

# High-Accuracy Partially- and Fully-Coherent Wavefront Propagation Calculations for Storage Ring and FEL Sources



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# Outline

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- Basics of Synchrotron Radiation (SR) calculation
- Basics of radiation Wavefront Propagation using Fourier Optics and compatible methods
- SR calculation examples; comparison with experiments
- Examples of Partially-Coherent SR propagation calculations for beamlines in Low-Emittance storage rings
- Example of Time-/Frequency-dependent Wavefront Propagation calculation for X-FEL applications
- Summary and comments

# Emission by a Relativistic Charged Particle in Free Space: Retarded Potentials Approach

$$\vec{A} = e \int_{-\infty}^{+\infty} \vec{\beta}_e R^{-1} \delta(\tau - t + R/c) d\tau, \quad \varphi = e \int_{-\infty}^{+\infty} R^{-1} \delta(\tau - t + R/c) d\tau \quad (\text{Gaussian CGS})$$

$$\Downarrow \quad \delta(t') = (1/2\pi) \int_{-\infty}^{+\infty} \exp(i\omega t') d\omega$$

$$\vec{A} = \frac{e}{2\pi} \int_{-\infty}^{+\infty} \exp(-i\omega t) d\omega \int_{-\infty}^{+\infty} \vec{\beta}_e R^{-1} \exp[i\omega(\tau + R/c)] d\tau$$

$$\varphi = \frac{e}{2\pi} \int_{-\infty}^{+\infty} \exp(-i\omega t) d\omega \int_{-\infty}^{+\infty} R^{-1} \exp[i\omega(\tau + R/c)] d\tau$$

Ternov used this approach to derive far-field SR expressions

$$\vec{E} = -\frac{1}{c} \frac{\partial \vec{A}}{\partial t} - \nabla \varphi = \frac{ie}{2\pi c} \int_{-\infty}^{+\infty} \omega \cdot \exp(-i\omega t) d\omega \int_{-\infty}^{+\infty} [\vec{\beta}_e - [1 + ic/(\omega R)] \cdot \vec{n}] R^{-1} \exp[i\omega(\tau + R/c)] d\tau$$

$$\Downarrow \quad \vec{E}_\omega = \int_{-\infty}^{+\infty} \vec{E} \exp(i\omega t) dt$$

Exact expression, valid in the Near Field:

$$\vec{E}_\omega = iec^{-1} \omega \int_{-\infty}^{+\infty} [\vec{\beta}_e - [1 + ic/(\omega R)] \cdot \vec{n}] R^{-1} \exp[i\omega(\tau + R/c)] d\tau \quad (\checkmark)$$

The equivalence of (✓) to the well-known expression of Jackson can be shown by integration by parts

$$\vec{E}_\omega = ec^{-1} \int_{-\infty}^{+\infty} \frac{\vec{n} \times [(\vec{n} - \vec{\beta}_e) \times \dot{\vec{\beta}}_e] + cR^{-1} \gamma^{-2} (\vec{n} - \vec{\beta}_e)}{R \cdot (1 - \vec{n} \cdot \vec{\beta}_e)^2} \cdot \exp[i\omega(\tau + R/c)] d\tau$$

# Emission by a Relativistic Charged Particle Efficient Computation

Exact expression obtained from Retarded Potentials:

$$\vec{E}_\omega = iec^{-1}\omega \int_{-\infty}^{+\infty} [\vec{\beta}_e - [1 + ic/(\omega R)] \cdot \vec{n}] R^{-1} \exp[i\omega(\tau + R/c)] d\tau$$

Phase expansion valid in the Near Field:

$$\omega \cdot (\tau + R/c) \approx \Phi_0 + \frac{\pi}{\lambda} \left[ s\gamma^{-2} + \int_0^s |\vec{\beta}_{e\perp}|^2 d\tilde{s} + \frac{(x-x_e)^2 + (y-y_e)^2}{z-s} \right]$$

Particle dynamics in external magnetic field:

$$\vec{r}_e = \vec{r}_e(s, \vec{r}_{e0}, \vec{\beta}_{e0}); \quad \vec{\beta}_e \approx d\vec{r}_e/ds$$

Asymptotic expansion of the radiation integral (to accelerate computation):

$$\begin{aligned} \int_{-\infty}^{+\infty} F \exp(i\Phi) ds &= \int_{s_1}^{s_2} F \exp(i\Phi) ds + \int_{-\infty}^{s_1} F \exp(i\Phi) ds + \int_{s_2}^{+\infty} F \exp(i\Phi) ds \\ \int_{-\infty}^{s_1} F \exp(i\Phi) ds + \int_{s_2}^{+\infty} F \exp(i\Phi) ds &\approx \left[ \left( \frac{F}{i\Phi'} + \frac{F'\Phi' - F\Phi''}{\Phi'^3} + \dots \right) \exp(i\Phi) \right]_{s_2}^{s_1} \end{aligned}$$



# Temporally-Incoherent and Coherent Spontaneous Emission by Many Electrons

**Electron Dynamics:**

$$\begin{pmatrix} x_e \\ y_e \\ z_e \\ \beta_{xe} \\ \beta_{ye} \\ \delta\gamma_e \end{pmatrix} = \mathbf{A}(\tau) \begin{pmatrix} x_{e0} \\ y_{e0} \\ z_{e0} \\ x'_{e0} \\ y'_{e0} \\ \delta\gamma_{e0} \end{pmatrix} \leftarrow \text{Initial Conditions} + \mathbf{B}(\tau)$$

**Spectral Photon Flux per unit Surface emitted by the whole Electron Beam:**

$$\frac{dN_{ph}}{dtdS(d\omega/\omega)} = \frac{c^2 \alpha I}{4\pi^2 e^3} \langle |\vec{E}_\omega|^2 \rangle$$

**“Incoherent” SR**

$$\langle |\vec{E}_\omega|^2 \rangle = \int |\vec{E}_{\omega 0}(\vec{r}; x_{e0}, y_{e0}, z_{e0}, x'_{e0}, y'_{e0}, \delta\gamma_{e0})|^2 f(x_{e0}, y_{e0}, z_{e0}, x'_{e0}, y'_{e0}, \delta\gamma_{e0}) dx_{e0} dy_{e0} dz_{e0} dx'_{e0} dy'_{e0} d\delta\gamma_{e0} +$$

$$+ (N_e - 1) \left| \int \vec{E}_{\omega 0}(\vec{r}; x_{e0}, y_{e0}, z_{e0}, x'_{e0}, y'_{e0}, \delta\gamma_{e0}) f(x_{e0}, y_{e0}, z_{e0}, x'_{e0}, y'_{e0}, \delta\gamma_{e0}) dx_{e0} dy_{e0} dz_{e0} dx'_{e0} dy'_{e0} d\delta\gamma_{e0} \right|^2$$

**Coherent SR**

**Common Approximation for CSR: “Thin” Electron Beam:**  $\langle |\vec{E}_\omega|^2 \rangle_{CSR} \approx N_e \left| \int_{-\infty}^{\infty} \tilde{f}(z_{e0}) \exp(ikz_{e0}) dz_{e0} \right|^2 |\vec{E}_{\omega 1}|^2$

**For Gaussian Longitudinal Bunch Profile:**  $\langle |\vec{E}_\omega|^2 \rangle_{CSR} \approx N_e \exp(-k^2 \sigma_b^2) |\vec{E}_{\omega 1}|^2$

If  $f(x_{e0}, y_{e0}, z_{e0}, x'_{e0}, y'_{e0}, \delta\gamma_{e0})$  is Gaussian, 6-fold integration over electron phase space can be done analytically for the (Mutual) Intensity of Incoherent SR and for the Electric Field of CSR

# Self-Amplified Spontaneous Emission Described by Paraxial FEL Equations

## Approximation of Slowly Varying Amplitude of Radiation Field

Particles' dynamics  
in undulator and radiation fields  
(averaged over many periods):

$$\frac{d\theta}{dz} = k_u - k_r \frac{1 + p_{\perp}^2 + a_u^2 - 2a_r a_u \cos(\theta + \phi_r)}{2\gamma^2}$$

$$\frac{d\gamma}{dz} = -\frac{k_r f_c a_r a_u}{\gamma} \sin(\theta + \phi_r)$$

$$\frac{d\vec{p}_{\perp}}{dz} = -\frac{1}{2\gamma} \frac{\partial a_u^2}{\partial \vec{r}_{\perp}} + \mathbf{k}_{foc} \vec{r}_{\perp}$$

$$\frac{d\vec{r}_{\perp}}{dz} = \frac{\vec{p}_{\perp}}{\gamma}$$

W.B.Colson  
J.B.Murphy  
C.Pellegrini  
E.Saldin  
E.Bessonov  
et. al.

Paraxial wave equation  
with current:

$$\left[ 2ik_r \frac{\partial}{\partial z} + \nabla_{\perp}^2 \right] a_r \exp(i\phi_r) = -\frac{e\epsilon_0 I f_c a_u}{mc} \left\langle \frac{\exp(-i\theta)}{\gamma} \right\rangle$$

Solving this system gives Electric Field at the FEL exit for one "Slice":  $E_{slice}|_{z=z_{exit}} \sim a_r \exp(i\phi_r)|_{z=z_{exit}}$

Loop on "Slices" (copying Electric Field to a next slice from previous slice, starting from back)

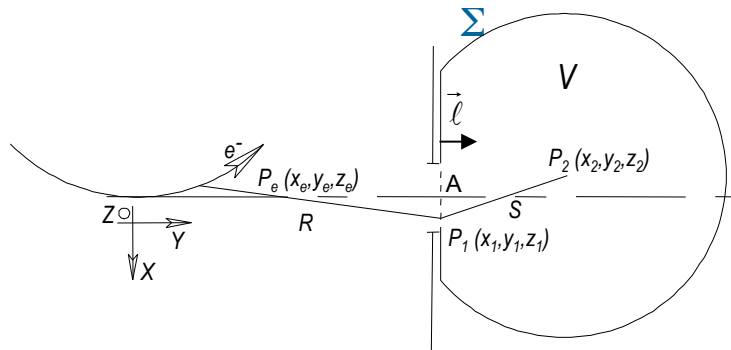
Popular TD 3D FEL computer code: **GENESIS** (S.Reiche)

One run provides Time-Domain Electric Field in transverse plane at FEL exit:  $E(x, y, z_{exit}, t)$

Electric Field in **Frequency** domain:  $\vec{E}(\vec{r}, \omega) \equiv \int_{-\infty}^{\infty} \vec{E}(\vec{r}, t) \exp(i\omega t) dt$

# Wavefront Propagation in the Case of Full Transverse Coherence

## Kirchhoff Integral Theorem applied to Spontaneous Emission by One Electron



$$\vec{E}_{\omega 2\perp}(P_2) \approx \frac{k^2 e}{4\pi} \int_{-\infty}^{+\infty} d\tau \iint_A \frac{\vec{\beta}_{e\perp} - \vec{n}_{\perp}}{RS} \exp[ik(c\tau + R + S)] \cdot (\vec{l} \cdot \vec{n}_{P_e P_1} + \vec{l} \cdot \vec{n}_{P_1 P_2}) d\Sigma$$

Valid at large observation angles;

Is applicable to complicated cases of diffraction inside vacuum chamber

## Huygens-Fresnel Principle

$$\vec{E}_{\omega 2\perp}(P_2) \approx \frac{k}{4\pi i} \iint_A \vec{E}_{\omega 1\perp}(P_1) \frac{\exp(ikS)}{S} (\vec{l} \cdot \vec{n} + \vec{l} \cdot \vec{n}_{P_1 P_2}) d\Sigma$$

## Fourier Optics

**Free Space:**  
(between parallel planes  
perpendicular to optical axis)

$$\vec{E}_{\omega 2\perp}(x_2, y_2) \approx \frac{k}{2\pi i L} \iint \vec{E}_{\omega 1\perp}(x_1, y_1) \exp[ik[L^2 + (x_2 - x_1)^2 + (y_2 - y_1)^2]^{1/2}] dx_1 dy_1$$

Assumption of small angles

**“Thin” Optical Element:**

$$\vec{E}_{\omega 2\perp}(x, y) \approx \mathbf{T}(x, y, \omega) \vec{E}_{\omega 1\perp}(x, y)$$

**“Thick” Optical Element:**  
(propagation from transverse  
plane before the element to a  
transverse plane just after it)

$$\vec{E}_{\omega 2\perp}(x_2, y_2) \approx \mathbf{G}(x_2, y_2, \omega) \exp[ik\Lambda(x_2, y_2, k)] \vec{E}_{\omega 1\perp}(x_1(x_2, y_2), y_1(x_2, y_2))$$

# “Economic” and Numerically Stable Version of the Free-Space Fourier-Optics Propagator

## Huygens-Fresnel Principle:

(paraxial approximation)

$$\vec{E}_{\omega 2\perp}(x_2, y_2) \approx \frac{k}{2\pi i L} \iint \vec{E}_{\omega 1\perp}(x_1, y_1) \exp[ik[L^2 + (x_2 - x_1)^2 + (y_2 - y_1)^2]^{1/2}] dx_1 dy_1$$

## Analytical Treatment of Quadratic Phase Term:

Before Propagation:

$$\vec{E}_{\omega 1\perp}(x_1, y_1) = \vec{F}_{\omega 1}(x_1, y_1) \exp\left[ik \frac{(x_1 - x_0)^2}{2R_x} + ik \frac{(y_1 - y_0)^2}{2R_y}\right]$$

After Propagation:

$$\begin{aligned} \vec{E}_{\omega 2\perp}(x_2, y_2) &\approx \frac{k}{2\pi i L} \exp(ikL) \iint_{\Sigma} \vec{F}_{\omega 1}(x_1, y_1) \exp\left[ik \frac{(x_1 - x_0)^2}{2R_x} + ik \frac{(y_1 - y_0)^2}{2R_y} + ik \frac{(x_2 - x_1)^2 + (y_2 - y_1)^2}{2L}\right] dx_1 dy_1 \\ &= \frac{k}{2\pi i L} \exp\left[ikL + ik \frac{(x_2 - x_0)^2}{2(R_x + L)} + ik \frac{(y_2 - y_0)^2}{2(R_y + L)}\right] \times \\ &\times \iint_{\Sigma} \vec{F}_{\omega 1}(x_1, y_1) \exp\left[ik \frac{R_x + L}{2R_x L} \left(x_1 - \frac{R_x x_2 + Lx_0}{R_x + L}\right)^2 + ik \frac{R_y + L}{2R_y L} \left(y_1 - \frac{R_y y_2 + Ly_0}{R_y + L}\right)^2\right] dx_1 dy_1 \\ &= \vec{F}_{\omega 2}(x_2, y_2) \exp\left[ik \frac{(x_2 - x_0)^2}{2(R_x + L)} + ik \frac{(y_2 - y_0)^2}{2(R_y + L)}\right] \end{aligned}$$



# An Approach to High-Accuracy Partially-Coherent Emission and Wavefront Propagation Simulations

**Averaging** (over phase-space volume occupied by e-beam) of the intensity (or mutual intensity, or mathematical brightness) obtained from electric field emitted by an electron and propagated through an optical system:

$$I_{\omega}(x, y) = \int I_{\omega 1}(x, y; x_e, y_e, z_e, x'_e, y'_e, \delta\gamma_e) f(x_e, y_e, z_e, x'_e, y'_e, \delta\gamma_e) dx_e dy_e dz_e dx'_e dy'_e d\delta\gamma_e$$

$$I_{\omega 1}(x, y; x_e, y_e, z_e, x'_e, y'_e, \delta\gamma_e) = |\mathbf{E}_{\omega 1\perp}(x, y; x_e, y_e, z_e, x'_e, y'_e, \delta\gamma_e)|^2$$

$$M_{\omega 1}(x, y, \tilde{x}, \tilde{y}; x_e, y_e, z_e, x'_e, y'_e, \delta\gamma_e) = \mathbf{E}_{\omega 1\perp}(x, y; x_e, y_e, z_e, x'_e, y'_e, \delta\gamma_e) \mathbf{E}_{\omega 1\perp}^*(\tilde{x}, \tilde{y}; x_e, y_e, z_e, x'_e, y'_e, \delta\gamma_e)$$

$$B_{\omega 1}(x, y, \theta_x, \theta_y; x_e, y_e, z_e, x'_e, y'_e, \delta\gamma_e) \sim \mathbf{E}_{\omega 1\perp}(x, y; x_e, y_e, z_e, x'_e, y'_e, \delta\gamma_e) \int \mathbf{E}_{\omega 1\perp}^*(\tilde{x}, \tilde{y}; x_e, y_e, z_e, x'_e, y'_e, \delta\gamma_e) \exp\left[i\frac{\omega}{c}(\theta_x \tilde{x} + \theta_y \tilde{y})\right] d\tilde{x} d\tilde{y}$$

This method is **general and accurate**. For the most part, it is already implemented in SRW code. However, it can be **CPU-intensive**, requiring **parallel calculations** on a multi-core server or a small cluster. Several approaches are considered for increasing the efficiency, including use of low-discrepancy sequences (collaboration with R. Lindberg, K.-J. Kim, X. Shi, ANL), “improved Monte-Carlo” type techniques, as well as “coherent mode decomposition”.

**NOTE:** the **smaller** the **e-beam emittance** (the higher the radiation coherence) – the **faster** is the **convergence** of simulations with this general method.

**NOTE:** **convolution** can be valid in some cases, such as pure projection geometry, focusing by a thin lens, diffraction at one slit, etc.

$$I_{\omega}(x, y) \approx \int \tilde{I}_{\omega 1}(x - \tilde{x}_e, y - \tilde{y}_e) \tilde{f}(\tilde{x}_e, \tilde{y}_e) d\tilde{x}_e d\tilde{y}_e$$

If convolution is valid, the **calculations can be accelerated** dramatically. The validity of the convolution relation can be easily verified numerically.

