystal (EO crystal).
- The THz-induced birefringence is probed using a laser pulse.
- ▷ Multi-THz bandwidth obtained: limited by crystal speed and laser pulse duration.



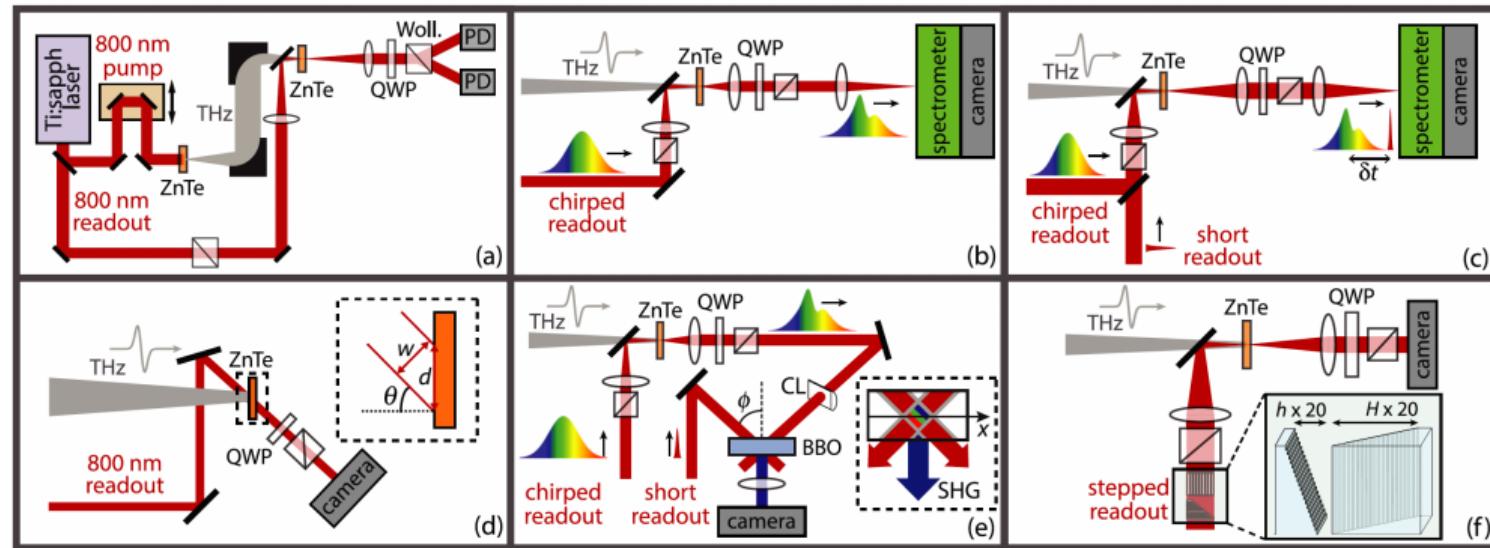
Free-propagating THz pulses (Time-domain spectroscopy, TDS): [Q. Wu & X.-C. Zhang, Appl. Phys. Lett. **67** (24), (1995)]

Scanned EO in accelerators: [Wilke et al., Phys. Rev. Lett. **88**, 124801 (2002)], [Katayama et al., App. Phys. Lett. **100**, 111112 (2012)]

Single-shot recording ?

Various strategies:

- time-to-space conversion,
- time-to-angle conversion,
- time-to-wavelength conversion.



[S. M. Teo, B. K. Ofori-Okai, C. A. Werley, K. A. Nelson, Rev. Sci. Instrum. 86, 051301 (2015)]

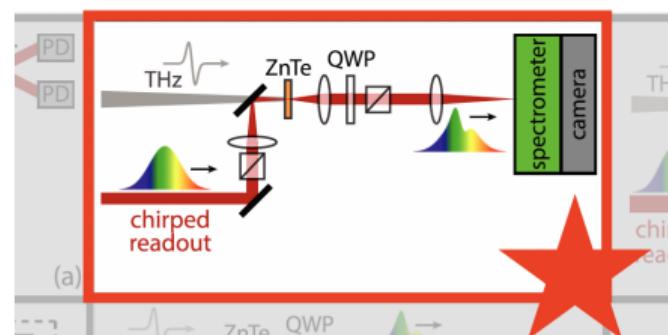
Single-shot recording ? → using chirped laser pulses

Various strategies:

- time-to-space conversion;
- time-to-angle conversion;
- time-to-wavelength conversion.

Potential applications:

- Monitoring non-repetitive phenomena,
e.g. in accelerators
- Time Domain Spectroscopy in situations where scanning is unpractical (low-rep. rate source, fast irreversible processes)



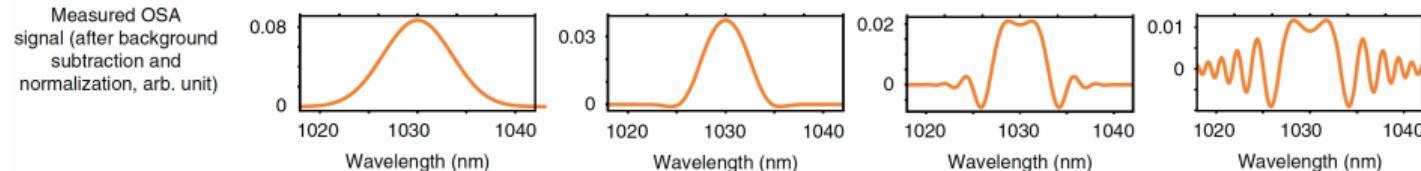
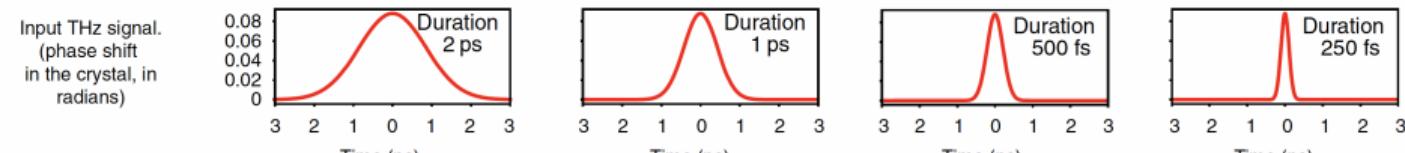
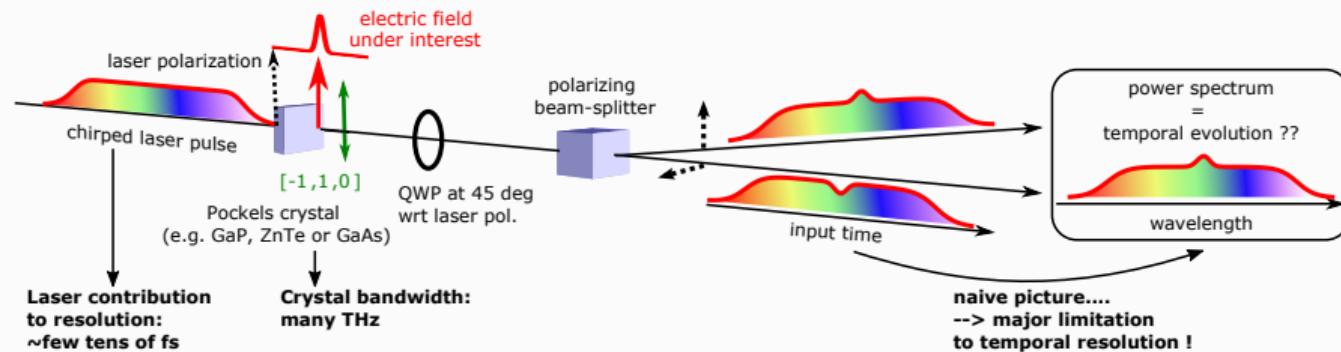
First demonstration using OSA readout: [Z. Jiang & X.-C. Zhang, Appl. Phys. Lett., 72, 1945 (1998)]