# All calculations presented below were done with “Synchrotron Radiation Workshop” code


First work on Wavefront Propagation applied to SR beamlines (PHASE code):  
**J. Bahrtdt, Appl. Opt. 36 (19) 4367 (1997)**

- First official version of SRW was developed at ESRF in 1997-98 (written in C++, interfaced to IGOR Pro); compiled versions are distributed from:  
<http://www.esrf.eu/Accelerators/Groups/InsertionDevices/Software/SRW>
- SRW was released to Open Source in 2012 under BSD type license. To make the release possible, permissions were obtained from all previously contributed Institutes: ESRF, European XFEL, SOLEIL, DIAMOND, BNL, and from US DOE



The main Open Source repository, containing all C/C++ sources, C API, all interfaces and project development files, is on GitHub:

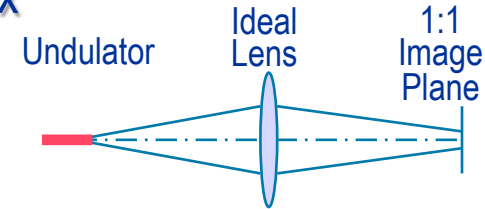
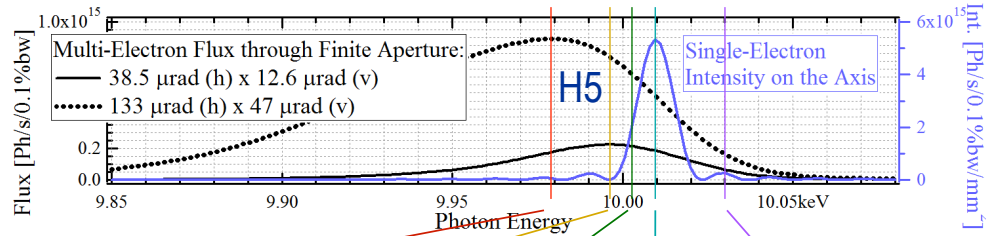
<https://github.com/ochubar/SRW>

- SRW for Python (2.7.x and 3.x, 32- and 64-bit) cross-platform versions were released in 2012
- SRW development is partially supported by US DOE SBIR Program (BNL acts as subcontractor of RadiaSoft LLC, headed by D. Bruhwiler) 

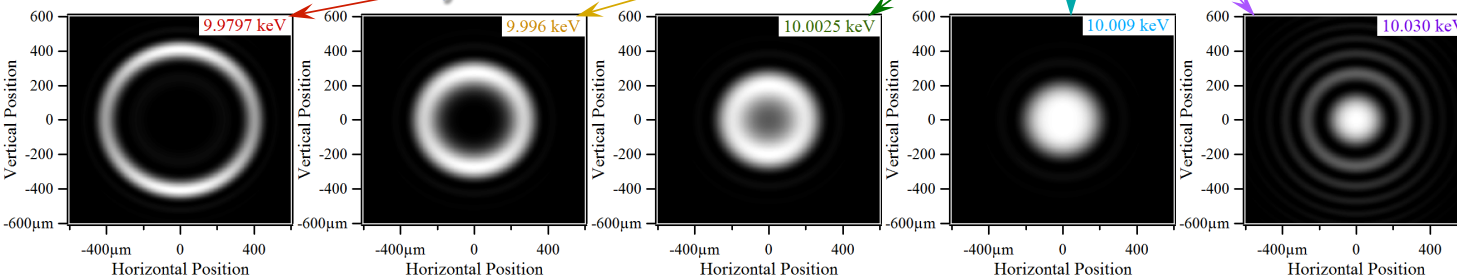
# Single-Electron (Fully Transversely-Coherent) UR Intensity Distributions, “in Far Field” and “at Source”

## UR “Single-Electron” Intensity and “Multi-Electron” Flux

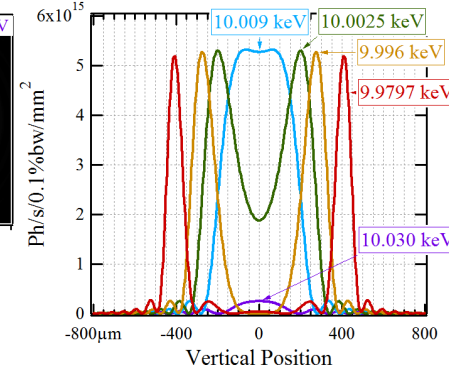
E-Beam Energy: 3 GeV  
Current: 0.5 A  
Undulator Period: 20 mm



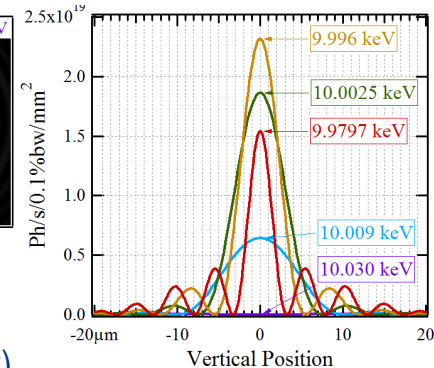
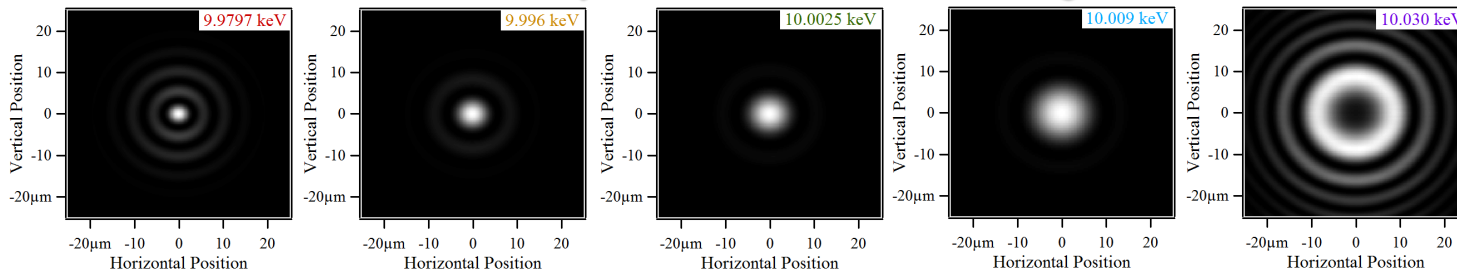
## Intensity Distributions at 30 m from Undulator Center



## Vertical Cuts (x = 0)



## Intensity Distributions in 1:1 Image Plane



## “Phase-Space Volume” Estimation for Vertical Plane

(RMS sizes/divergences calculated for the portions of intensity distributions containing 95% of flux)

$$\sigma_y \sigma_y' \approx 7.7 \frac{\lambda}{4\pi}$$

$$3.3 \frac{\lambda}{4\pi}$$

$$1.9 \frac{\lambda}{4\pi}$$

$$1.5 \frac{\lambda}{4\pi}$$

$$9.2 \frac{\lambda}{4\pi}$$

# “Phase Correction” for Coherent Radiation

“Real Wave Front” + “Phase Correction” = “Spherical Wave Front”

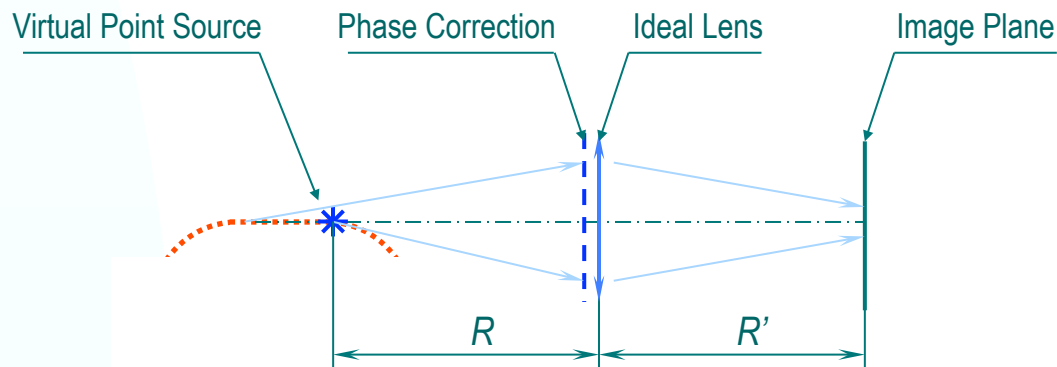
$$E_{out}(x, y) = T(x, y)E_{in}(x, y) = A(x, y) \exp[i\pi(x^2 + y^2)/(\lambda R)]$$

$$T(x, y) = \exp[i\Phi_{cor}(x, y)]$$



$$\Phi_{cor}(x, y) = \arg[\exp[i\pi(x^2 + y^2)/(\lambda R) + i\Phi_0]/E_{in}(x, y)]$$

## Testing Efficiency of Phase Corrections



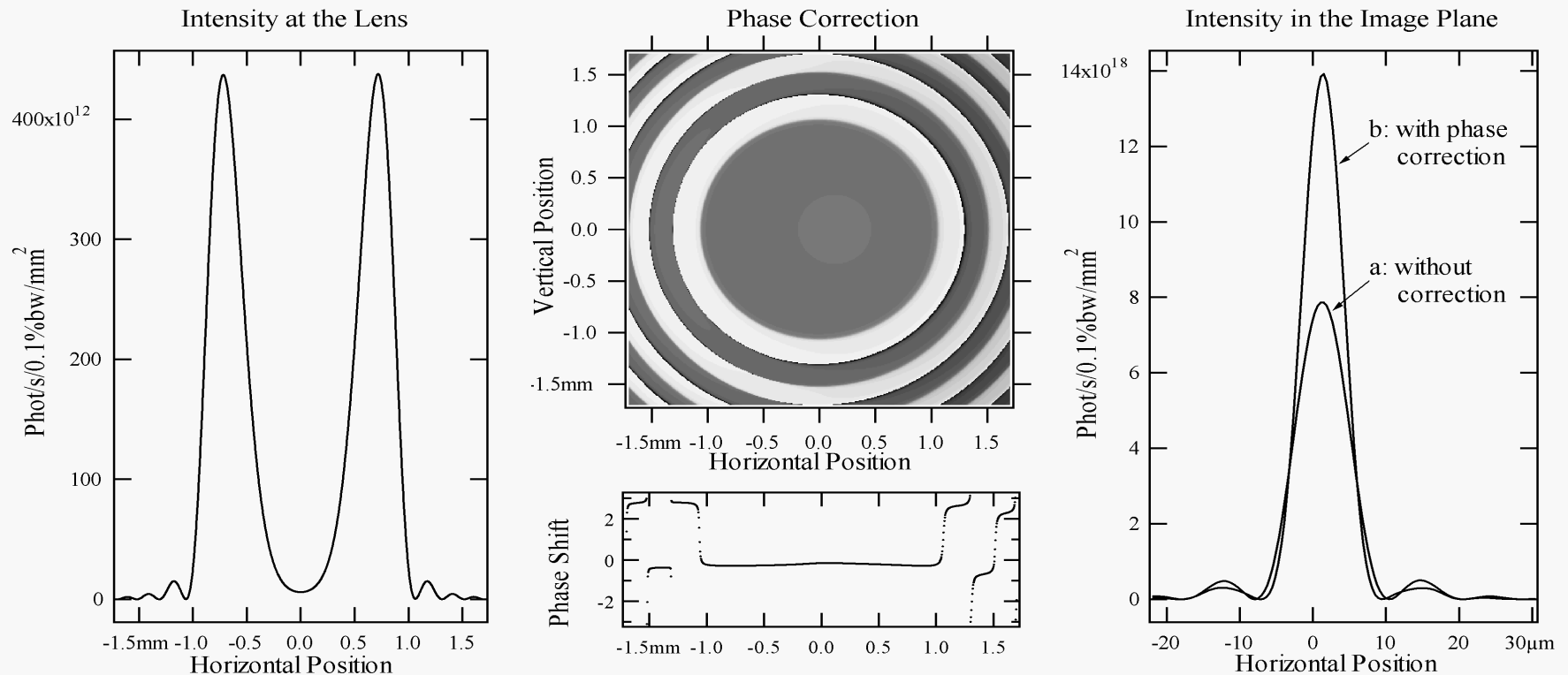


# Phase Corrections for Single-Electron UR (I)

## Planar undulator, odd harmonics

$E = 6$  GeV;  $K = 2.2$ ;  $38 \times 42$  mm;  $\varepsilon = 2.36$  keV ( $\sim$  fundamental)

1 : 1 imaging; 30 m from middle of Undulator to Thin Lens & Phase Correction

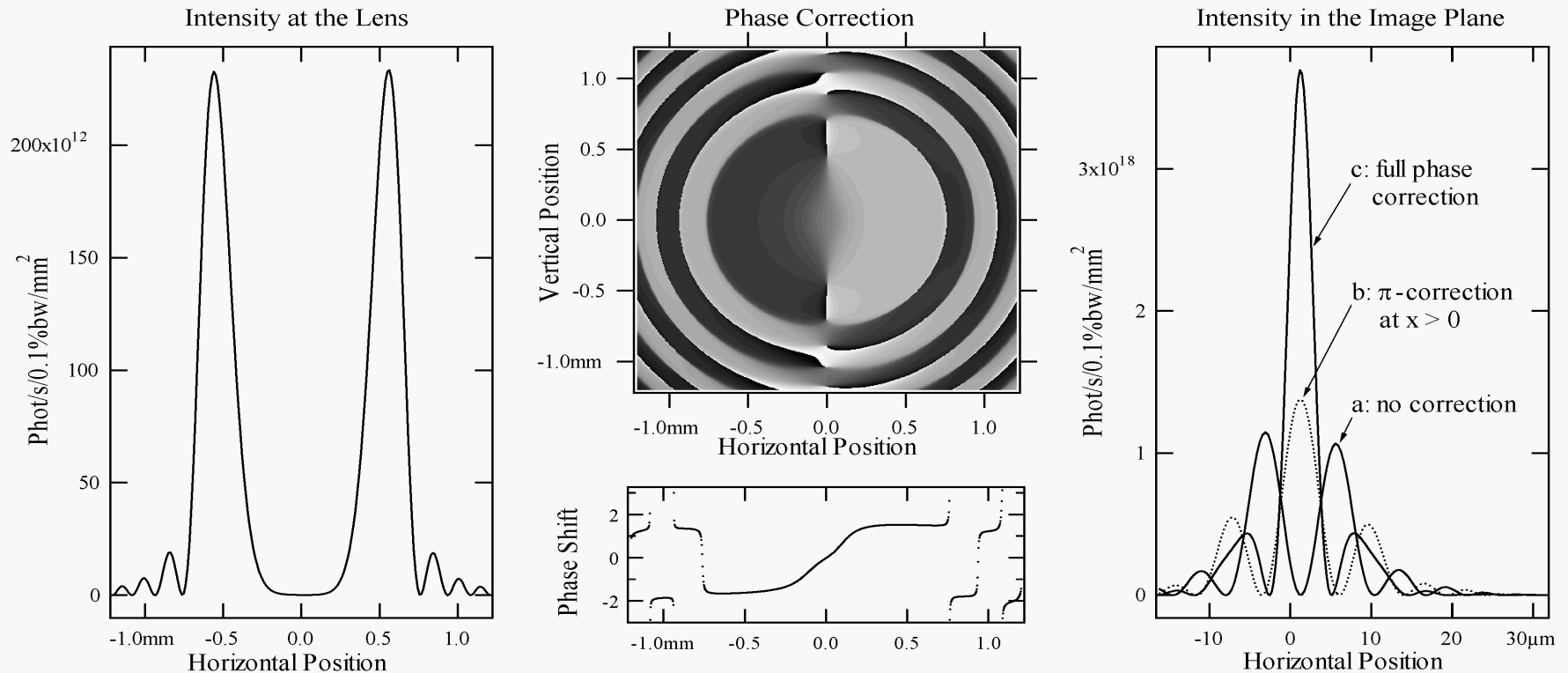


# Phase Corrections for Single-Electron UR (II)

## Planar undulator, even harmonics

$E = 6$  GeV;  $K = 2.2$ ;  $38 \times 42$  mm;  $\varepsilon = 4.775$  keV (2<sup>nd</sup> harmonic)

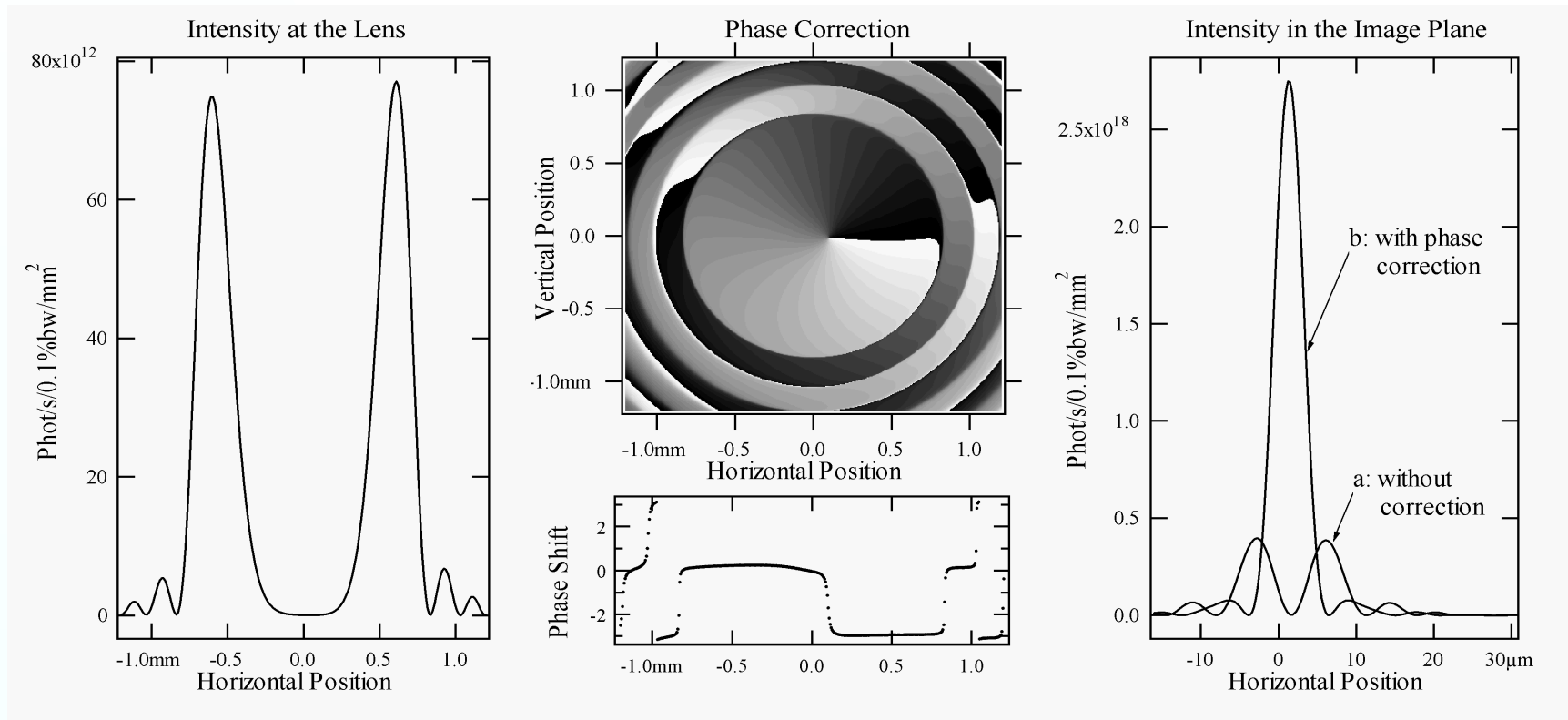
1 : 1 imaging; 30 m from middle of Undulator to Thin Lens & Phase Correction



# Phase Corrections for Single-Electron UR (III)

## Helical undulator, harmonics $n > 1$

$E = 6 \text{ GeV}$ ;  $B_{x \text{ max}} = B_{z \text{ max}} = 0.3 \text{ T}$ ;  $28 \times 52 \text{ mm}$ ;  $\varepsilon = 4.20 \text{ keV}$  (2<sup>nd</sup> harmonic)  
1 : 1 imaging; 30 m from middle of Undulator to Thin Lens & Phase Correction



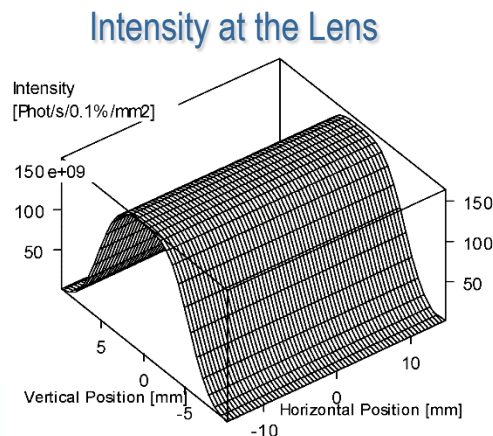
O. Chubar, P. Elleaume, A. Snigirev, NIMA 435 (1999) 495 - 508

S. Sasaki, I. McNulty, PRL 100, 124801 (2008) interpreted of this effect – azimuthal phase dependence – as “Orbital Angular Momentum”; several other publications followed.

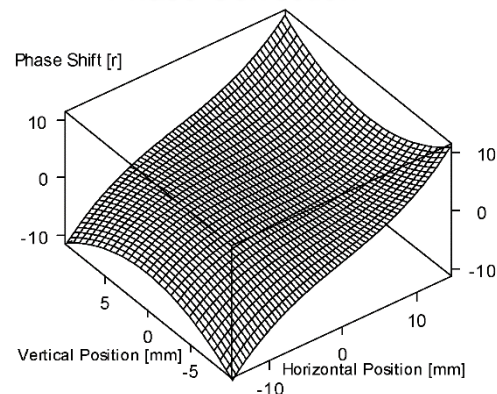
# Phase Corrections for Bending Magnet SR

$E = 2.5 \text{ GeV}$   
 $B = 1.6 \text{ T}$   
 $\varepsilon = 40 \text{ eV}$   
 $5 \text{ m from source}$

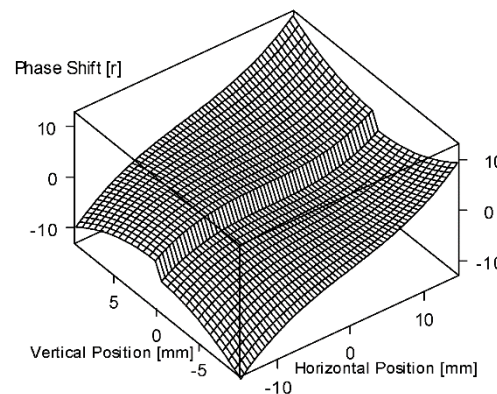
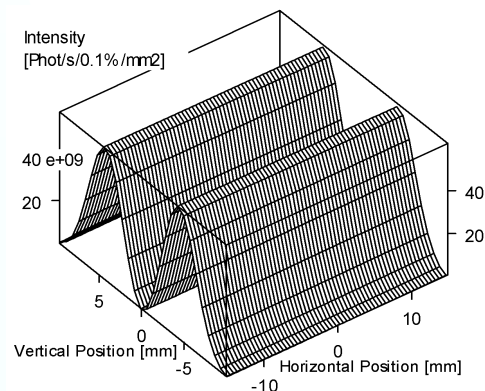
Horizontal  
Polarization



Phase Correction



Vertical  
Polarization



Analytical Approximation:

$$\Phi_{cor BM hor} \approx -(\pi/\lambda)\rho\theta_x(\gamma^{-2} + \theta_x^2/3 + \theta_y^2)$$

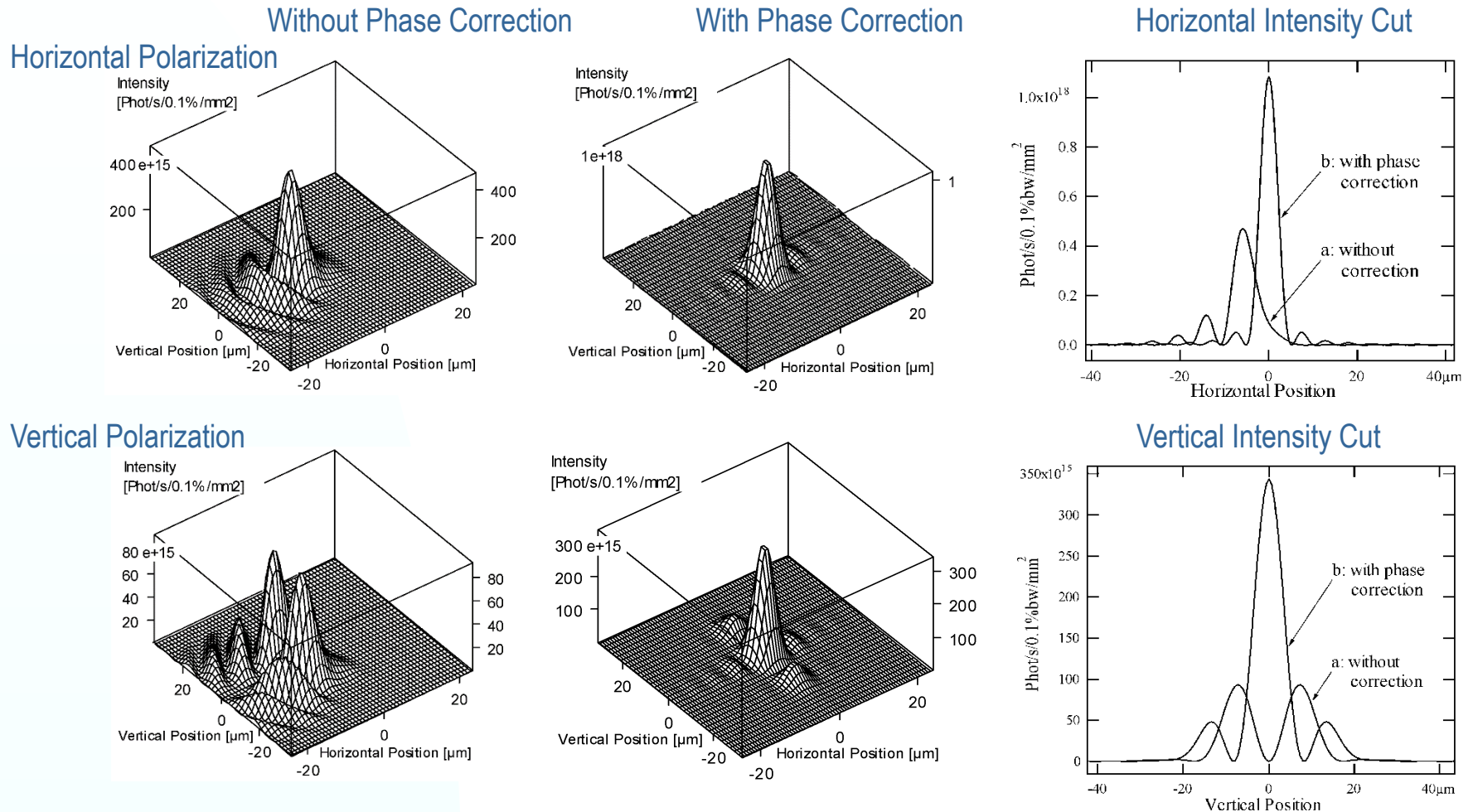
$$\Phi_{cor BM vert} = \Phi_{cor BM hor} + \pi\eta(\theta_y)$$



# Phase Corrections for Bending Magnet SR

## Intensity in the Image Plane

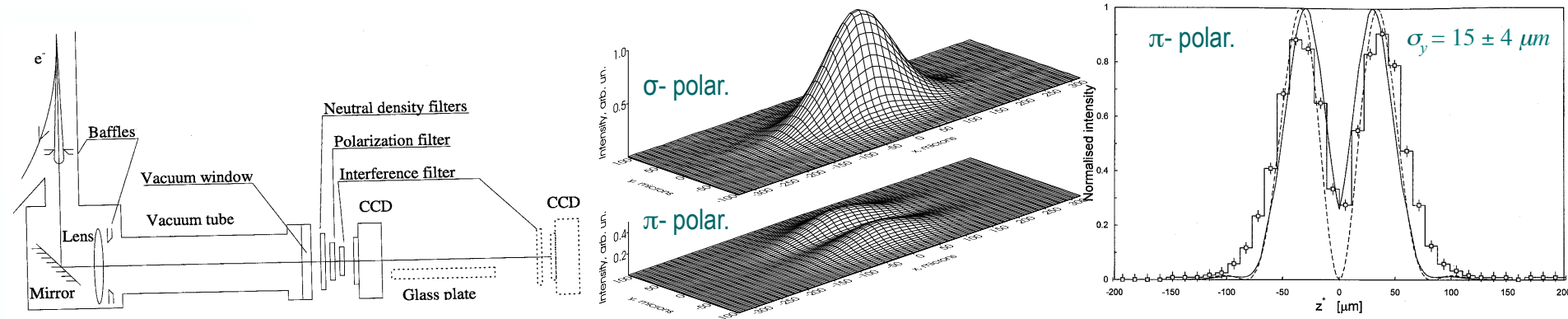
$E = 2.5 \text{ GeV}$ ;  $B = 1.56 \text{ T}$ ;  $\varepsilon = 40 \text{ eV}$ ; 1 : 1 imaging; 5 m from “Source Point” to Thin Lens



# Determining Electron Beam Size from Focused Visible Bending Magnet SR

## Measurements at MAX-II

Å. Andersson, M. Eriksson, O. Chubar, 1996



## Measurements at MAX-IV

J. Breunlin, Å. Andersson, 2015

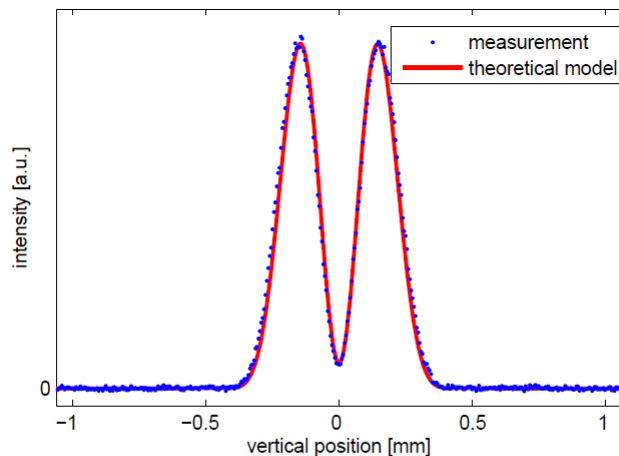


Figure 3: Vertical profile of imaged  $\pi$ -polarized SR at 488 nm wavelength. Measurement (blue dots) and SRW calculation (red lines). The vertical beam size is  $11.5 \mu\text{m}$ .

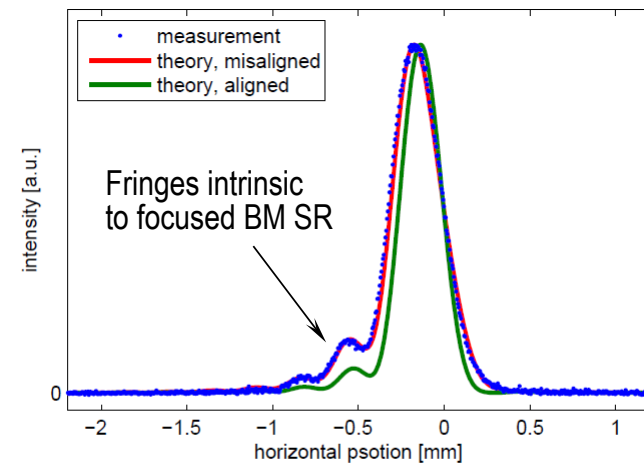
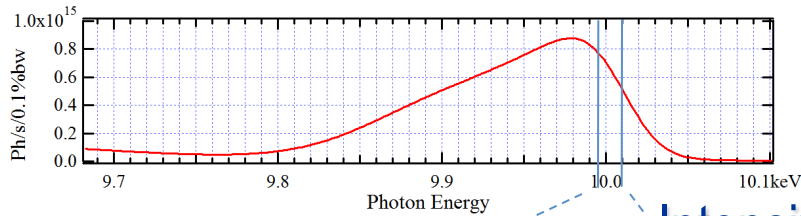


Figure 7: Horizontal profiles of  $\sigma$ -polarized SR at 930 nm for 8.2 mrad horizontal opening angle. The horizontal beam size is  $24.5 \mu\text{m}$ .

# Calculated UR Intensity Distributions from Finite-Emittance Electron Beam, “in Far Field” and “at Source”

## IVU20-3m Spectral Flux

through 100  $\mu\text{rad}$  (H) x 50  $\mu\text{rad}$  (V) Aperture  
at K~1.5 providing H5 peak at ~10 keV



Electron Beam (NSLS-II):

Hor. Emittance: 0.9 nm

Vert. Emittance: 8 pm

Energy Spread:  $8.9 \times 10^{-4}$

Current: 0.5 A

Low-Beta Straight

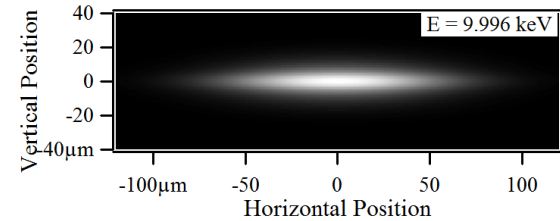
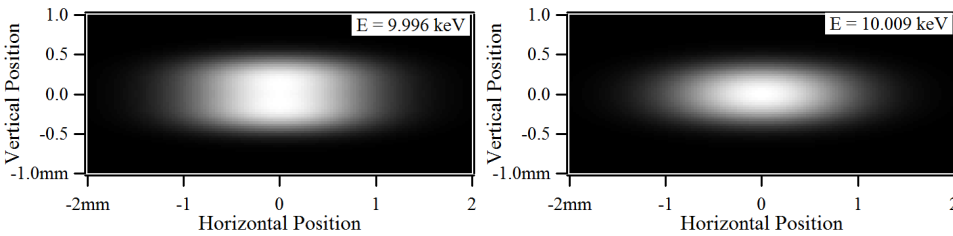
## Test Optical Scheme



## Intensity Distributions at ~10 keV

At 30 m from Undulator

In 1:1 Image Plane

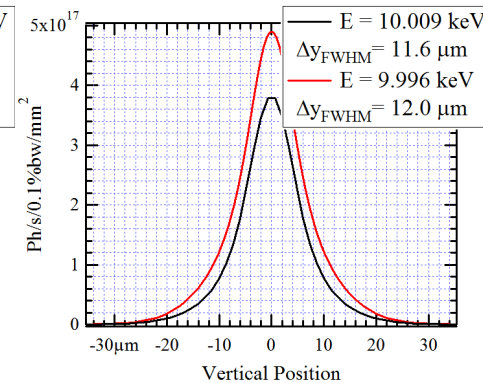
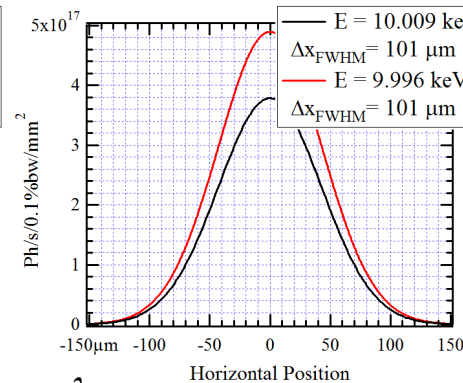
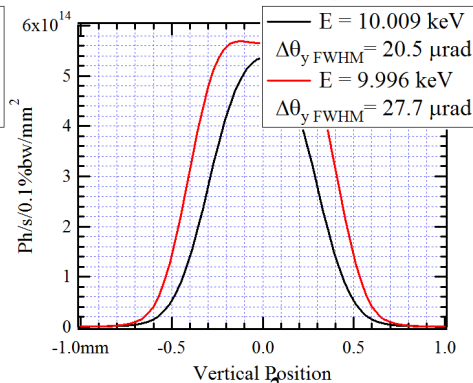
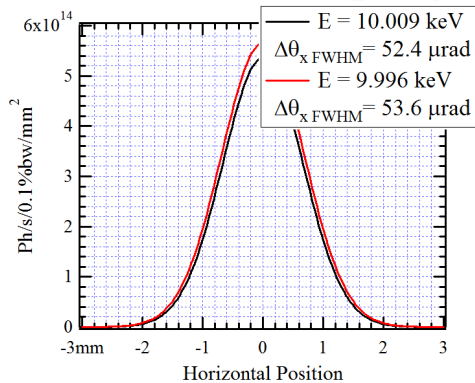


## Horizontal Cuts (y = 0)

## Vertical Cuts (x = 0)

## Horizontal Cuts (y = 0)

## Vertical Cuts (x = 0)



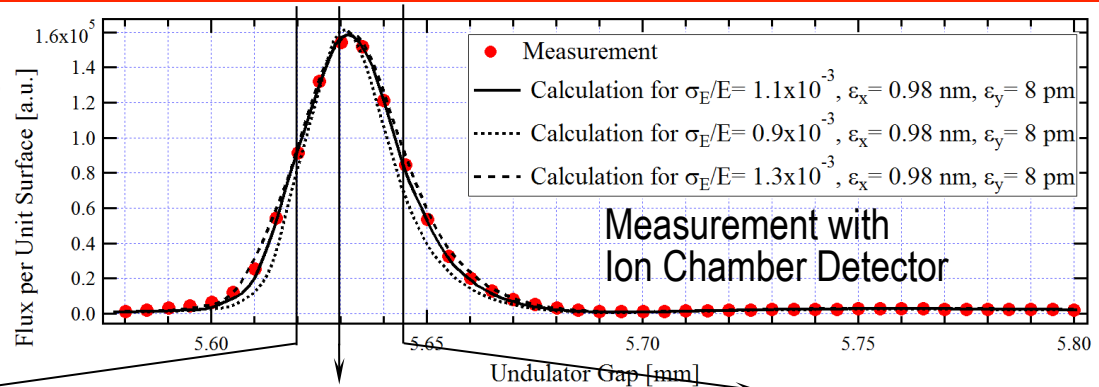
$$\sigma_x \sigma_x' \approx 97 \frac{\lambda}{4\pi}; \quad \sigma_y \sigma_y' \approx 5.7 \frac{\lambda}{4\pi}$$

...very far from Coherent Gaussian Beam !

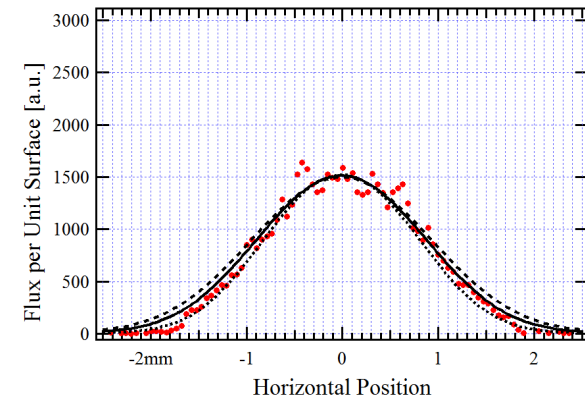
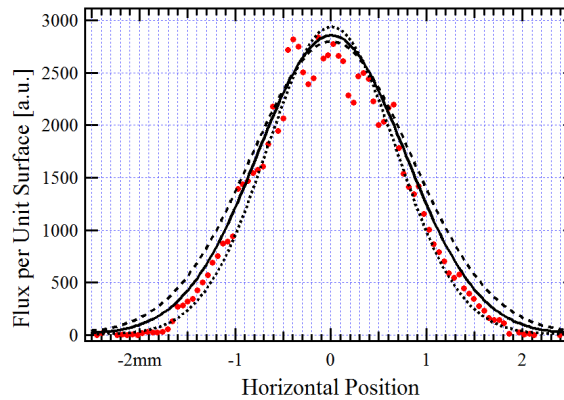
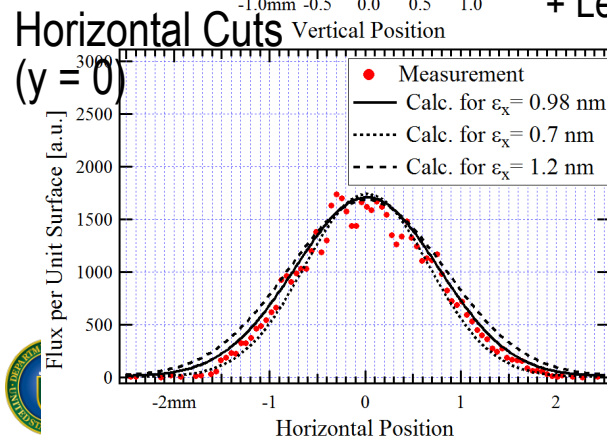
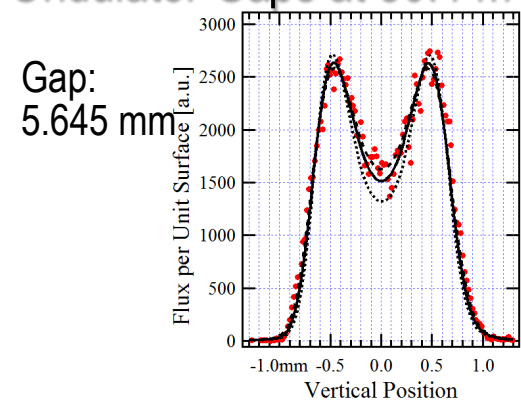
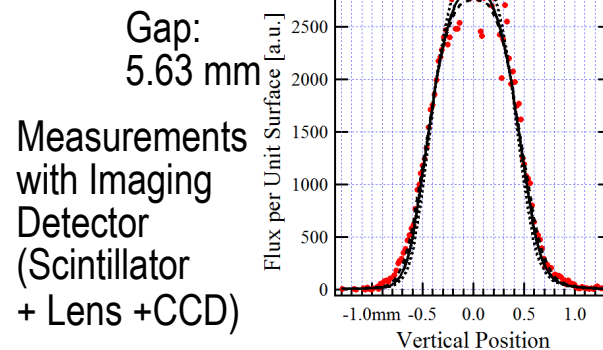
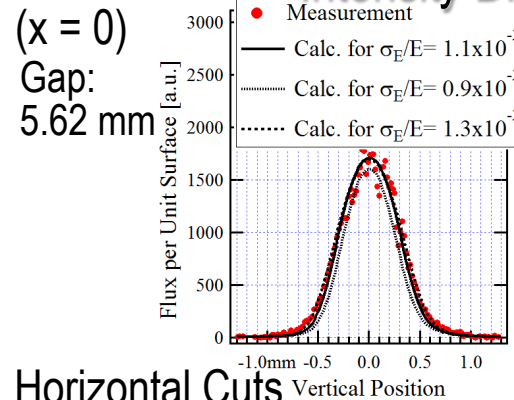
# On-Axis "Gap Spectrum" and Intensity Distributions of Radiation from IVU20 at HXN Beamline (I)

## On-Axis Gap Spectrum at ~8.0 keV Photon Energy (5<sup>th</sup> Harmonic)

Undulator:  $\lambda_u = 20$  mm,  $L_u = 3$  m  
 Low-Beta Straight Section of NSLS-II:  
 $\beta_x = 1.84$  m ( $\sigma'_x = 22$   $\mu$ rad at  $\epsilon_x = 0.9$  nm)  
 $\beta_y = 1.17$  m ( $\sigma'_y = 2.6$   $\mu$ rad at  $\epsilon_y = 8$  pm)