Applications in accelerators: [Müller et al., Phys. Rev. ST Accel. Beams 15, 070701 (2012)], [Hiller et al., IPAC'13, p. 500 (2013)]

MHz+ acquisition rate with photonic time-stretch readout: [Roussel, et al., Sci Rep 5, 10330 (2015)], [Bielawski, et al., Sci Rep 9, 10391 (2019)]

(20-year-old) Temporal resolution issue: the “time \times bandwidth” limit (1)

Time-resolution limitation (20-year-old problem) [Sun, Jiang & Zhang, Appl. Phys. Lett. 73, 2233 (1998)]

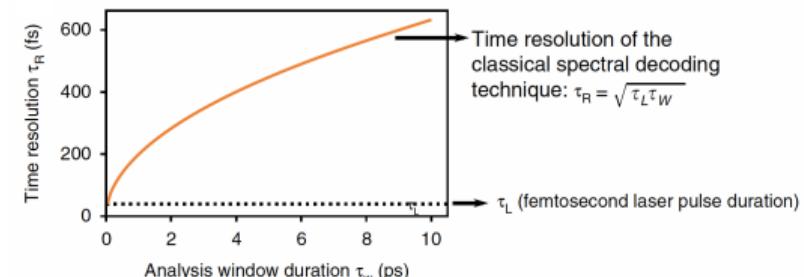


Temporal resolution issue: the “time \times bandwidth” limit (2)

Time-resolution (assuming an infinitely fast crystal) [Sun, Jiang & Zhang, Appl. Phys. Lett. 73, 2233 (1998)]

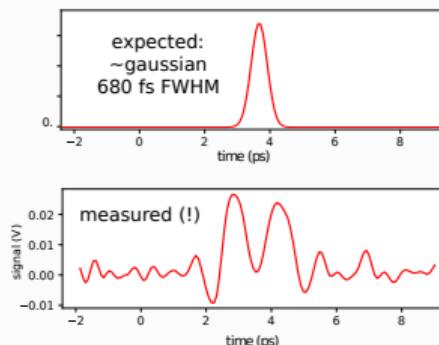
$$\tau = \sqrt{t_{laser} \times t_{window}}$$

Example: $t_{laser} = 100 \text{ fs}$
 $t_{window} = 10 \text{ ps}$ → $\tau = 1 \text{ ps} \gg t_{laser}$ ☺

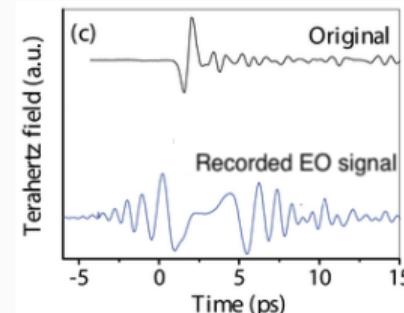


Examples of temporal resolution issue

- at short timescales e.g. e-bunch near field at EuXFEL

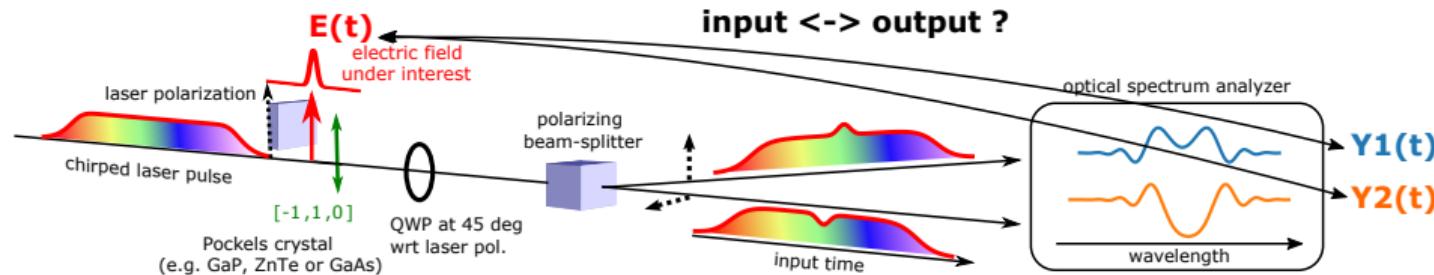


- for long observation windows e.g. TDS



[Murakami, doi: 10.5772/67195 (2017)]

A new point of view: calculation of Fourier-domain transfer functions



Derivation of the transfer functions

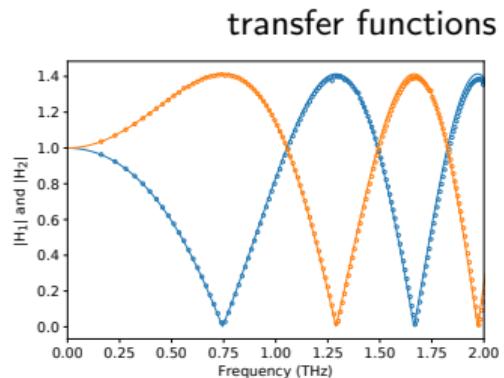
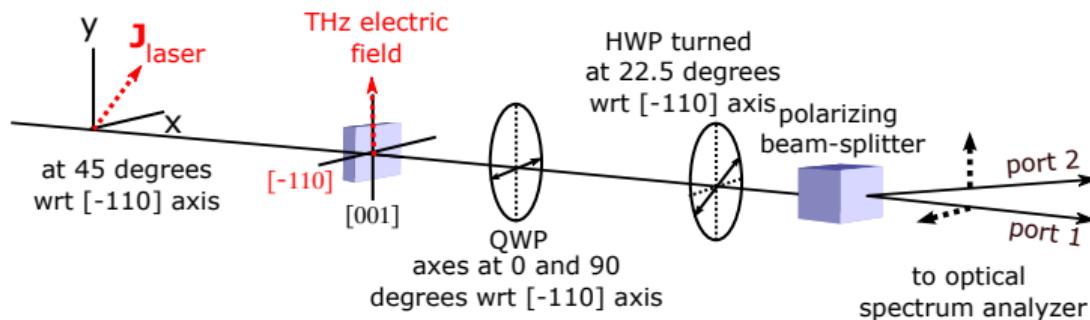
$$\begin{array}{ll} \text{Input field} & E(t) \stackrel{\leftrightarrow}{=} \tilde{E}(\Omega) \\ \text{Measurements} & Y_{1,2}(t) \stackrel{\leftrightarrow}{=} \tilde{Y}_{1,2}(\Omega) \approx H_{1,2}(\Omega) \times \tilde{E}(\Omega) \end{array}$$

with $H_{1,2}(\Omega) = h_{1,2} \cos(B\Omega^2 + \phi_{1,2})$, the transfer functions !

$h_{1,2}, \phi_{1,2}$ depend on the crystal and waveplates orientation, $B = 1/2C$ with $C = \partial\omega/\partial t$ the laser chirp.

calculation details in [Roussel et al., Light Sci Appl 11, 14 (2022)]

Our strategy: Diversity Electro-Optic Sampling (DEOS)



Goal: interleave the zeros of transfer functions

$$H_1(\Omega) = \sqrt{2} \cos \left(B\Omega^2 + \frac{\pi}{4} \right)$$

- in practice: crystal and waveplates orientation \neq “classical” EO
- problem well-posed \rightarrow “deconvolution” possible using the two channels

$$H_2(\Omega) = -\sqrt{2} \cos \left(B\Omega^2 - \frac{\pi}{4} \right)$$

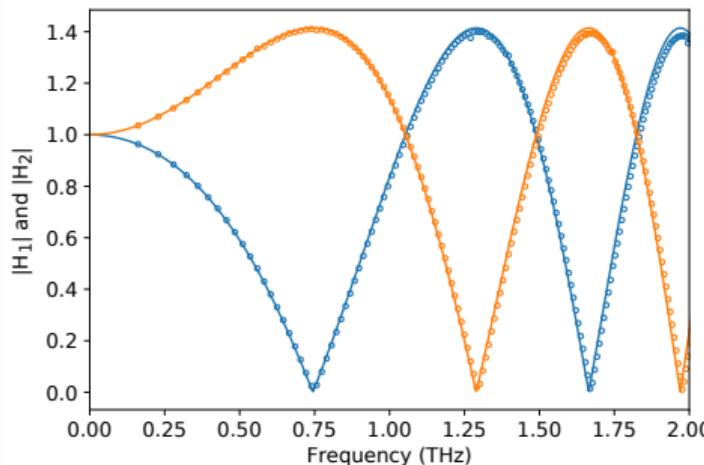
Algorithm for input field reconstruction: Maximum Ratio Combining (MRC)

Simple approach: retrieve the input field \tilde{E} from the measured EO signals $\tilde{Y}_{1,2}$ using either

$$\tilde{E}_R(\Omega) = \frac{\tilde{Y}_1(\Omega)}{H_1(\Omega)} \quad \text{or} \quad \tilde{E}_R(\Omega) = \frac{\tilde{Y}_2(\Omega)}{H_2(\Omega)} \quad \text{depending on frequency } \Omega$$

Refined algorithm

Use a combination of the two EO signals $\tilde{Y}_{1,2}$ with **optimal** weights

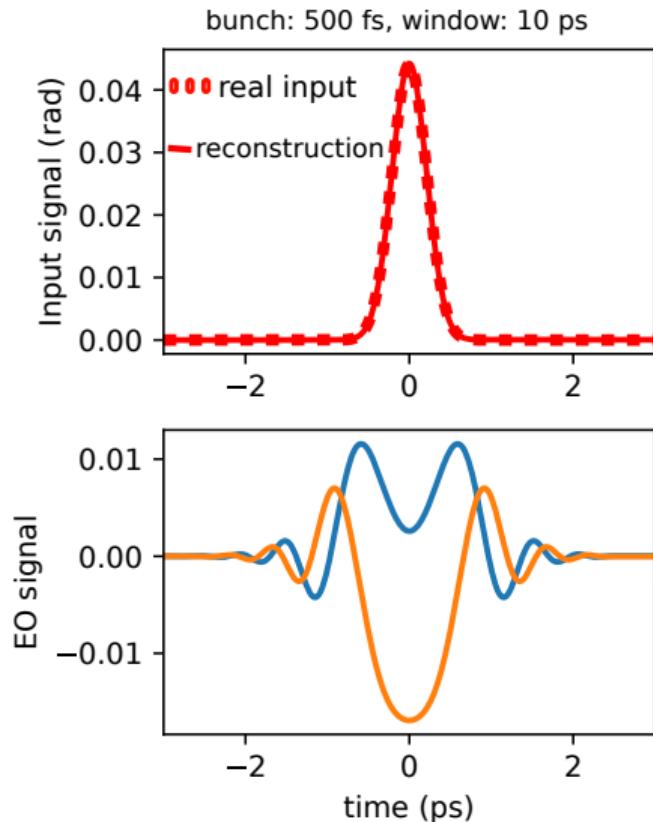


Maximum Ratio Combining (MRC) method:

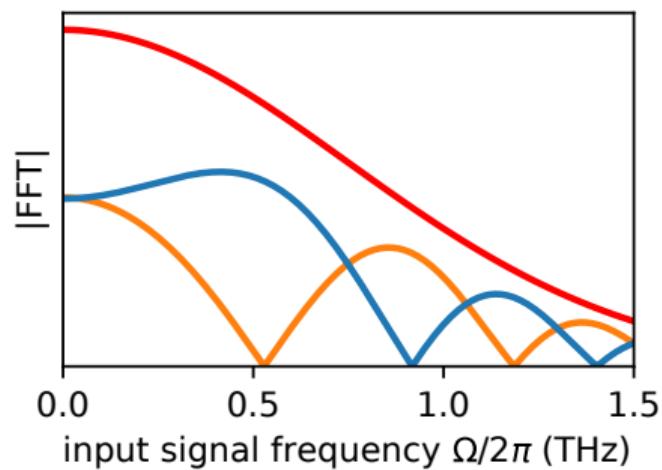
$$\tilde{E}_R = \frac{H_1 \tilde{Y}_1 + H_2 \tilde{Y}_2}{|H_1|^2 + |H_2|^2}$$

Inspired by: [Han, Boyraz & Jalali, *Microwave Theory and Techniques, IEEE Transactions on* 53, 1404-1408 (2005)]

Reconstruction algorithm: numerical test

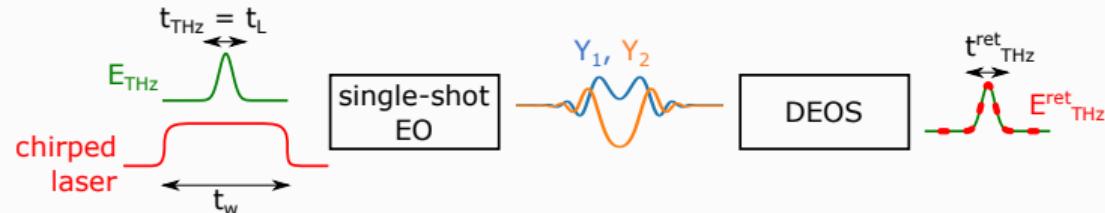


- Old limitation $\tau = \sqrt{t_{laser} \times t_{window}}$
- New resolution limit $\tau \sim t_{laser}$?
- Time window t_{window} : no limit (theoretically)

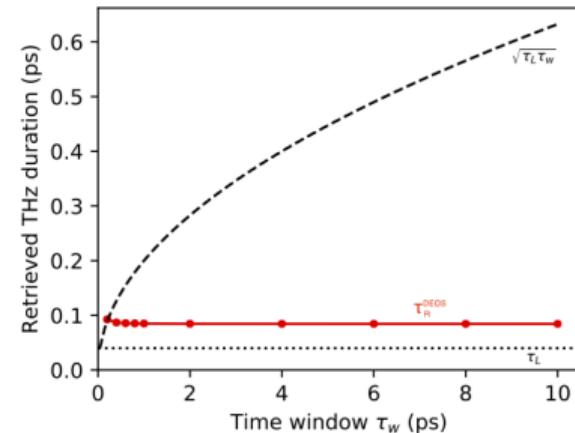
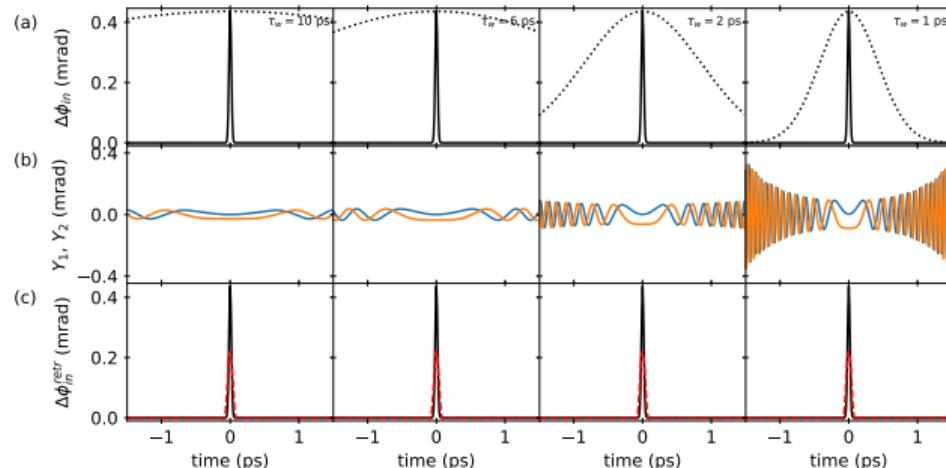


"Time resolution" of DEOS

Time resolution of DEOS: $\tau_R^{DEOS} \equiv \tau_{THz}^{retrieved}$ when $\tau_{THz} = \tau_L$

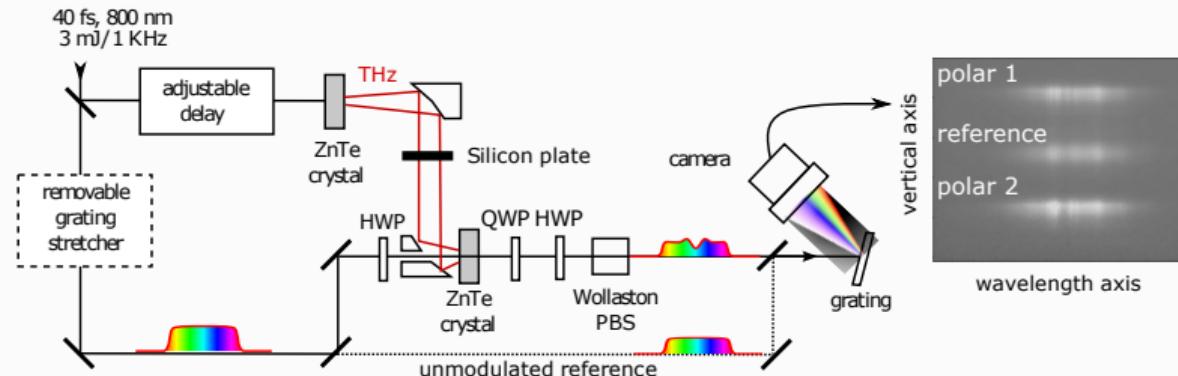


DEOS reconstruction versus time window τ_w :