## Vertical Cuts Intensity Distributions at 5<sup>th</sup> Harmonic at Different Undulator Gaps at 30.4 m

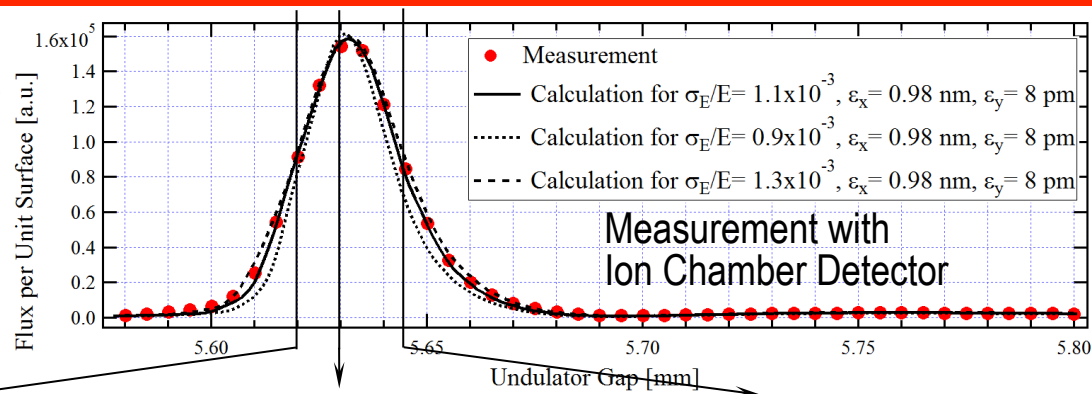




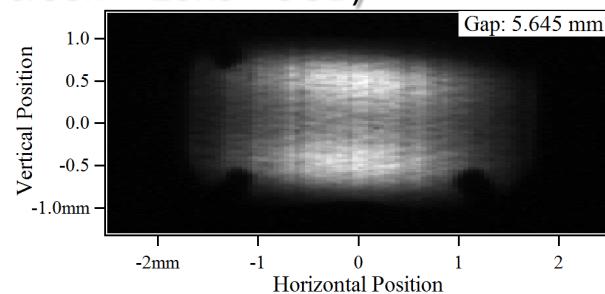
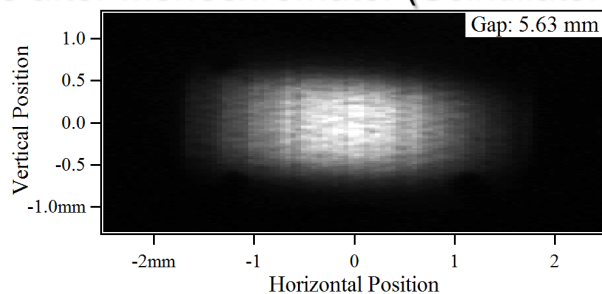
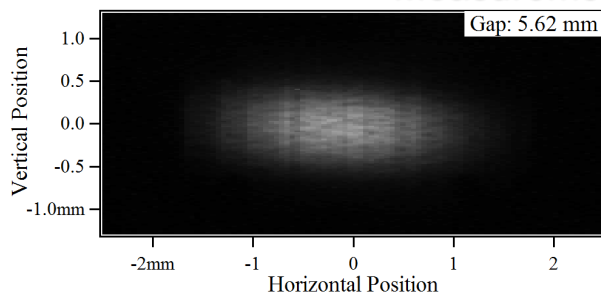
# On-Axis "Gap Spectrum" and Intensity Distributions of Radiation from IVU20 at HXN Beamline (II)

## On-Axis Gap Spectrum at ~8.0 keV Photon Energy (5<sup>th</sup> Harmonic)

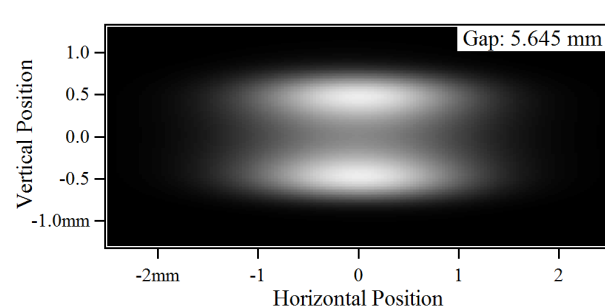
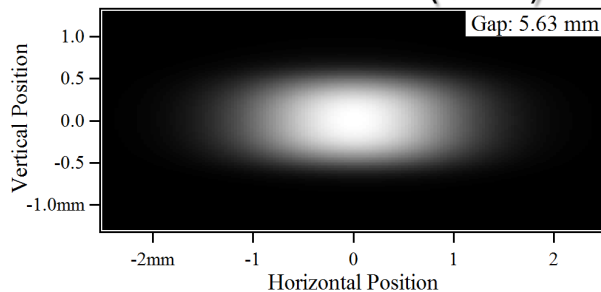
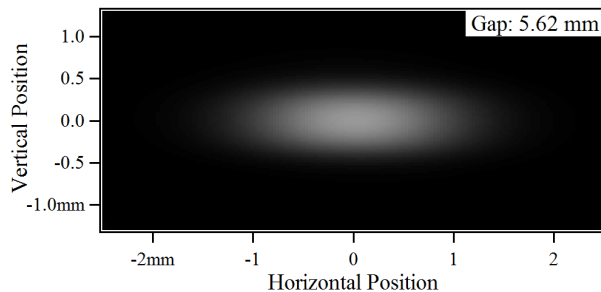
Undulator:  $\lambda_u = 20$  mm,  $L_u = 3$  m  
 Low-Beta Straight Section of NSLS-II:  
 $\beta_x = 1.84$  m ( $\sigma'_x = 22$   $\mu$ rad at  $\epsilon_x = 0.9$  nm)  
 $\beta_y = 1.17$  m ( $\sigma'_y = 2.6$   $\mu$ rad at  $\epsilon_y = 8$  pm)



## Intensity Distributions at 5<sup>th</sup> Harmonic at Different Undulator Gaps at 30.4 m Measurements after Monochromator (Scintillator Screen + Lens + CCD)



## Calculations (SRW)



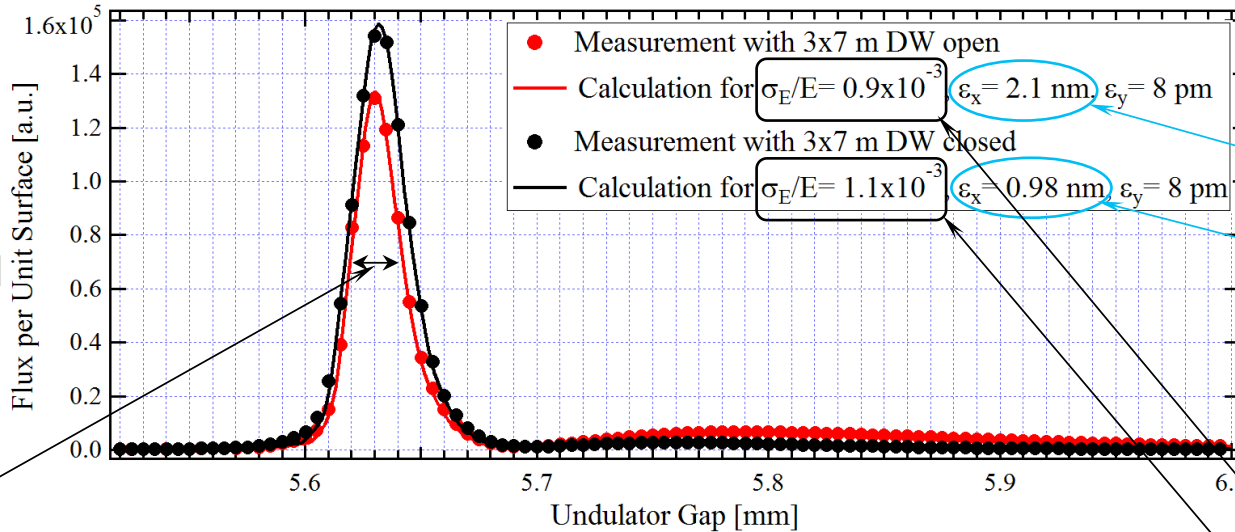
# IVU20 (HXN) On-Axis "Gap Spectra" with Damping Wiggler Gaps "Open" and "Closed"

$E_{ph} \approx 8.0$  keV  
5<sup>th</sup> UR Harm.

Low-Beta Straight  
Section of NSLS-II  
 $\beta_x = 1.84$  m  
 $\beta_y = 1.17$  m

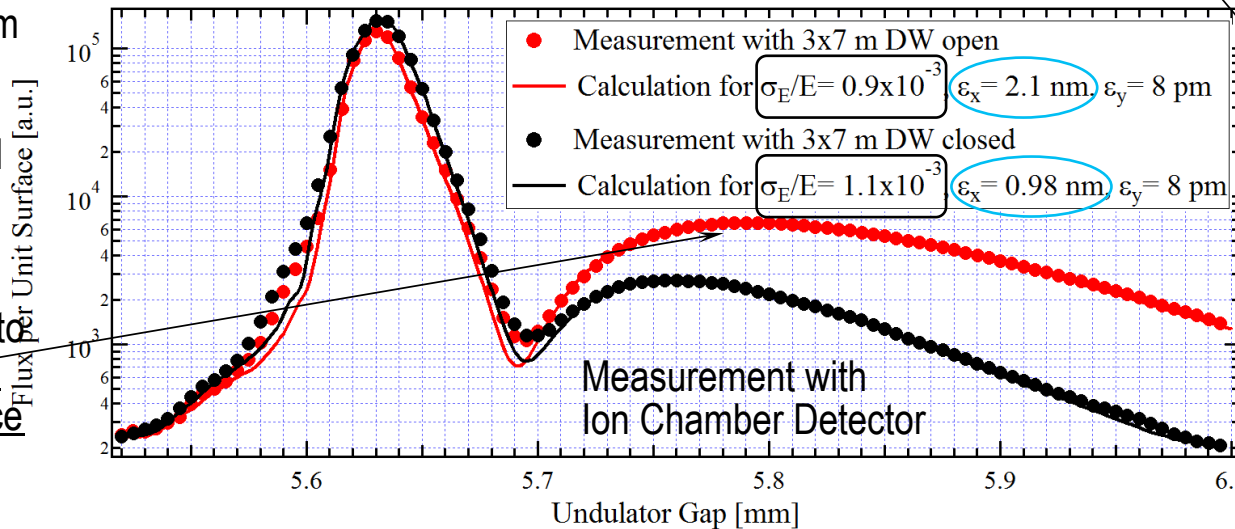
Harmonic width is  
sensitive to e-beam  
Energy Spread  
(and other factors,  
e.g. undulator field  
quality)

Intensity in "Side  
Lobe" is sensitive to  
e-beam Horizontal  
Angular Divergence



Good Agreement  
with Accelerator  
Physics data:  
 $\epsilon_x = 2.1$  nm for  
Bare Lattice,  
 $\epsilon_x = 0.9$  nm with  
3x7 m DW closed

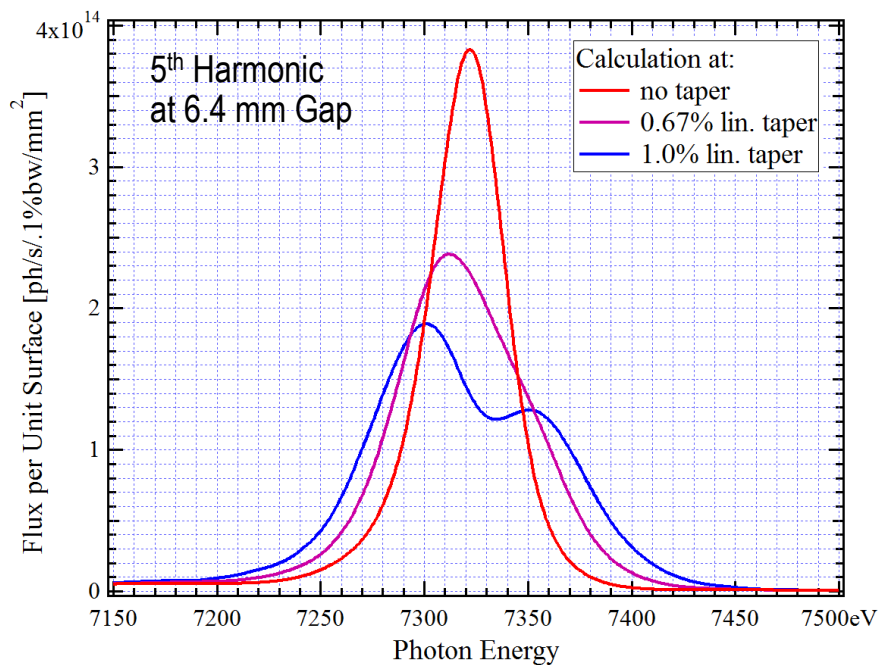
~Poor Agreement  
with Accelerator  
Physics data:  
 $\sigma_E/E = 0.5 \times 10^{-3}$  for  
Bare Lattice,  
 $\sigma_E/E = 0.9 \times 10^{-3}$  with  
3x7 m DW closed



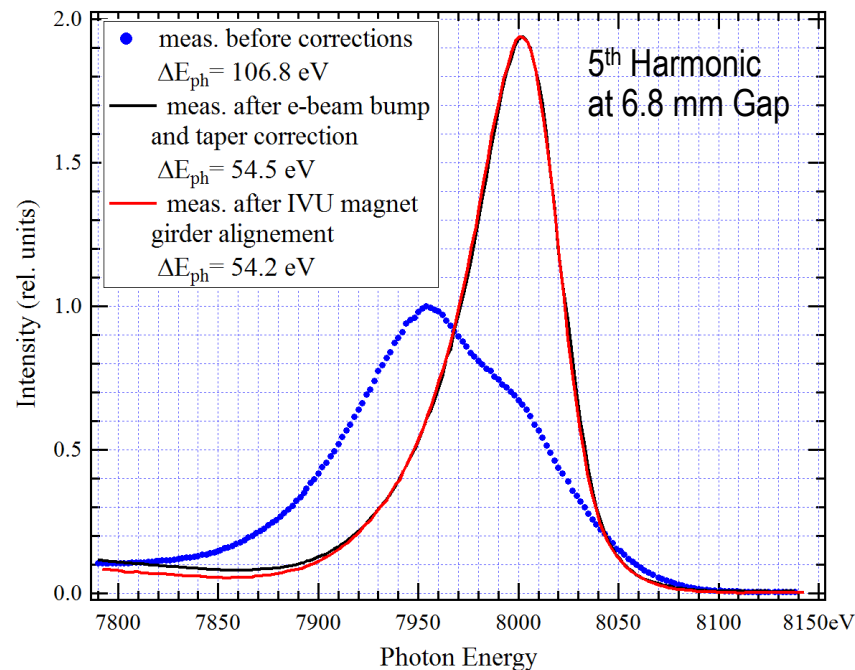
UR based e-beam  
diagnostics was  
used at ESRF  
(P. Elleaume et al.)  
and at APS  
(A. Lumpkin,  
E. Gluskin et al.)

# Example of Using High-Accuracy UR Calculation for Advanced Commissioning of SRX Beamline at NSLS-II

## Simulation of Taper / Misalignment Effects



## Measurements



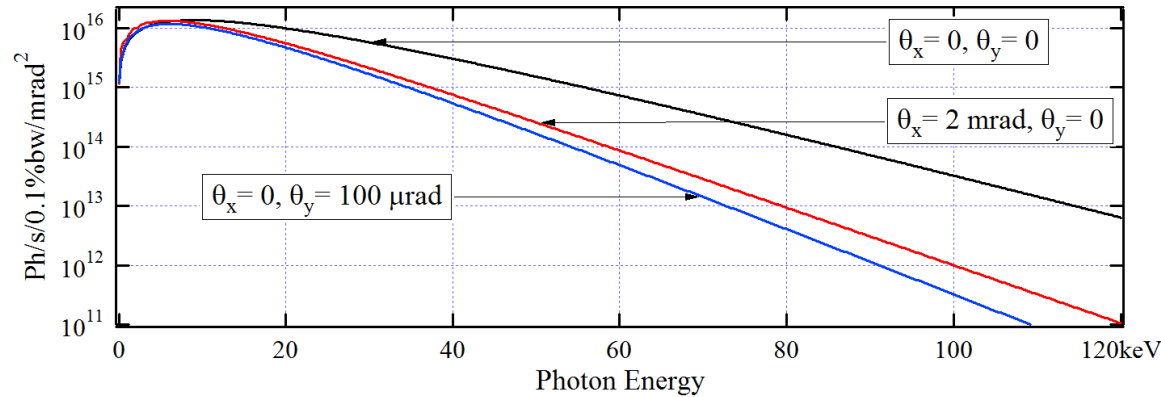
Undulator Radiation Simulations with SRW allowed to:

- Identify case of an under-performing In-Vacuum Undulator;
- Find reason for the reduction of spectral performance (small misalignment of magnet arrays);
- Implement most efficient correction and **restore nearly ideal IVU spectrum.**

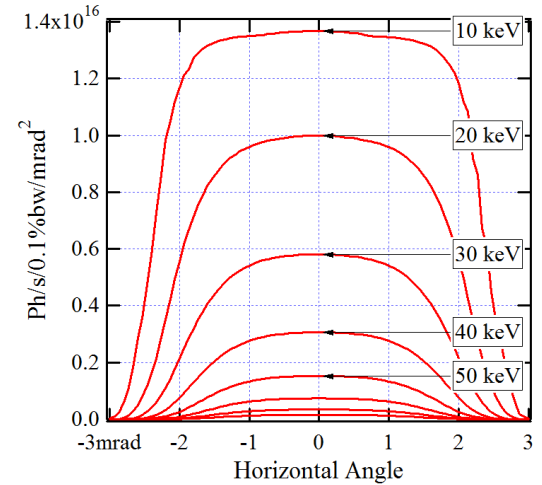
# Spectral-Angular Distributions of Emission from NSLS-II 2 x 3.5 m Long Damping Wiggler in “Inline” Configuration

## Angular Profiles of DW Emission at Different Photon Energies

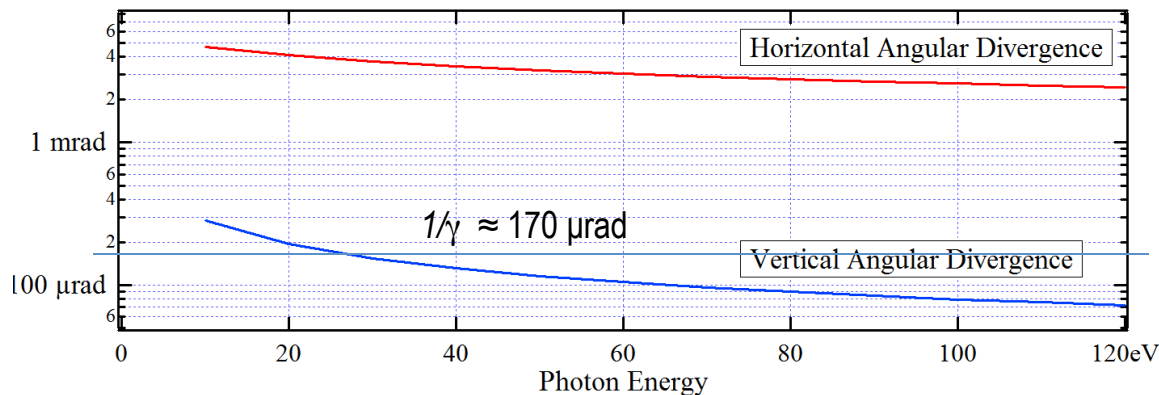
### Spectral Flux per Unit Solid Angle



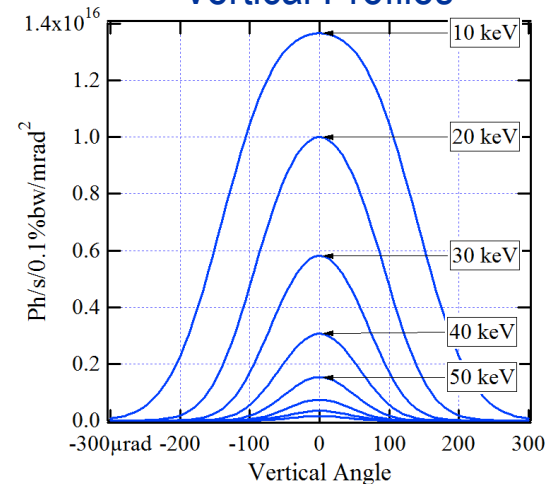
### Horizontal Profiles



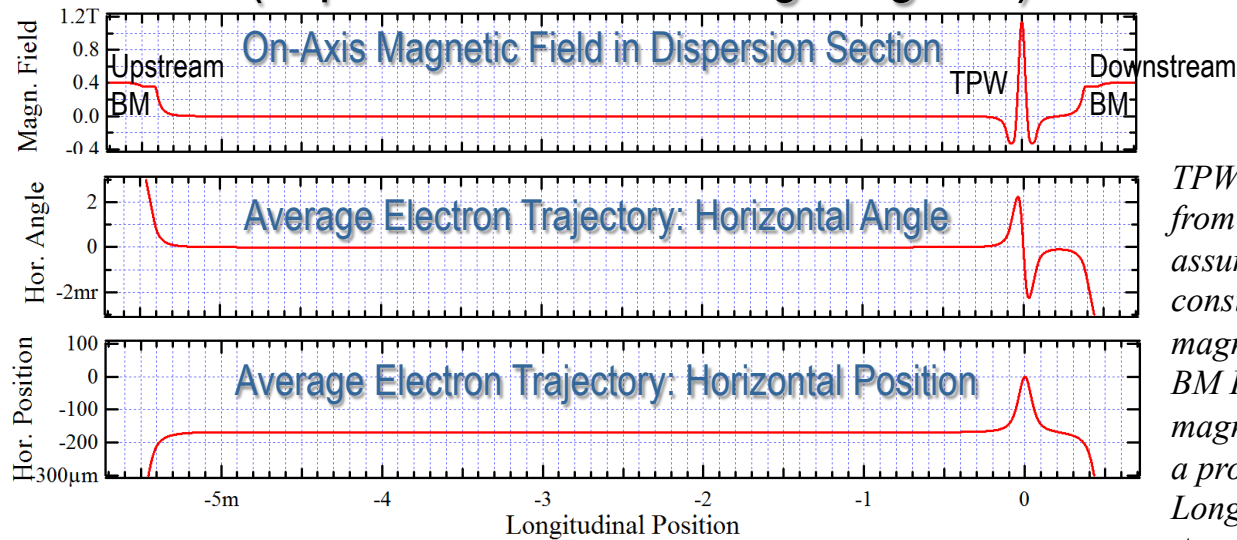
### FWHM Angular Divergence of DW Emission