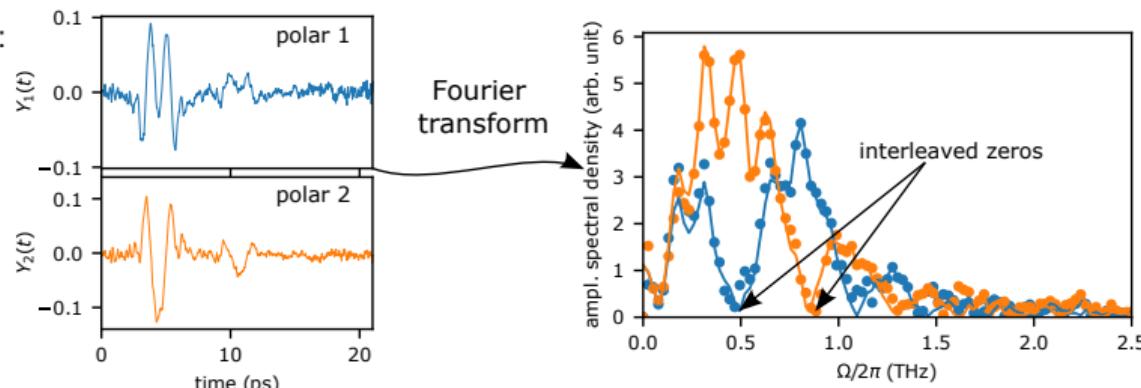


Experimental investigations using a table-top experiment

Terahertz signal generated by optical rectification of laser pulses

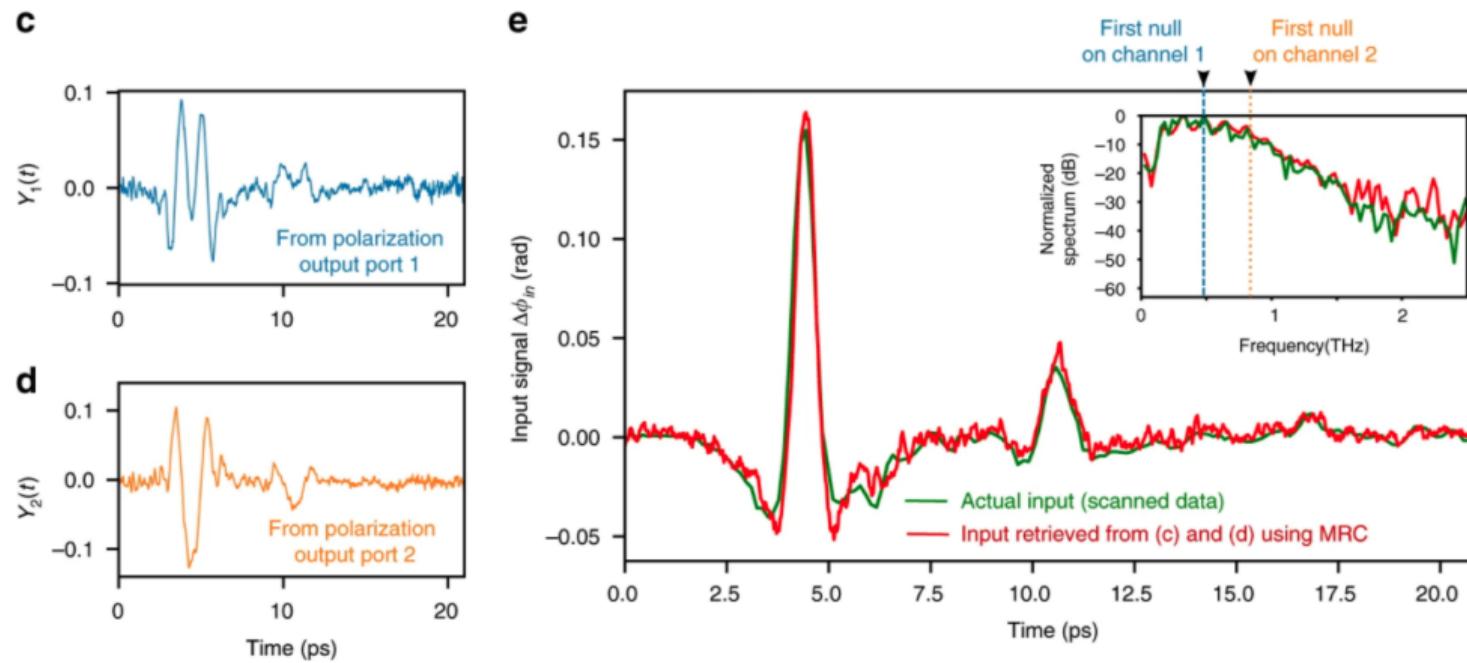


Computed EO signals:

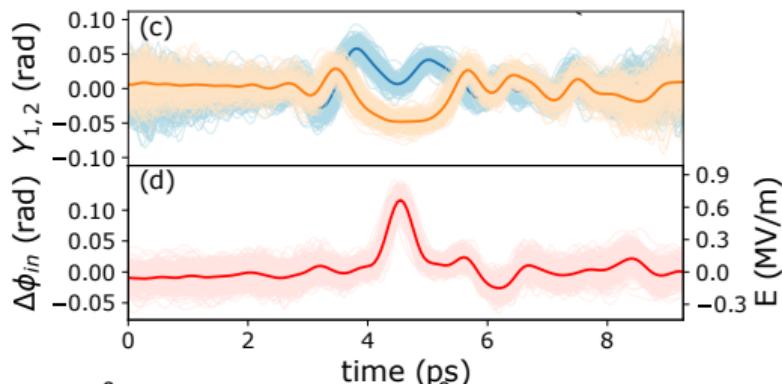
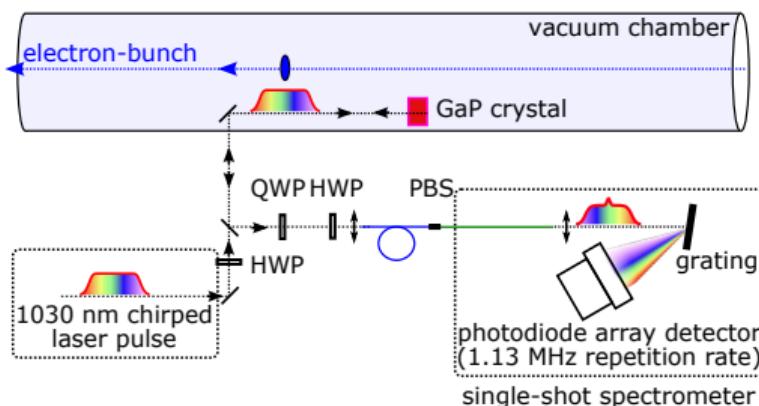


Comparison between DEOS and scanned EOS

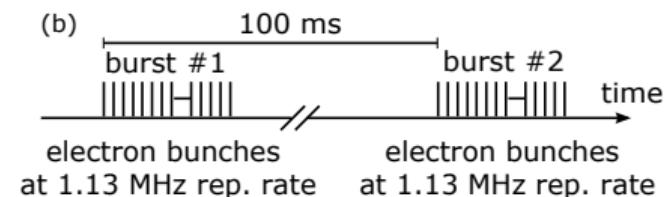
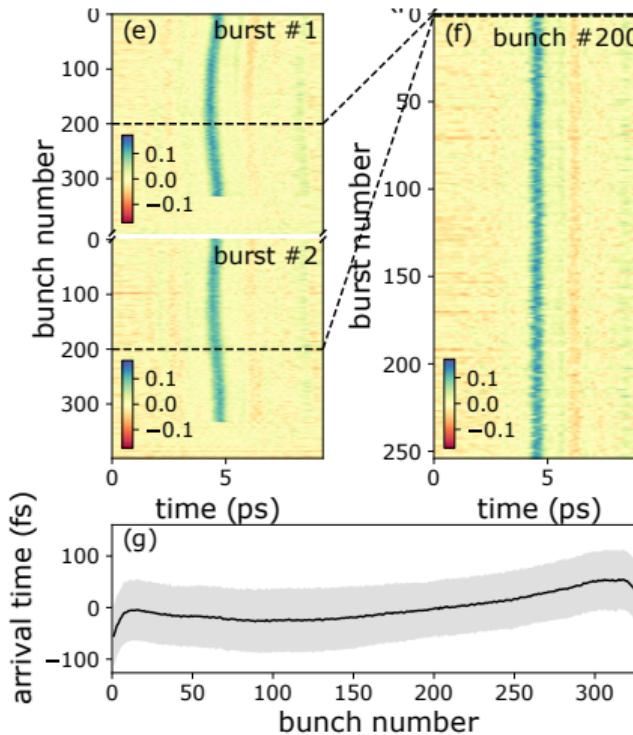
Reconstructed single-shot THz signal vs reference signal (obtained with scanned EOS)



Studies of e-bunch shapes at the European XFEL



Preliminary results at the European XFEL



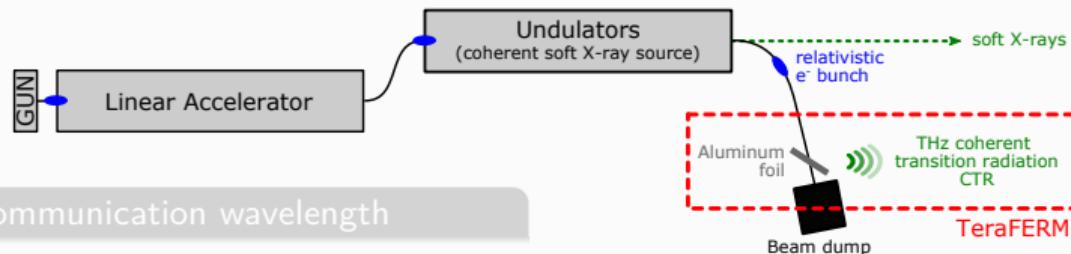
Train of 300 e-bunches over 250 bursts.

- bunch duration: ~ 218 fs RMS
- arrival time jitter: ~ 58 fs

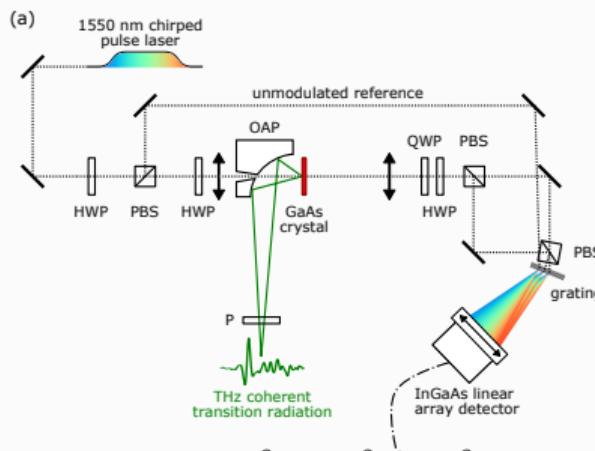
TeraFERMI: a "parasitic" THz source

TeraFERMI (Italy)

Single-cycle THz pulses from the coherent transition radiation (CTR) emitted by a short relativistic e-beam passing through a 1 μm thick Al foil. [A. Perucchi et al., Rev. Sci. Instrum. 84, 022702 (2013)]



THz TDS at telecommunication wavelength



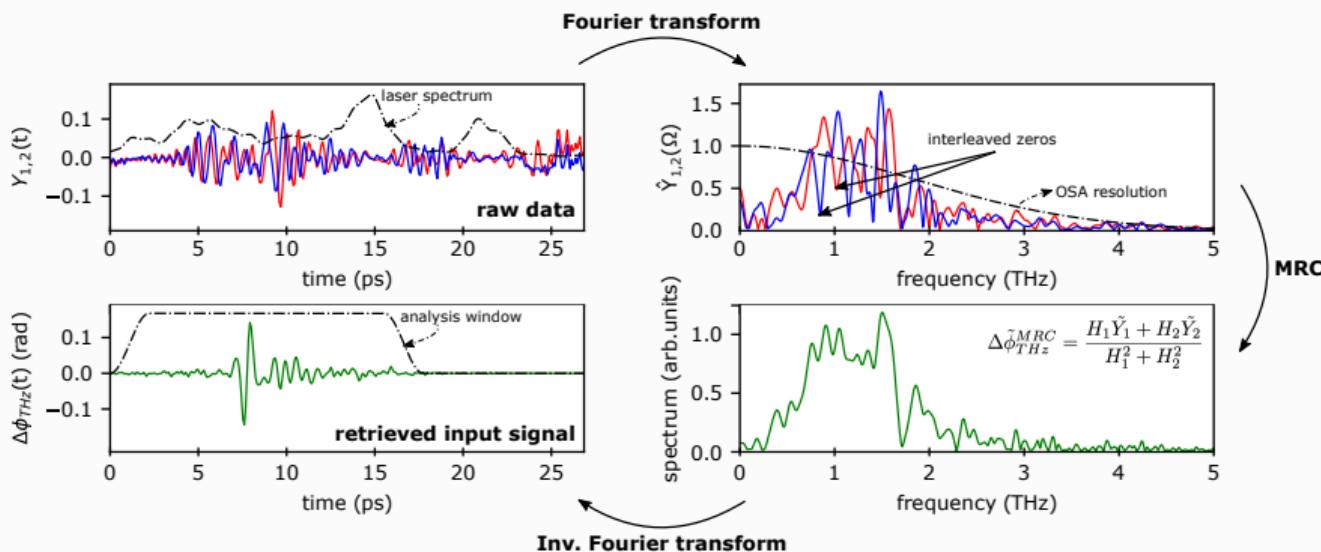
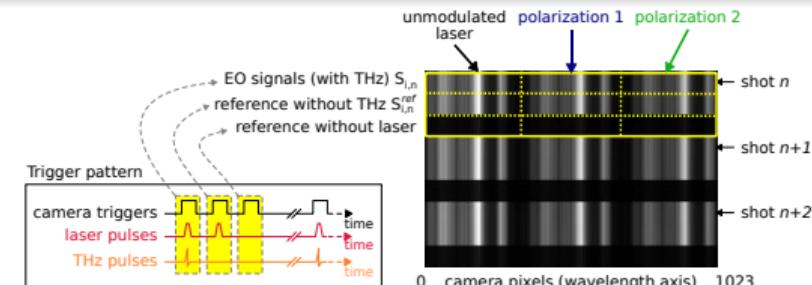
Energy per pulse	$\geq 10 \mu\text{J}$ ☺
Pulse duration	$\leq 1 \text{ ps}$
Frequency range	1 – 10 THz
THz e-field strength	$\sim 50 \text{ MV/m}$ ☺
Repetition rate	50 Hz ☹