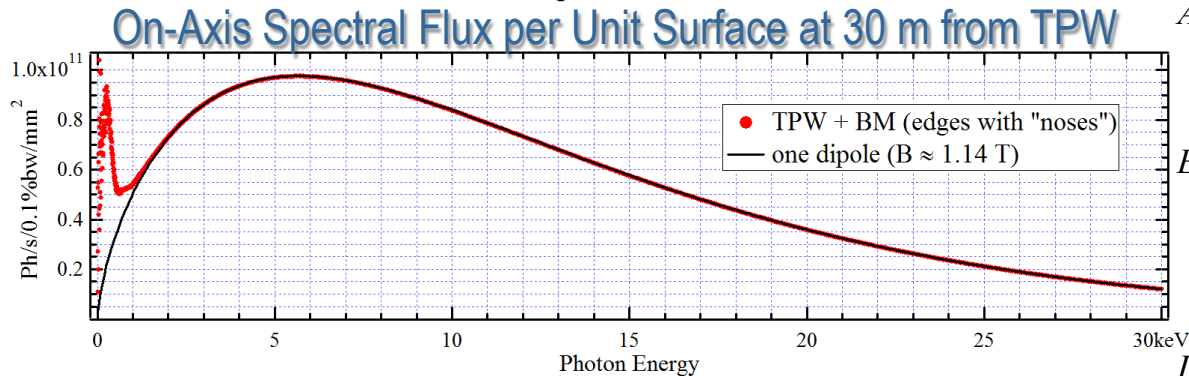
### Vertical Profiles



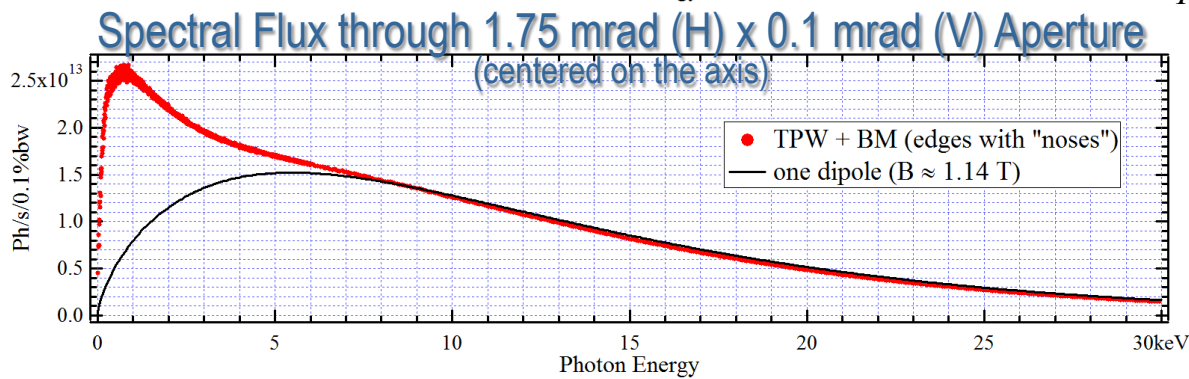
# NSLS-II 3PW: Magn. Field, Electron Trajectory, Spectra (in presence of Bending Magnets)



*TPW Field taken from magnetic simulations, assuming that TPW will be constructed out of spare DW magnets;  
BM Field is taken from magnetic measurements on a prototype BM with "nose";  
Longitudinal Positions are Approximate (+/- 10 cm)*



*Electron Energy: 3 GeV  
Current: 0.5 A  
Hor. Emittance: 0.55 nm  
Vert. Emittance: 8 pm*

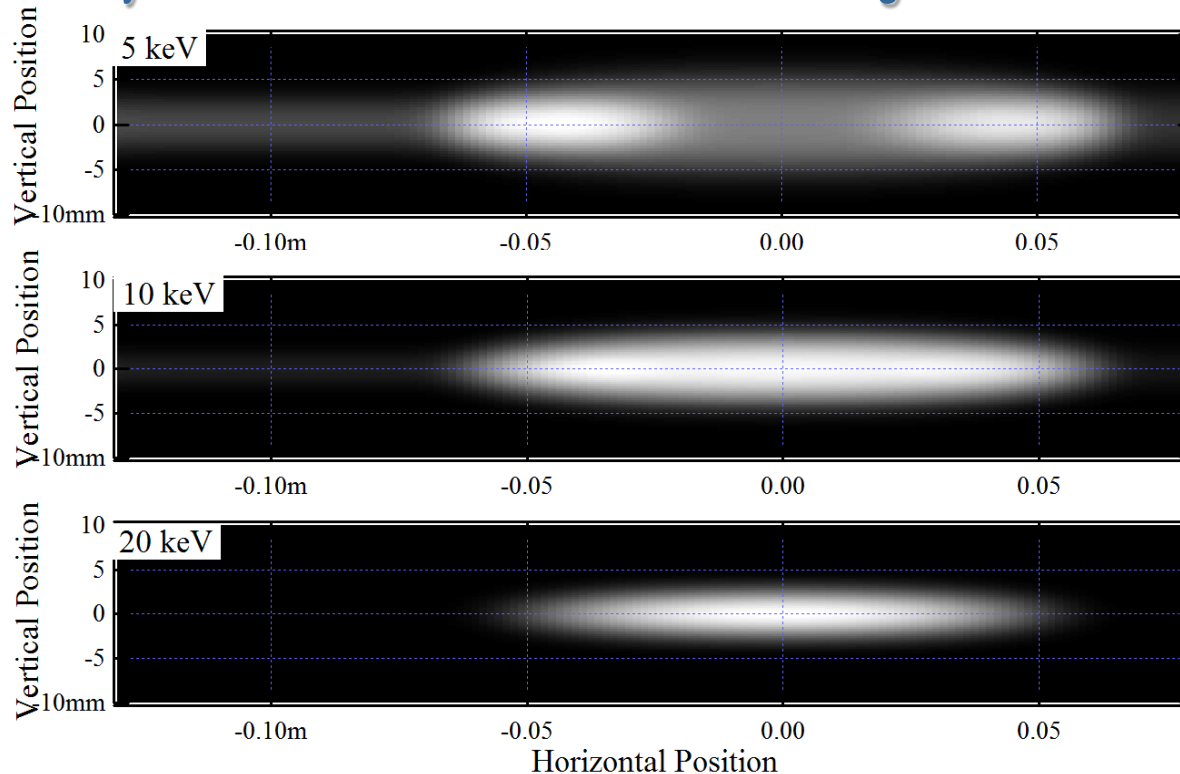


*Initial Conditions:  
<x> = 0, <x'> = 0 in TPW  
Center*



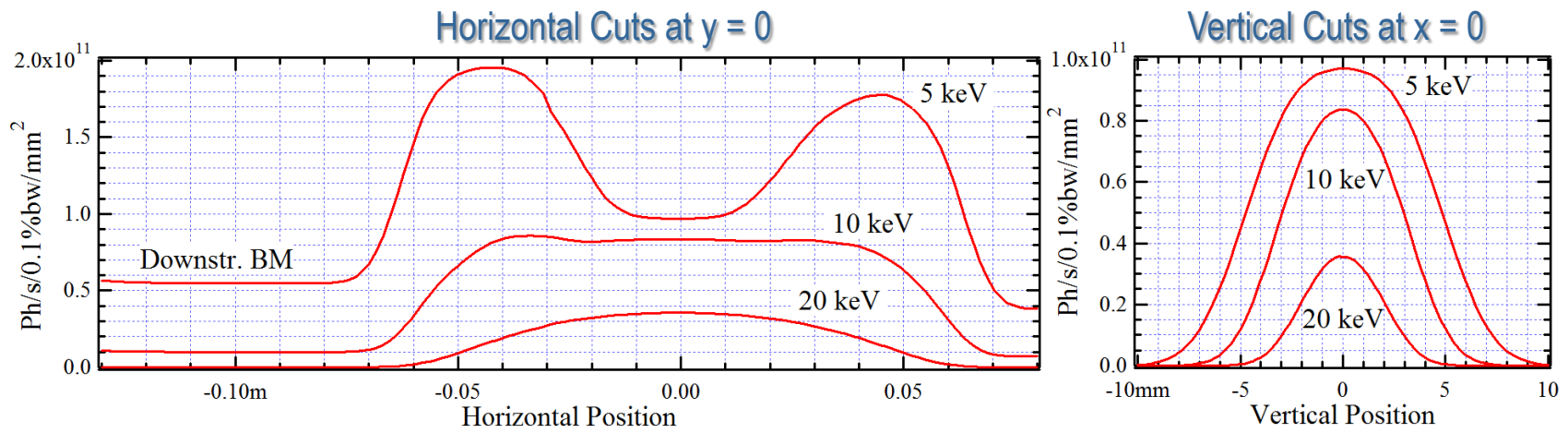
# NSLS-II 3PW+BM Radiation Intensity (Hard X-Rays)

## Intensity Distributions at Different Photon Energies at 30 m from TPW



*TPW Field taken from magnetic simulations, assuming that TPW will be constructed out of spare DW magnets; BM Field taken from magnetic measurements on a prototype BM with "nose".*

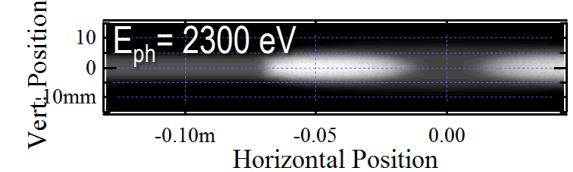
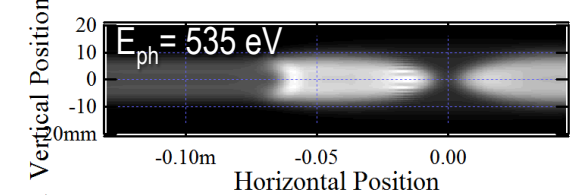
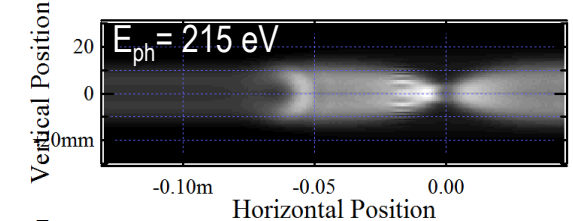
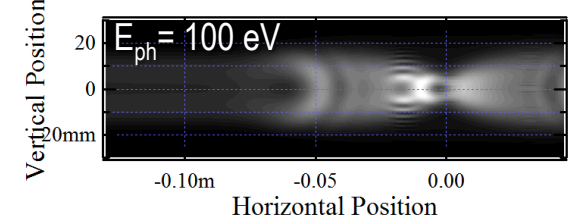
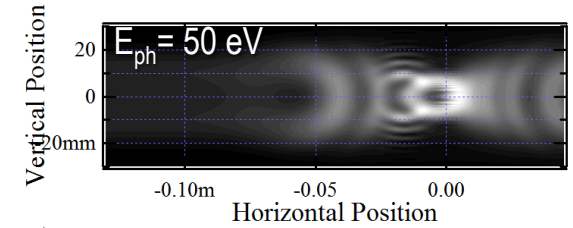
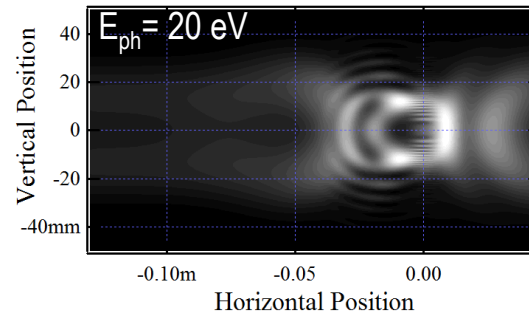
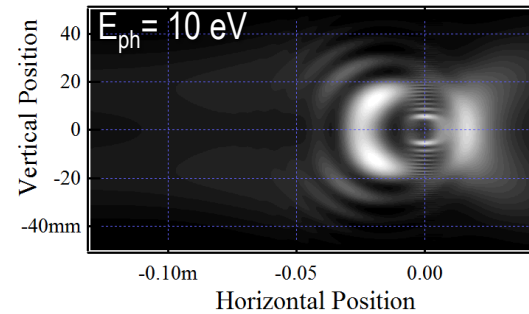
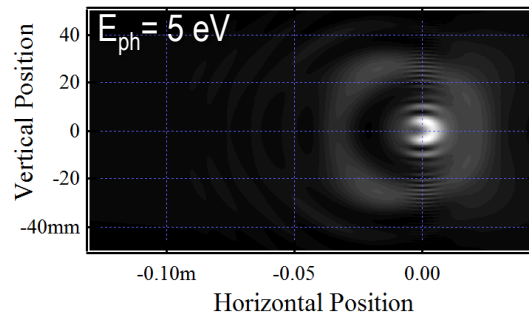
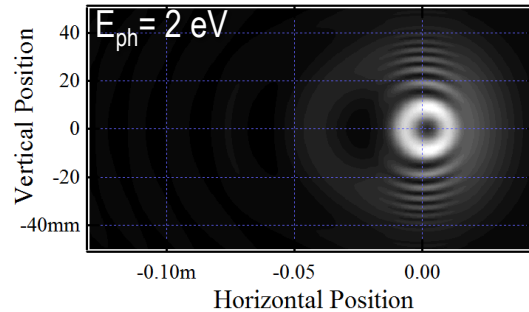
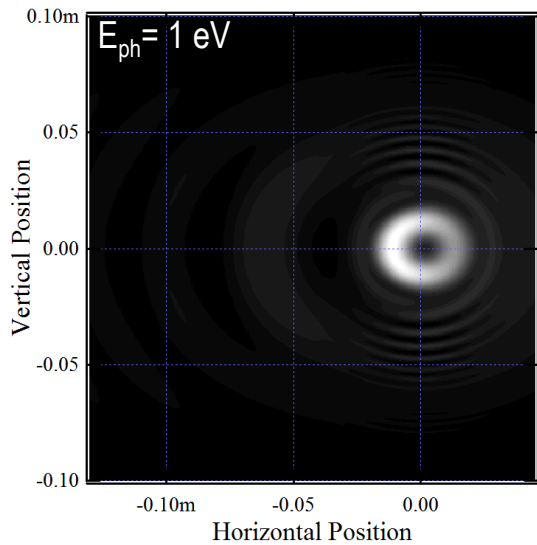
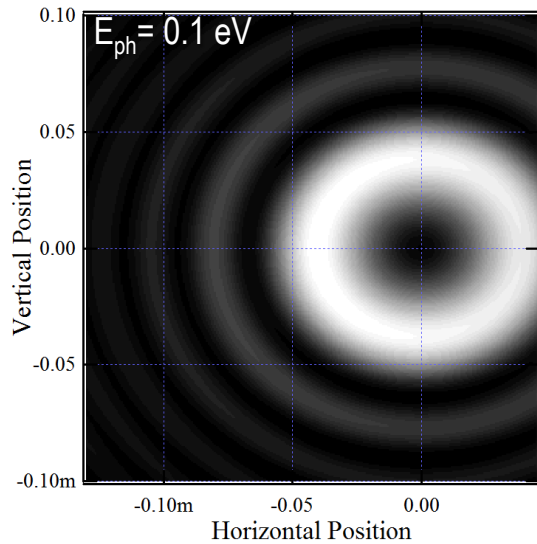
Electron Current: 0.5 A





# NSLS-II 3PW+BM Radiation Intensity (IR to Soft X-Rays)

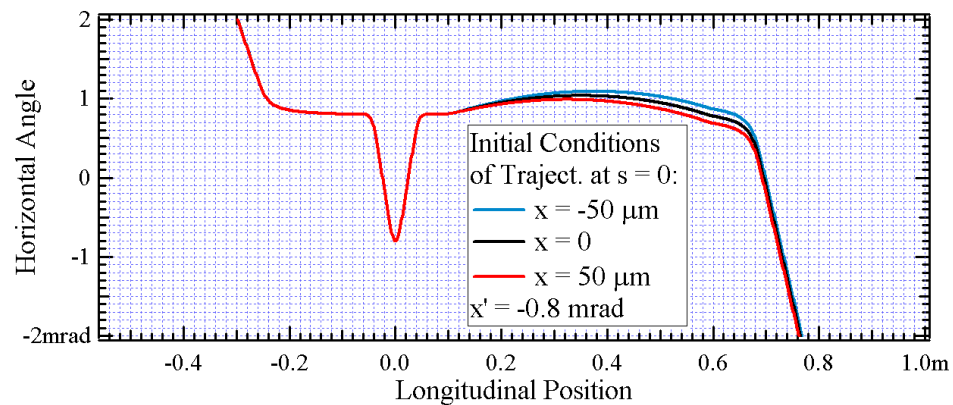
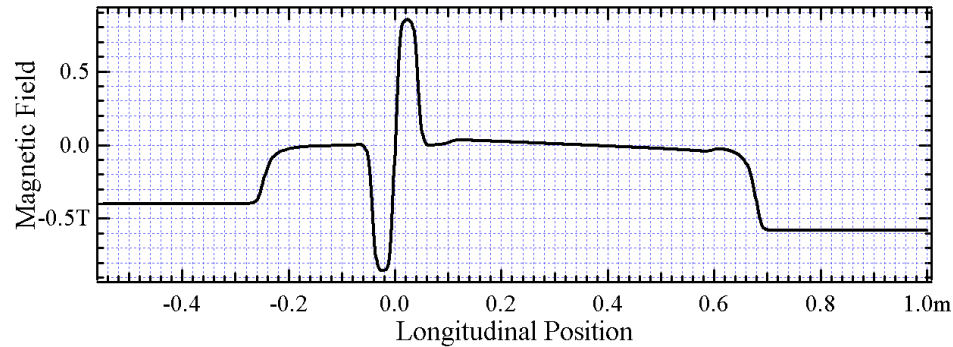
Observation Distance: 30 m  
(from TPW center)



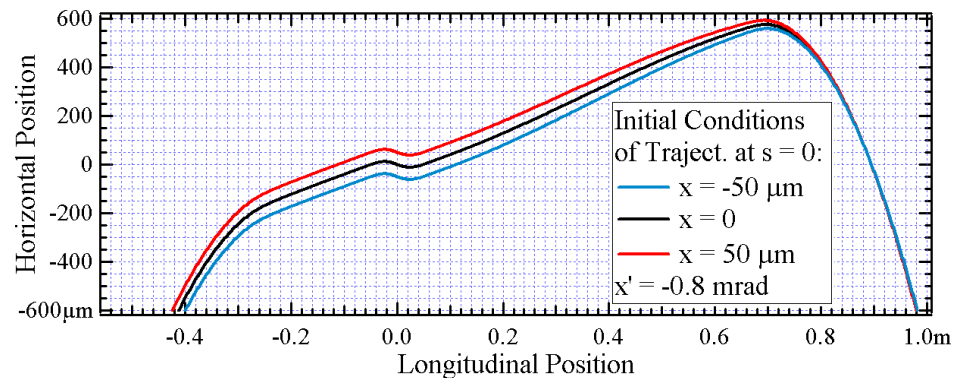
*TPW Field taken from magnetic simulations,  
assuming that TPW will be constructed out of  
spare DW magnets;  
BM Field taken from magnetic measurements  
on a prototype BM with “nose”.*