High peak power THz CTR recording

At each FERMI clock (@50 Hz):

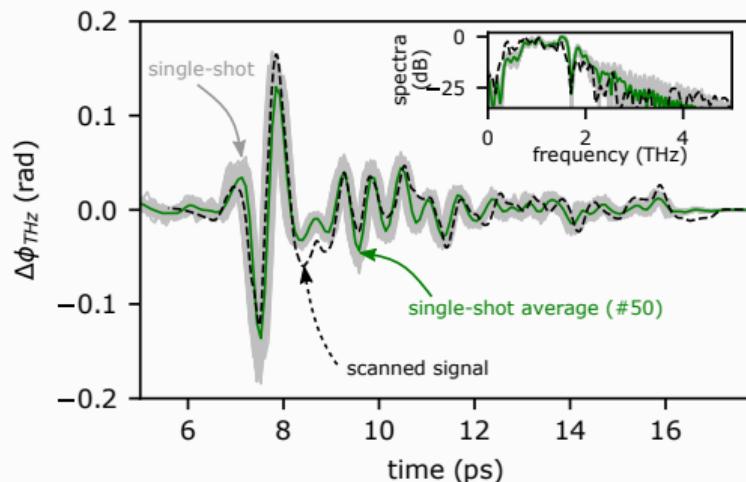
- 1 laser pulse modulated by THz signal
- 1 reference laser pulse, i.e. unmodulated
- 1 camera background

[Roussel et al., Opt. Express 31, 31072 (2023)]



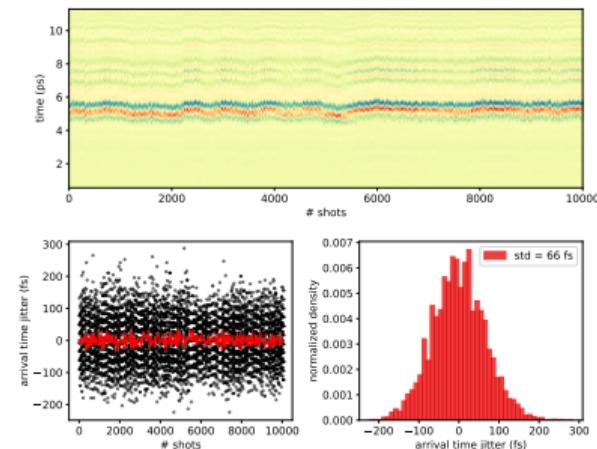
Comparison with scanning technique

Scanned signal obtained by passing the optical stretcher (laser pulse duration ~ 110 fs).



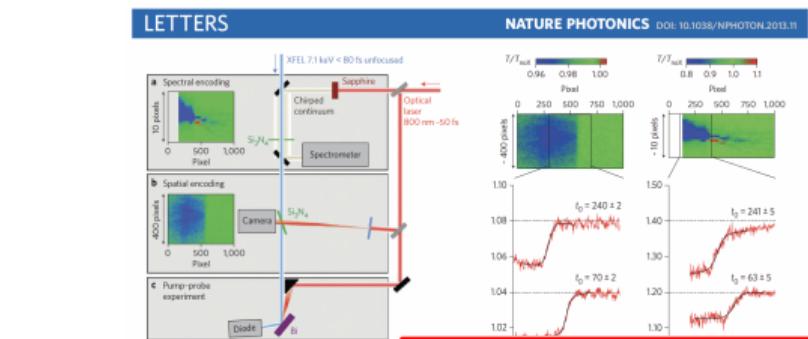
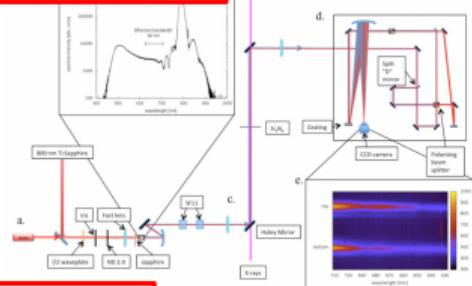
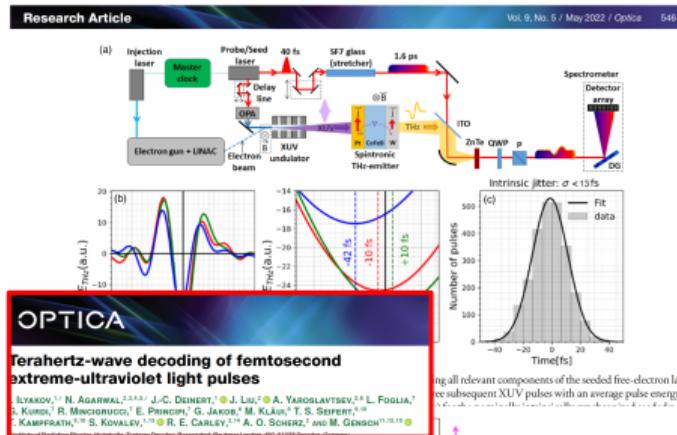
The scanning technique is sensitive to the time jitter between the THz signal and the laser pulse.

- e-bunch arrival time jitter: ~ 40 fs
- + jitter of laser synchronization loop

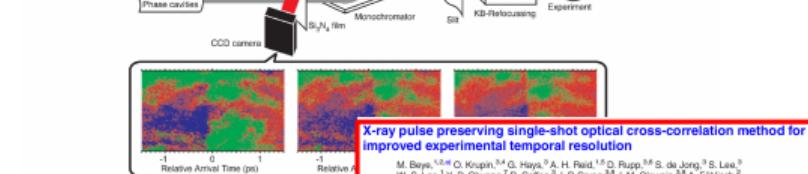


→ Measured time jitter of ~ 66 fs.

Potential applications for fs-XUV light pulses characterization ?



121108-2 Beye et al.



Conclusion

Diversity Electro-Optic Sampling (DEOS)

- ▷ High temporal resolution (limited by laser and crystal) for arbitrary long windows.
- ▷ Table-top proof-of-principle tests + experiments in accelerator environments.

Related projects in machine physics

- ▷ PhLAM/DESY project: investigate DEOS + photonic time-stretch readout
- ▷ PhLAM/FERMI: TeraFERMI THz beamline (high power, low rep. rate source)
- ▷ PhLAM/KARA/SOLEIL (French-German ANR-DFG ULTRASYNC project).
- ▷ Feasibility studies at TELBE and FELBE.
- ▷ Advanced diagnostics for the European TWAC project (THz Waveguide Accelerating Cavity).

Other milestones

- ▷ High acquisition rate with photonic time-stretch readout. [[Roussel, et al., Sci Rep 5, 10330 \(2015\)](#)]
- ▷ High sensitivity EOS. [[SzwaJ et al., Rev. Sci. Instrum. 87, 103111 \(2016\)](#)]
- ▷ Cost reduction, using 1550 nm wavelength. [[Roussel et al., Opt. Express 31, 31072 \(2023\)](#)]

Acknowledgement

Collaboration



UCLA: B. Jalali,

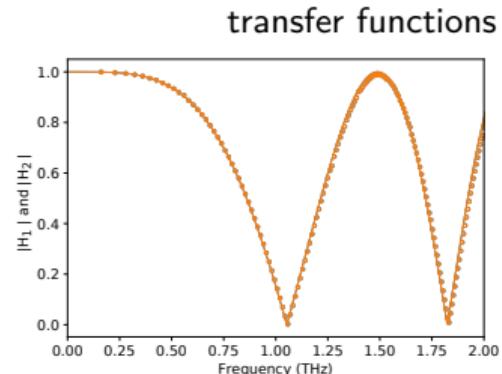
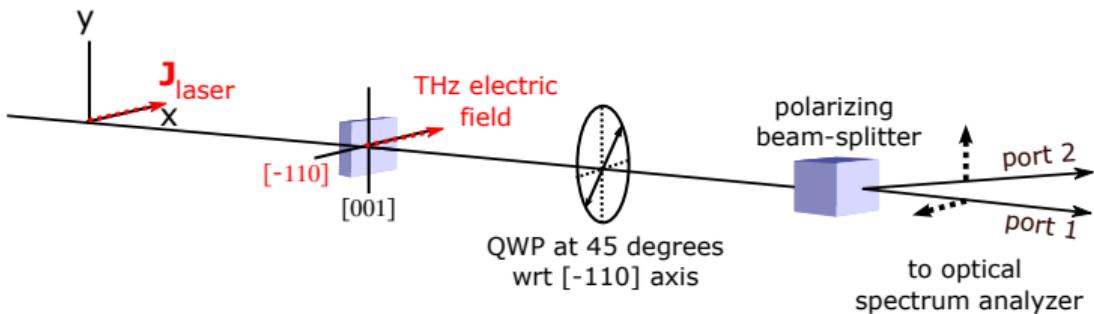
EuXFEL: B. Steffen, C. Gerth ,

FERMI: P. Di Pietro, N. Adhlakha, P. Cinquegrana, M. Veronese, S. Di Mitri, A. Perucchi

Fundings

CPER Photonics4Society, CEMPI, CNRS Momentum (METEOR), ANR/DFG (ULTRASYNC), EIC Pathfinder (TWAC).

"Classical" EO configuration



Transfer functions $H_{1,2}$ for the "classical" crystal & waveplates orientations

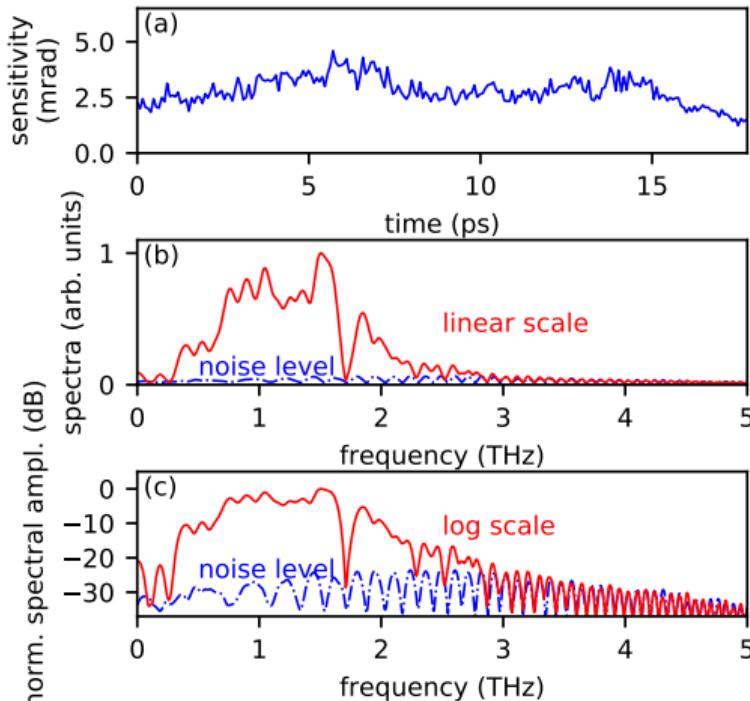
$$H_1(\Omega) = \cos(B\Omega^2)$$

$$H_2(\Omega) = -\cos(B\Omega^2)$$

- clear existence of **zeros** at particular frequencies
problem ill-posed → "deconvolution" impossible using one channel
- "classical" EO configuration: zeros of H_1 and H_2 at the same frequencies

→ find an other configuration to separate the zeros ?

Sensitivity and dynamic range (TeraFERMI TDS setup 1550)



- RMS noise fluctuation (estimated from data without THz signal): **2.5 mrad over 5 THz bandwidth**
- ≡ Noise-equivalent input e-field: **2.1 kV/cm** (crystal thickness $d = 100 \mu\text{m}$!)

$$\Delta\phi = \frac{\pi d}{\lambda} n_0^3 r_{41} E_{\text{THz}}$$

- Dynamic range: $\sim 30 \text{ dB}$