# ESRF-U 2PW (option): Magnetic Field and Electron Trajectories

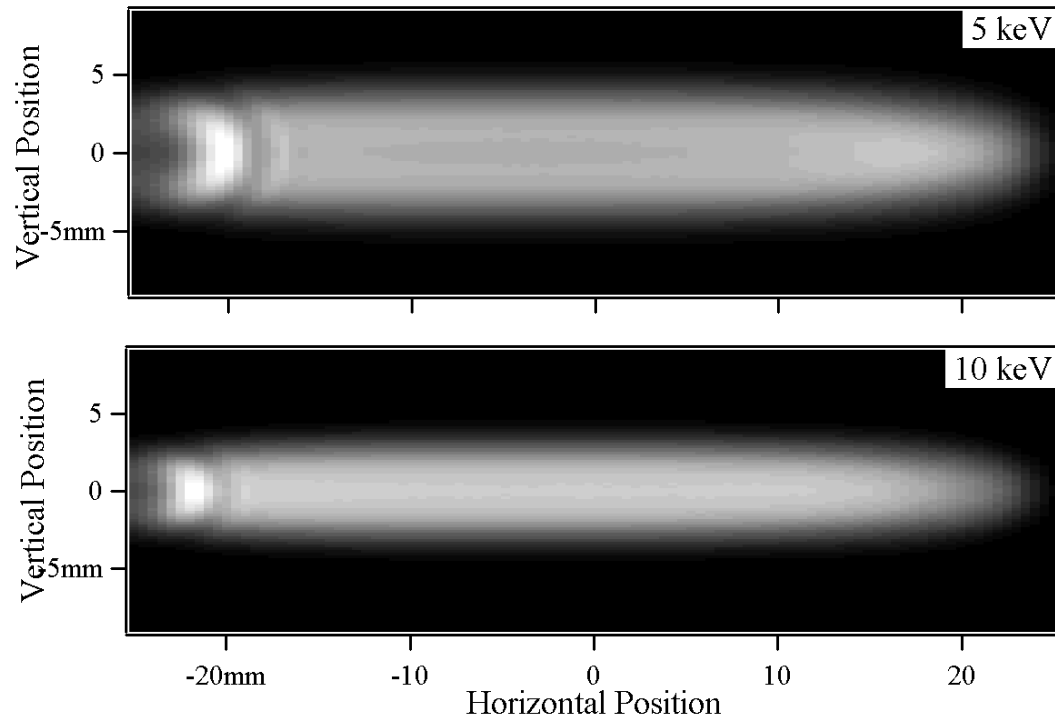
Magnetic design  
by J. Chavanne



Quadrupole  
Lens is included  
into analysis  
(under testing)

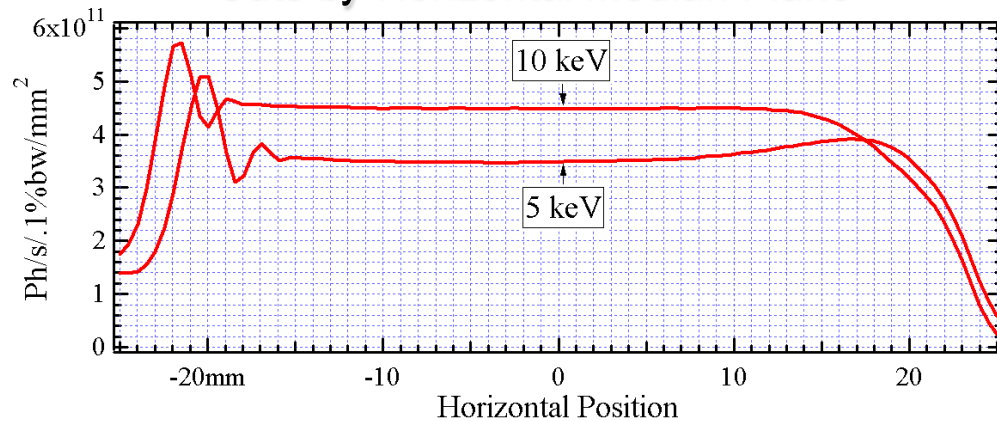


# ESRF-U 2PW Radiation Intensity Distributions

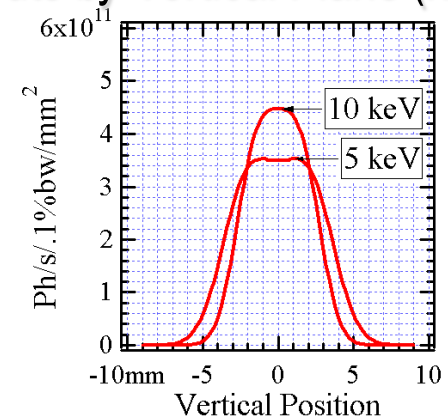


Observation Distance:  
 $R = 30 \text{ m}$

## Cuts by Horizontal Median Plane

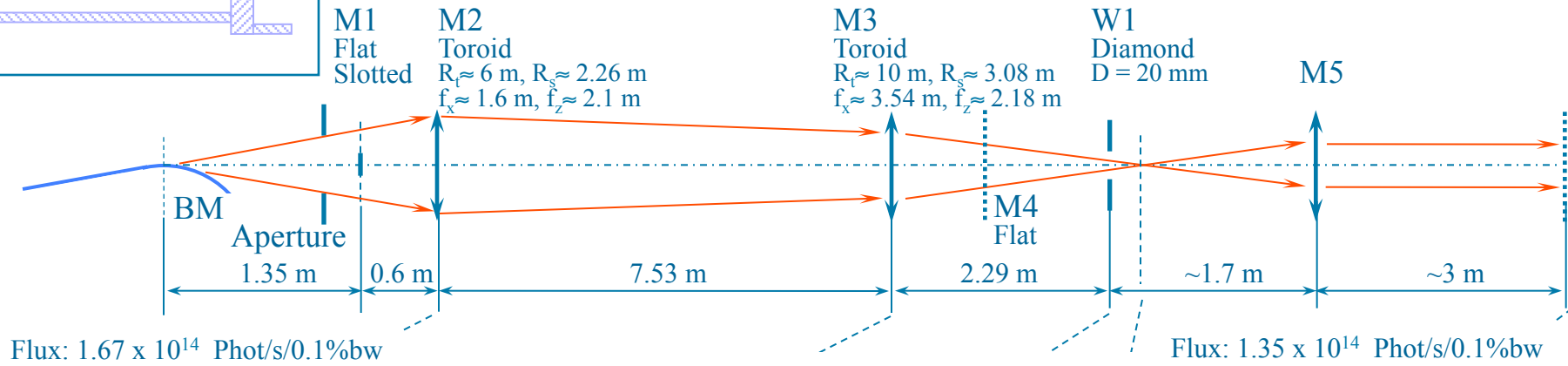
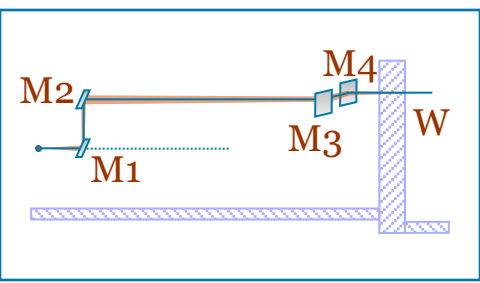


## Cuts by Vertical Plane (x = 0)

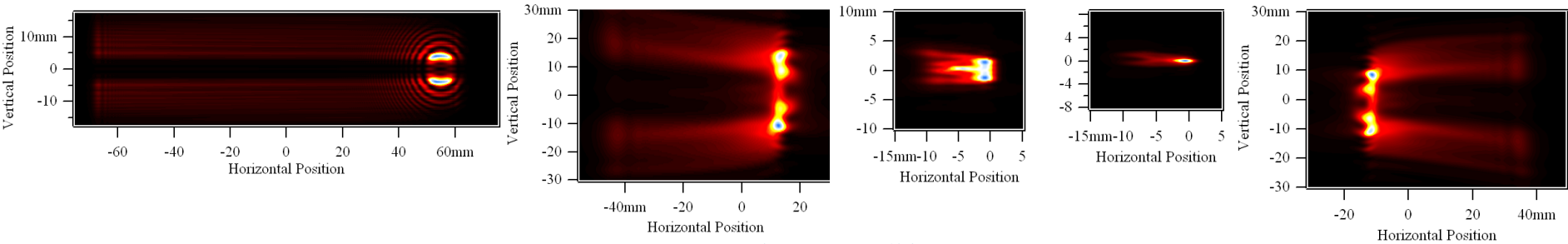


# SMIS IR Extraction Scheme at SOLEIL

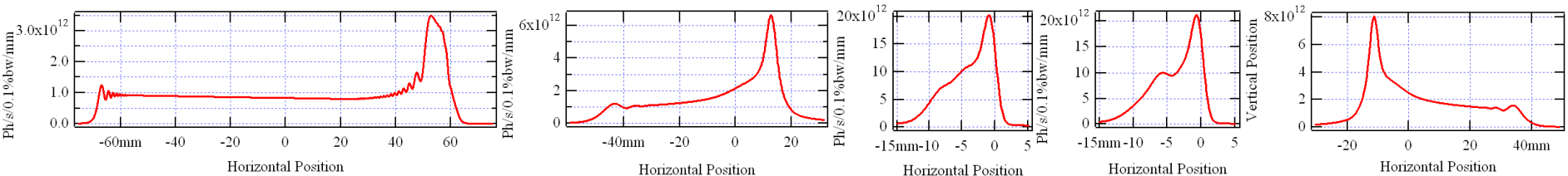
## Fully-Coherent Wavefront Propagation



### Intensity Distributions at $10 \mu\text{m}$ Wavelength



### Intensity Profiles

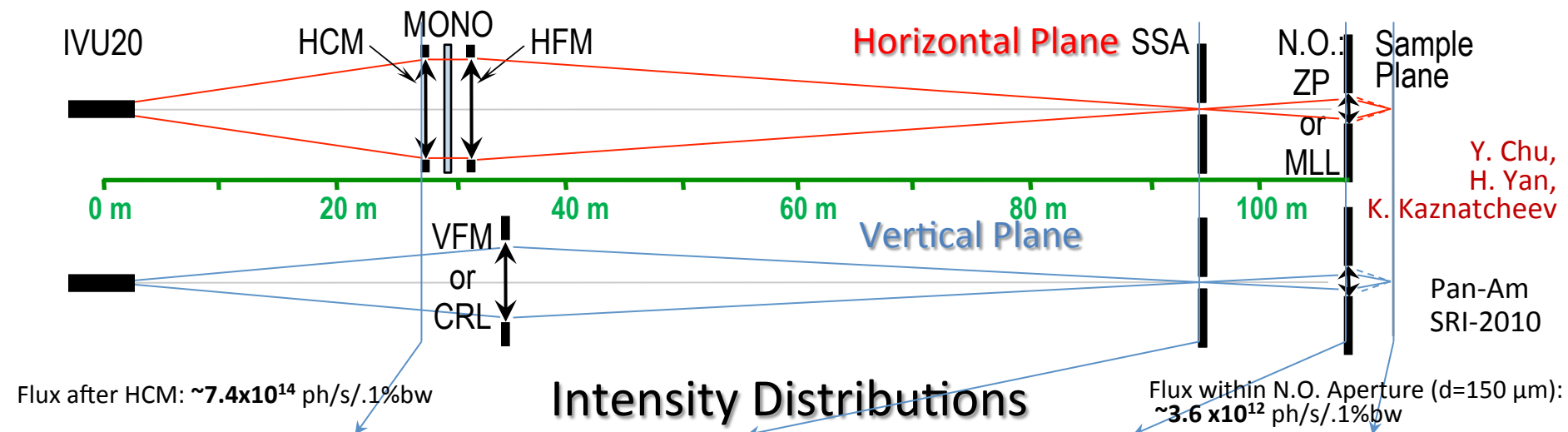


# Updates of Core Functions in “Synchrotron Radiation Workshop” Code Enabling Physical-Optics Calculations for Beamlines in Low-Emittance Rings and X-FEL

- Accurate partially-coherent emission and wavefront propagation simulations for SR sources are possible with SRW since ~2009:
  - O.Chubar, Y.S.Chu, K.Kaznatcheev, H.Yan, AIP Conf. Proc. Vol. 1234, pp.75-78 (2009)
  - O.Chubar, Y.S.Chu, K.Kaznatcheev, H.Yan, Nucl. Instr. and Meth., vol. A649, Issue 1, pp.118-122 (2011)
- Parallel calculations of Partially-Coherent Emission and Wavefront Propagation are implemented in SRW for Python (based on MPI / mpi4py). Besides “normal” Intensity, calculation of Mutual Intensity / Degree of Coherence is possible:
  - O.Chubar, A.Fluerasu, L.Berman, K.Kaznatcheev, L.Wiegart, J. Phys.: Conf. Ser. 425, 162001 (2013)
  - D.Laundy, J.P.Sutter, U.H.Wagner, C.Rau, C.A.Thomas, K.J.S.Sawhney, and O.Chubar, J. Phys.: Conf. Ser. 425, 162002 (2013)
- Increased reliability of Time- / Frequency-Dependent FEL Pulse Propagation simulations:
  - S.Roling, H.Zacharias, L.Samoylova, H.Sinn, Th.Tschentscher, O.Chubar, A.Buzmakov, E.Schneidmiller, M.V.Yurkov, F.Siewert, S.Braun, and P.Gawlitza, Phys. Rev. ST Accel. Beams 17, 110705 (2014)
- Physical-optics “propagators” are implemented for:
  - Grazing-Incidence Focusing Mirrors, using the stationary phase method / “local ray-tracing”:
    - N.Canestrari, O.Chubar, R.Reininger, J. Synchrotron Rad. 21, 1110-1121 (2014)
  - Perfect Crystals, using the X-ray Dynamical Diffraction methods:
    - J.P.Sutter, O.Chubar, A.Suvorov, Proc. SPIE Vol. 9209, 92090L (2014)
    - A.Suvorov, Y.Q.Cai, J.P.Sutter, O.Chubar, Proc. SPIE Vol. 9209, 92090H (2014)
    - O.Chubar, G.Geloni, V.Kocharyan, A.Madsen, E.Saldin, S.Serkez, Y.Shvyd'ko, J.Sutter, JSR 23, 410-424 (2016)
  - Variable Line Spacing Gratings, using the Stationary Phase method:
    - N.Canestrari, V.Bisogni, A.Walter, Y.Zhu, J.Dvorak, E.Vescovo, O.Chubar, Proc. SPIE Vol. 9209, 92090I (2014)

# NSLS-II Hard X-Ray Nanoprobe (HXN) Beamline

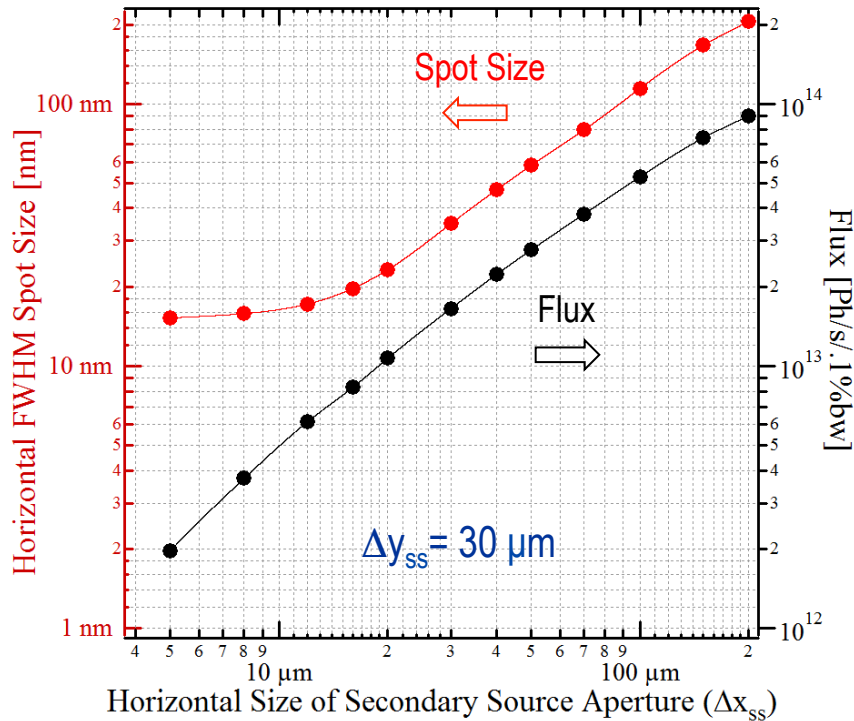
## Optical Scheme and Partially-Coherent Wavefront Propagation Simulation



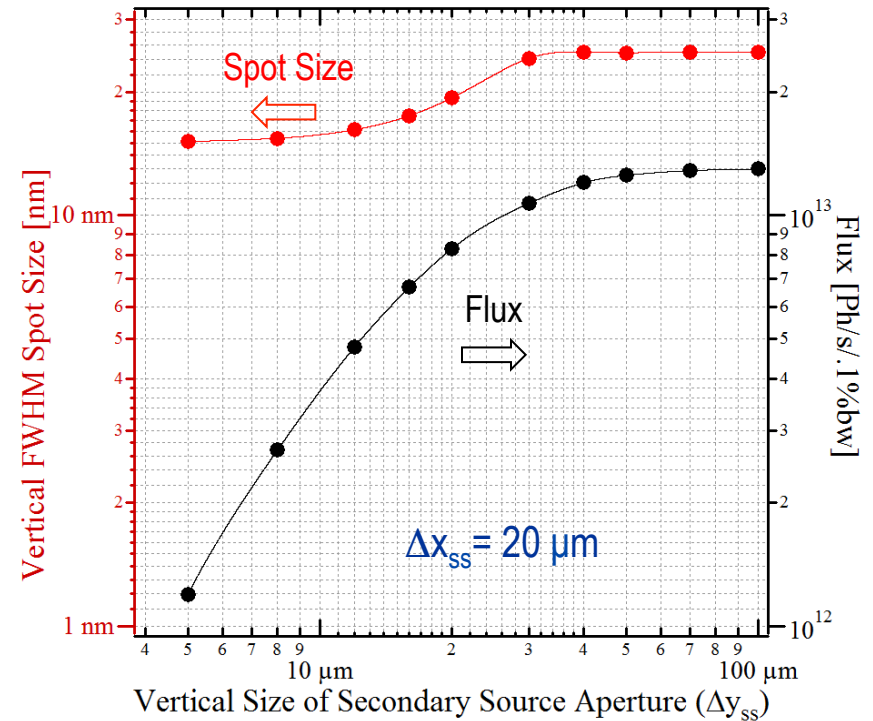


# Final Focal Spot Size and Flux at Sample vs Secondary Source Aperture Size (HXN, NSLS-II)

## Horizontal Spot Size and Flux vs Horizontal Secondary Source Aperture Size



## Vertical Spot Size and Flux vs Vertical Secondary Source Aperture Size



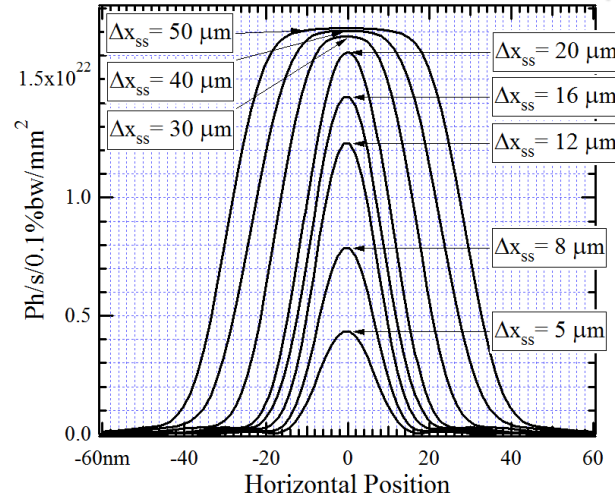
Pan-Am SRI-2010

Secondary Source Aperture located at 94 m from Undulator  
 Spot Size and Flux calculated for Nanofocusing Optics simulated by Ideal Lens  
 with  $F = 18.14 \text{ mm}$ ,  $D = 150 \mu\text{m}$  located at 15 m from Secondary Source (109 m from Undulator)

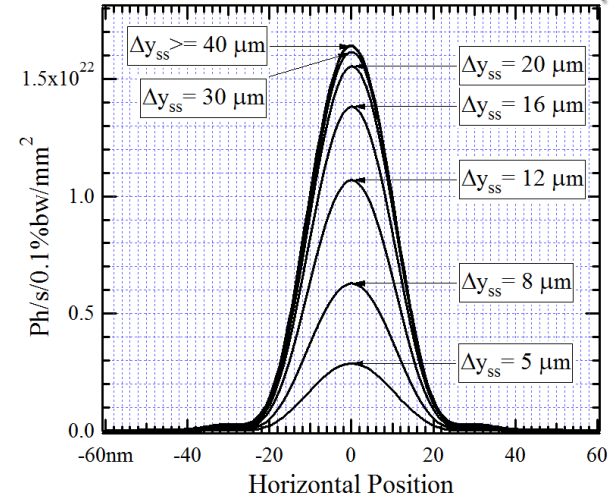
# Intensity Distributions at Sample for Different Secondary Source Aperture Sizes at HXN (NSLS-II)

In Horizontal Median Plane ( $y = 0$ )

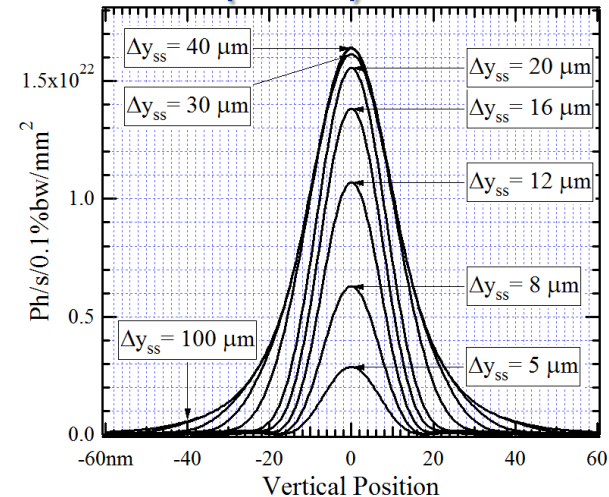
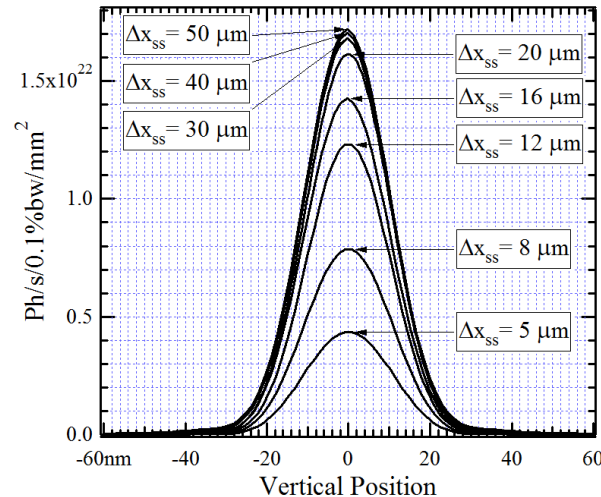
For Different Horizontal SSA Sizes ( $\Delta x_{ss}$ )



For Different Vertical SSA Sizes ( $\Delta y_{ss}$ )

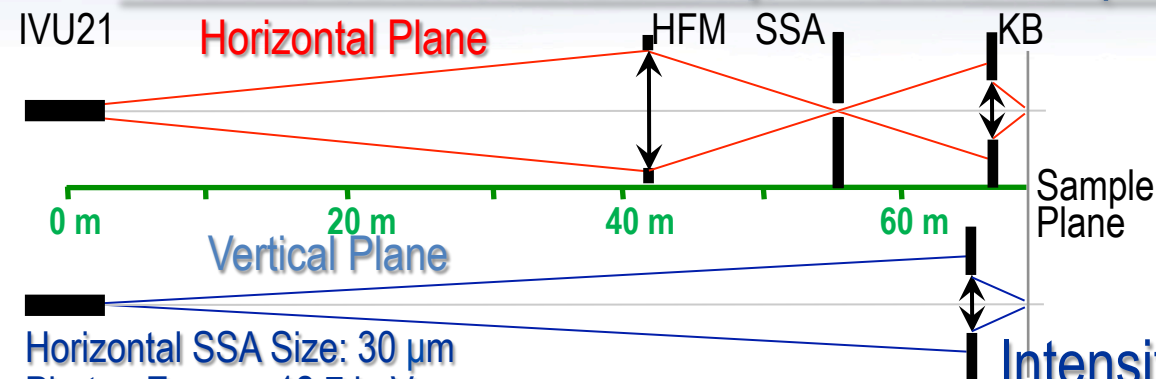


In Vertical Median Plane ( $x = 0$ )



For Nanofocusing Optics with  $F = 18.14 \text{ mm}$ ,  $D = 150 \mu\text{m}$  ( $\Delta r \approx 15 \text{ nm}$ ;  $E_{ph} \approx 10 \text{ keV}$ )  
SSA located at 94 m, Nanofocusing Optics at 109 m from Undulator

# Partially-Coherent Wavefront Propagation Simulations for a Beamline with Grazing-Incidence Focusing Mirrors, Taking Into Account Their Imperfections (FMX @ NSLS-II)

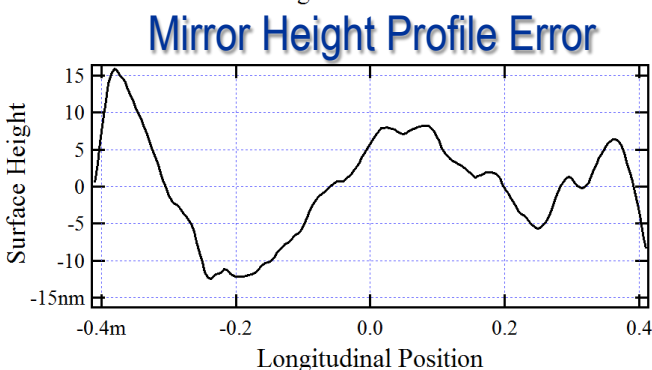
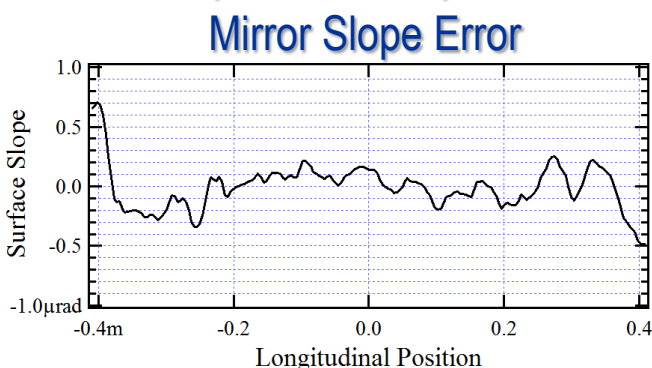


KB simulated using Grazing-Incidence "Thick Optical Element" Propagator based on "Local Ray-Tracing".

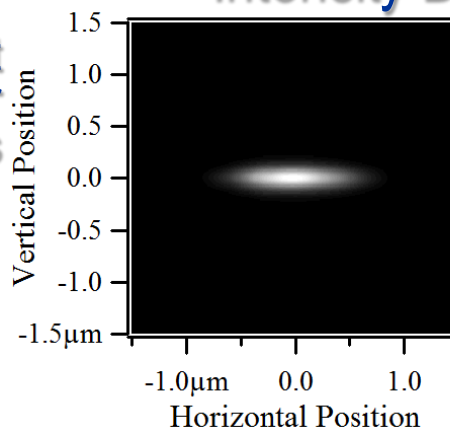
KB Surface Height Error simulated by corresponding Phase Shifts ("Masks") in Transverse Plane at Mirror Locations.

## Intensity Distributions at Sample

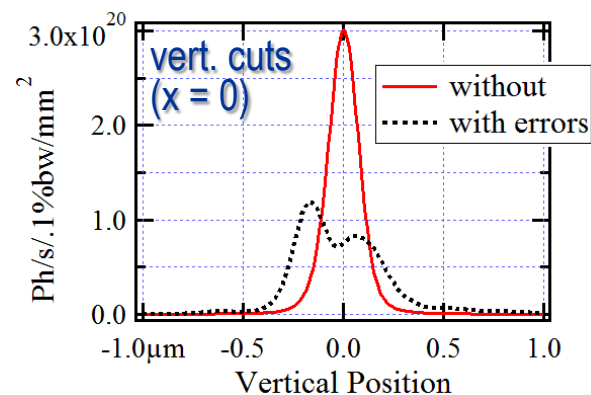
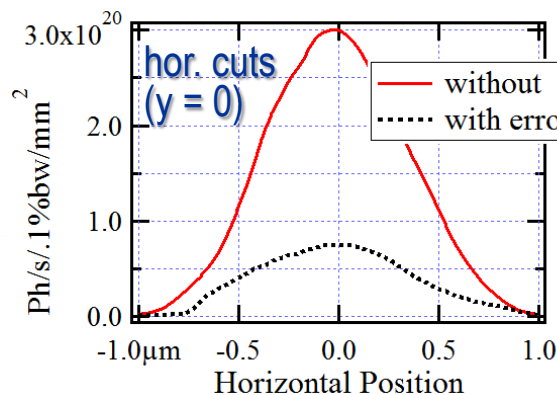
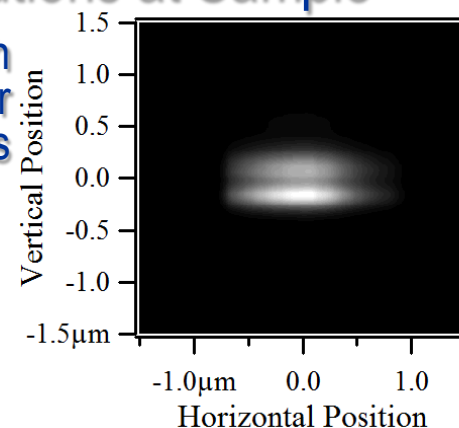
Horizontal SSA Size:  $30\ \mu\text{m}$   
 Photon Energy: 12.7 keV  
 Flux at Sample:  $\sim 5.4 \times 10^{13}\ \text{ph/s/.1\%bw}$



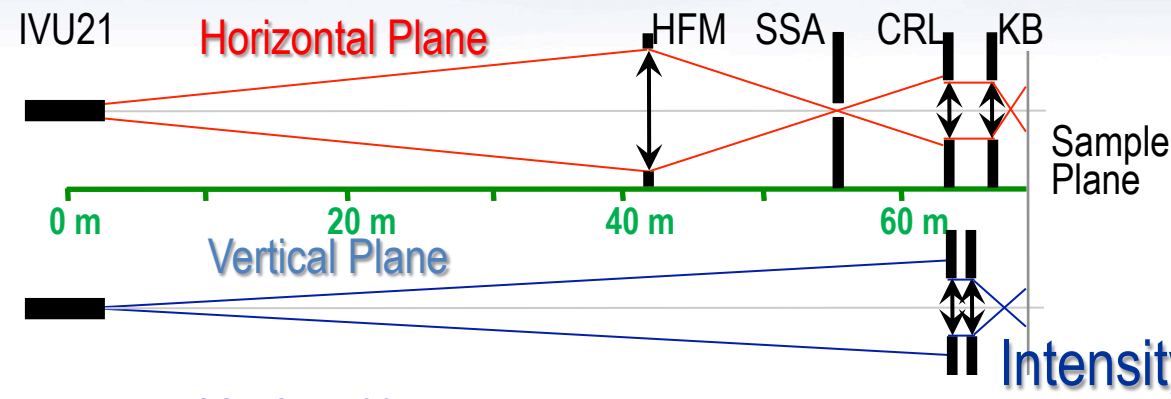
Without  
Mirror  
Errors



With  
Mirror  
Errors



# Using CRL for Producing “Large Spot” at Sample of FMX Beamline @ NSLS-II



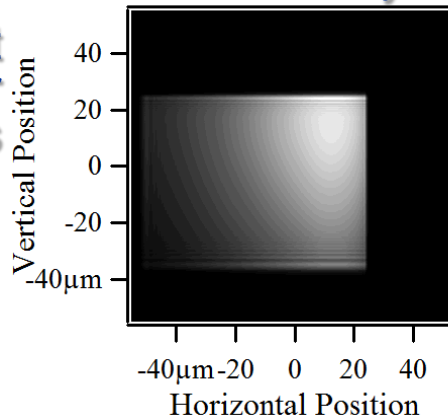
## Source:

Electron Current: 0.5 A  
 Horizontal Emittance: 0.55 nm (“ultimate”)   
 Vertical Emittance: 8 pm  
 Undulator: IVU21-1.5 m centered at +1.25 m from Low-Beta Straight Section Center

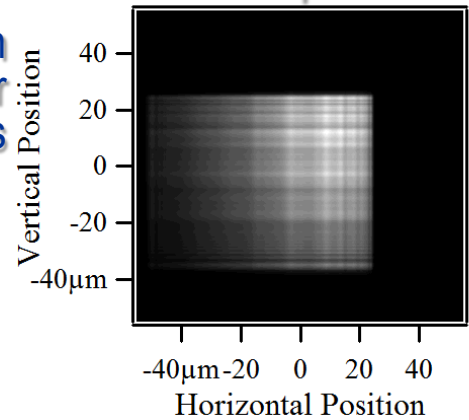
## Intensity Distributions at Sample

Horizontal SSA Size: 30  $\mu\text{m}$   
 Photon Energy: 12.7 keV

Without  
Mirror  
Errors



With  
Mirror  
Errors



## CRL “Transfocator”:

**8 Horizontally + 3 Vertically-Focusing Be Lenses**

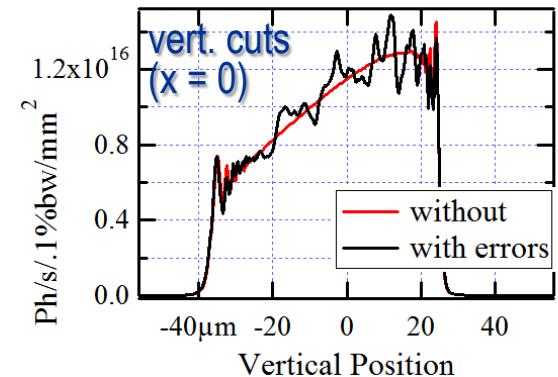
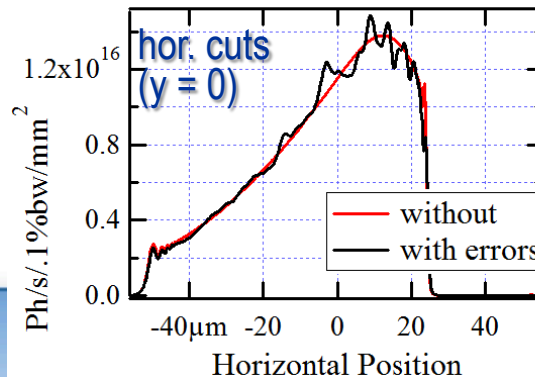
$R_{\min} = 200 \mu\text{m}$

$F_h \approx 5.9 \text{ m}$ ,  $F_v \approx 15.8 \text{ m}$

Geom. Ap.: 1 mm x 1 mm

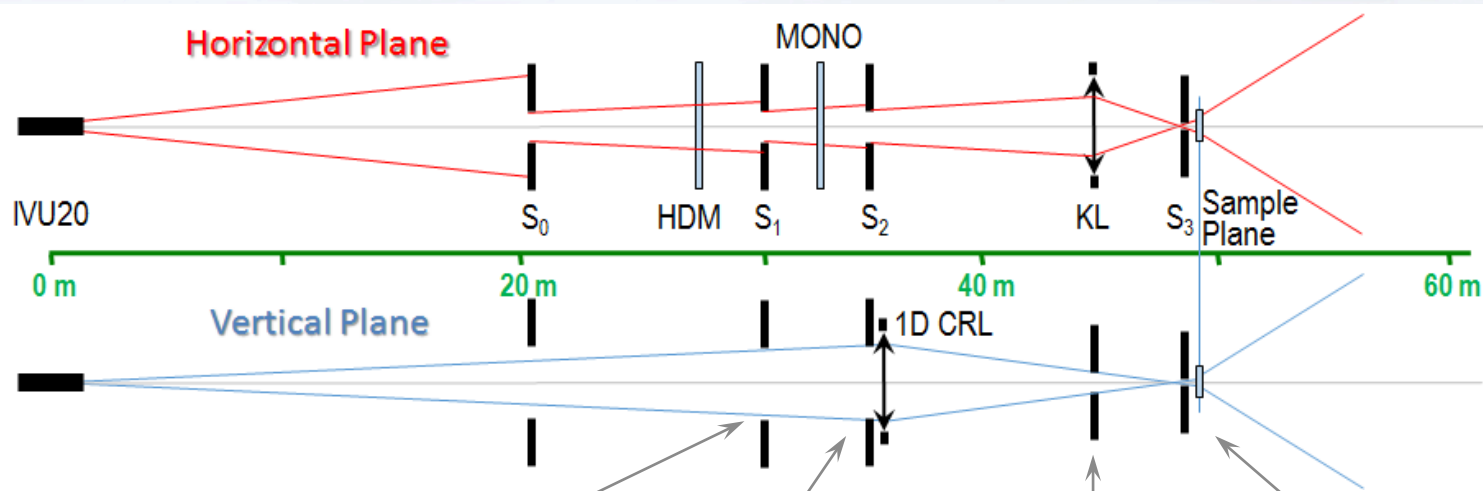
Located at 0.75 m before VKB edge  
 (10 m after SSA)

Flux Losses at CRL:  $\sim 1.6$  times





# Partially-Coherent Wavefront Propagation Simulations for CHX Beamline @ NSLS-II

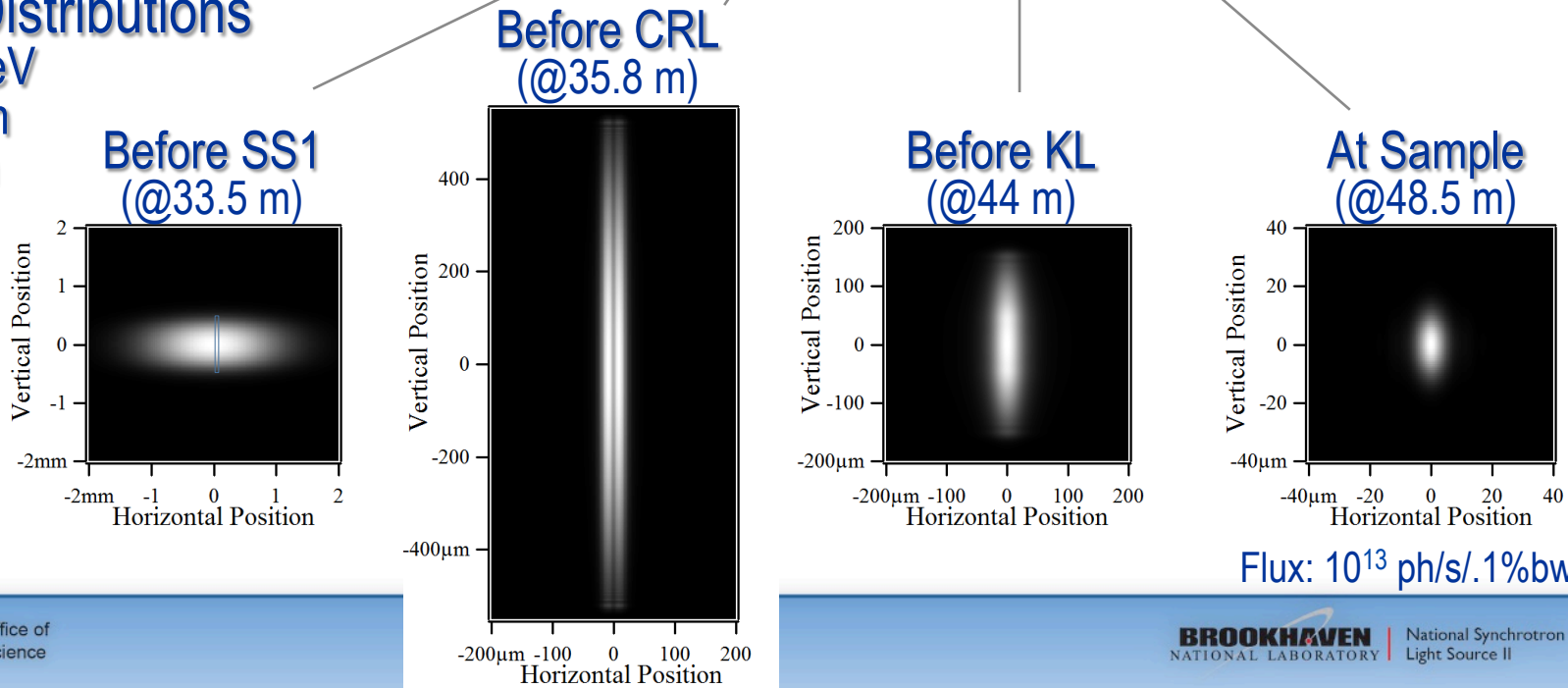


## Intensity Distributions

for  $E = 10 \text{ keV}$

$\Delta S_{1x} = 44 \text{ } \mu\text{m}$

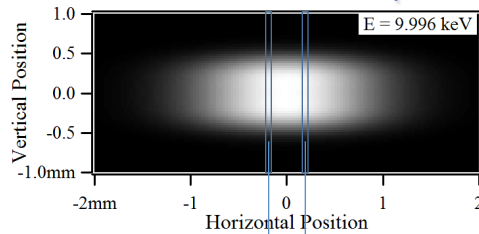
$\Delta S_{1y} = 1 \text{ mm}$



Flux:  $10^{13} \text{ ph/s/.1\%bw}$

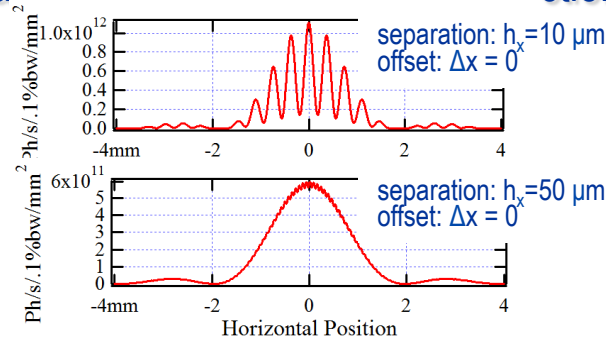
# Estimating Degree of Coherence of Radiation from U20 Installed in Low-Beta Straight Section of NSLS-II

Intensity Distribution  
at 30 m from Undulator

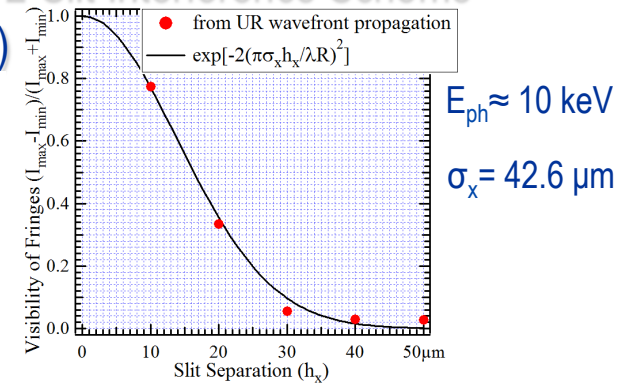


Slit Size:  $2\ \mu\text{m}$

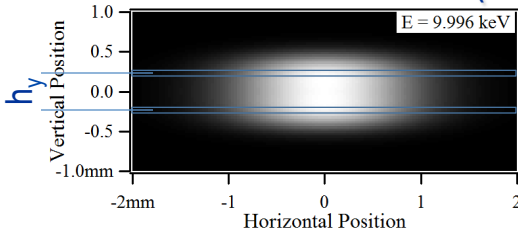
Vertical Slits (to estimate coherence in horizontal direction)



Visibility of Fringes in Young's  
2-Slit Interference Scheme

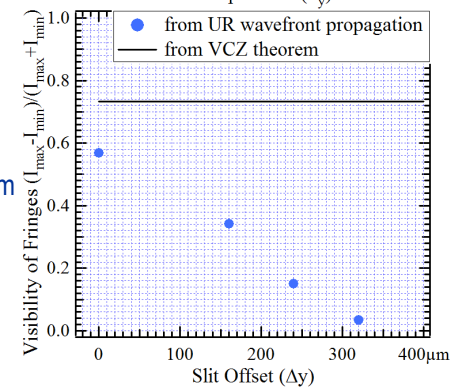
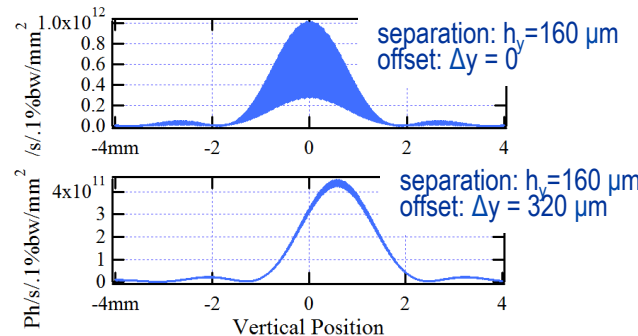
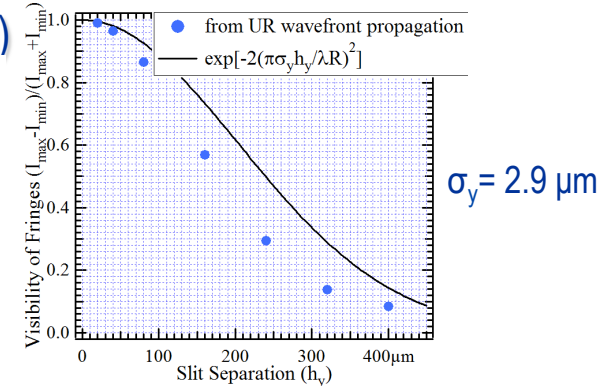
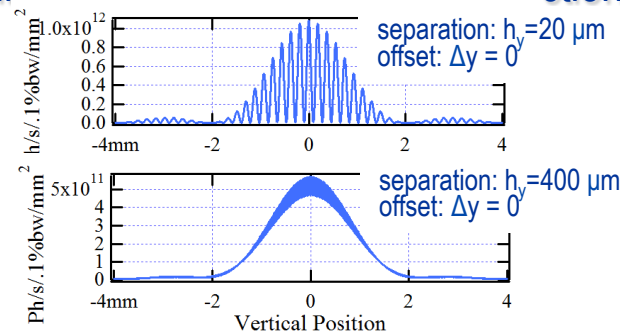


Horizontal Slits (to estimate coherence in vertical direction)



$h_y$

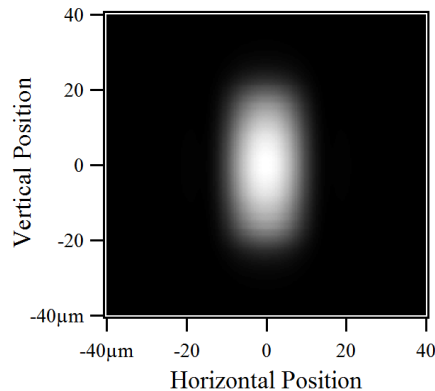
$\Delta y$





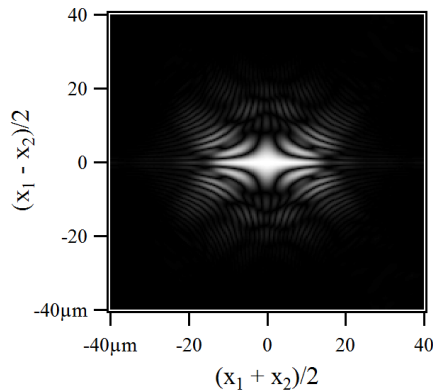
# Tracking Intensity and Degree of Transverse Coherence at a Sample (CHX @ NSLS-II)

Intensity Distribution

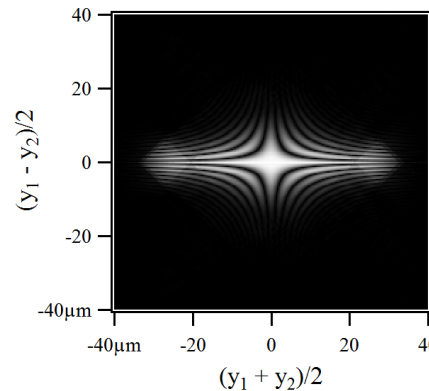


Degree of Transverse Coherence

In Horizontal Mid-Plane



In Vertical Mid-Plane

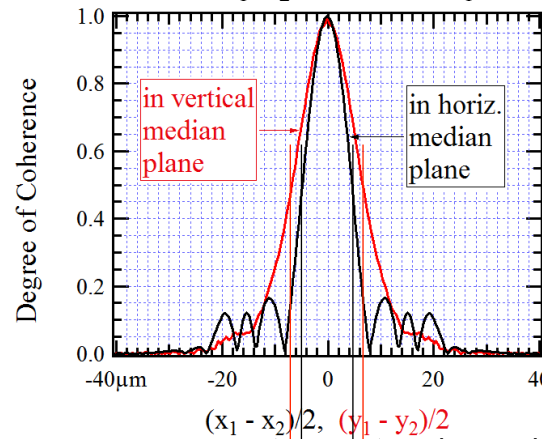
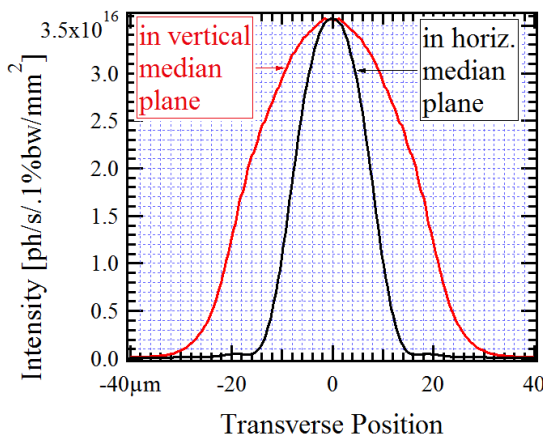
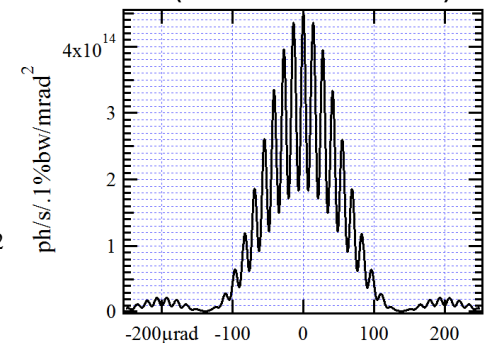


$$\mu(\mathbf{r}_1, \mathbf{r}_2, \omega) = |W(\mathbf{r}_1, \mathbf{r}_2, \omega) / [W(\mathbf{r}_1, \mathbf{r}_1, \omega)W(\mathbf{r}_2, \mathbf{r}_2, \omega)]|^{1/2}$$

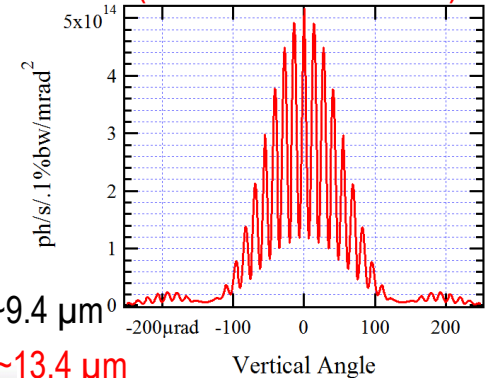
$$W(\mathbf{r}_1, \mathbf{r}_2, \omega) \sim \langle E(\mathbf{r}_1, \omega)E^*(\mathbf{r}_2, \omega) \rangle$$

Angular Intensity (far field)  
after Two Slits  
separated by 10 μm

In Horizontal Plane  
(after vertical slits)



In Vertical Plane  
(after horizontal slits)



$(x_1 - x_2)/2$      $(y_1 - y_2)/2$   
 →    ←    hor. coherence length: ~9.4 μm  
 →    ←    vert. coherence length: ~13.4 μm

Good agreement with 2-slit interference simulation results

# Partially-Coherent Wavefront Propagation Simulations for Inelastic X-ray Scattering Beamline with Advanced High-Resolution Crystal Optics (IXS @ NSLS-II)

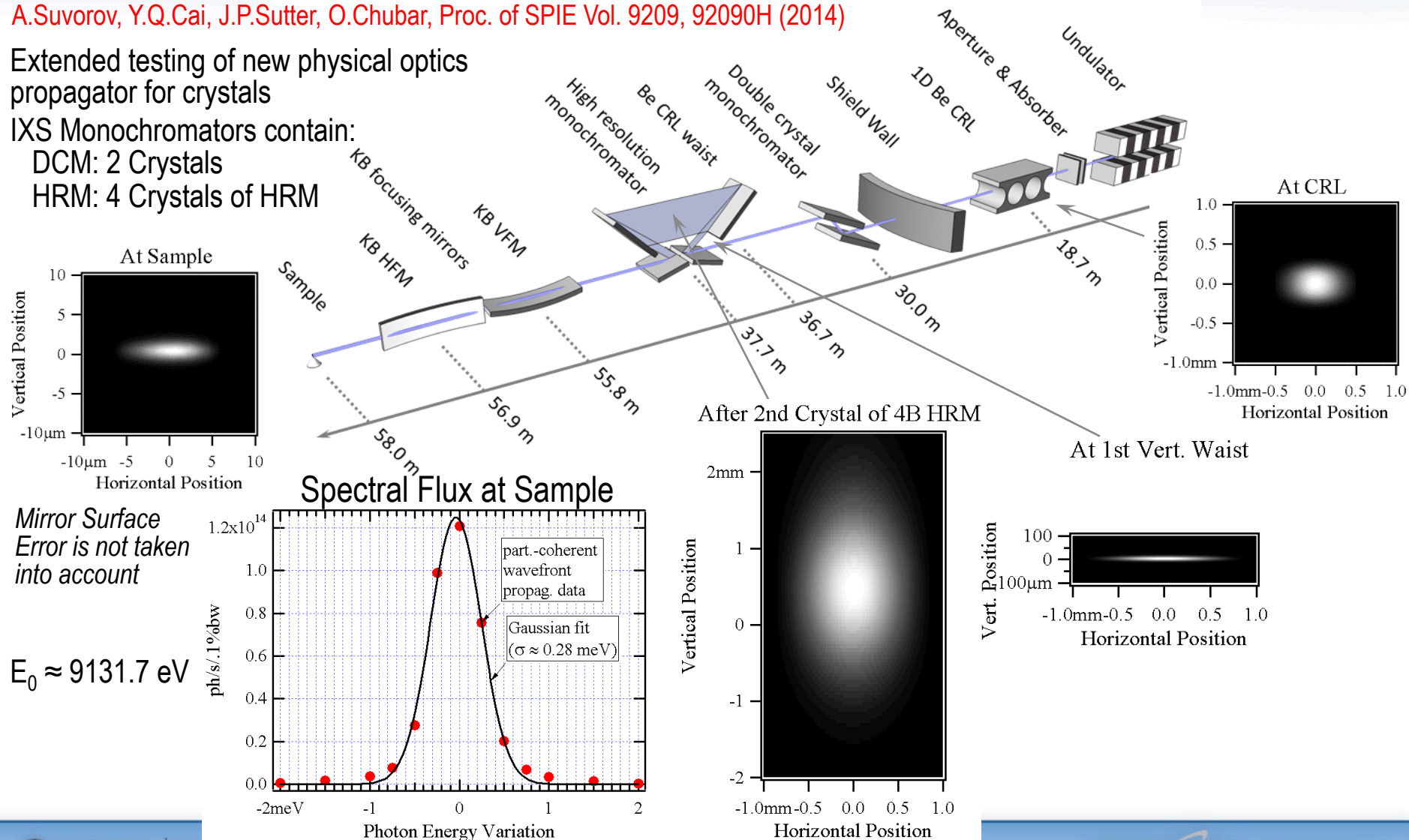
A.Suvorov, Y.Q.Cai, J.P.Sutter, O.Chubar, Proc. of SPIE Vol. 9209, 92090H (2014)

Extended testing of new physical optics propagator for crystals

IXS Monochromators contain:

DCM: 2 Crystals

HRM: 4 Crystals of HRM



Mirror Surface  
Error is not taken  
into account

$E_0 \approx 9131.7$  eV

# NSLS-II Soft Matter Interfaces beamline modelling

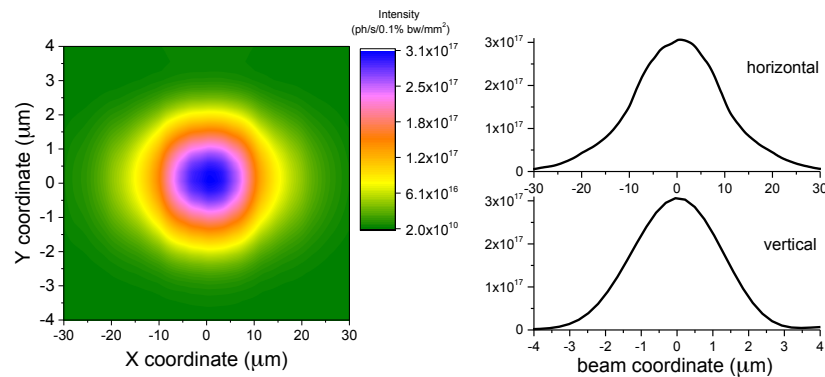
Courtesy of M. Zhernenkov and M. Rakitin

SRW modelling with:

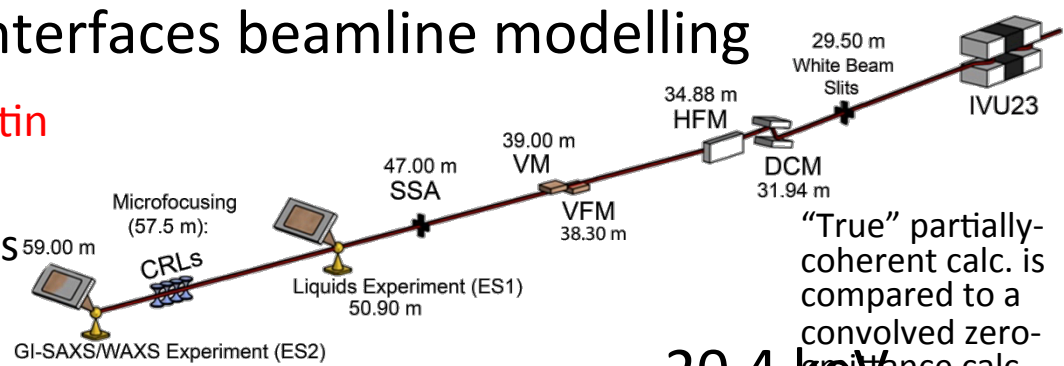
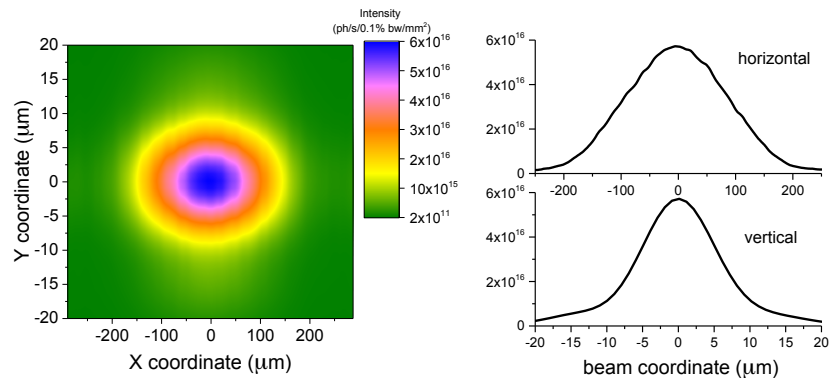
- ✓ actual measured SMI mirrors' profiles
- ✓ FEA heat load on 1<sup>st</sup> DCM crystal

2.1 keV

ES2 focus with CRLs



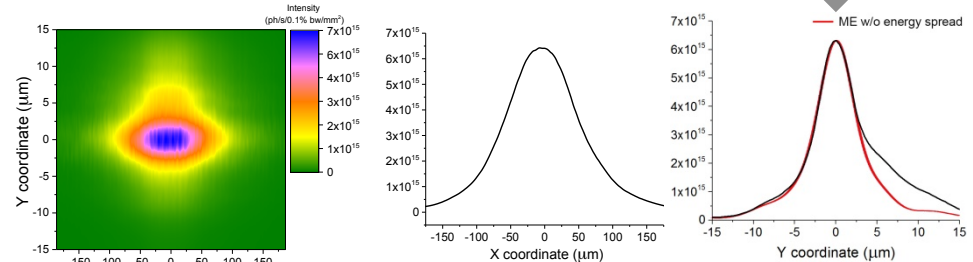
ES2 focus no CRLs



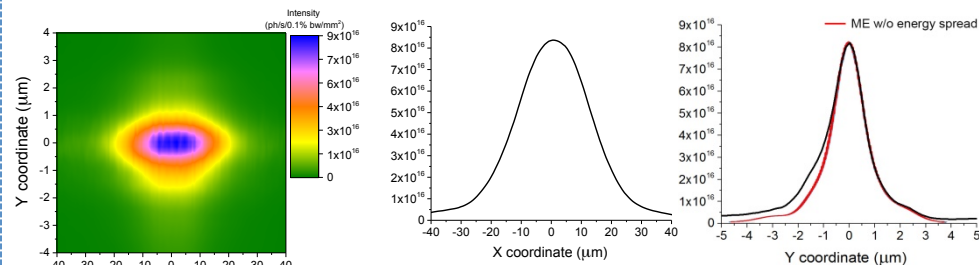
“True” partially-coherent calc. is compared to a convolved zero-radiance calc. (obtained in 30 s)

20.4 keV

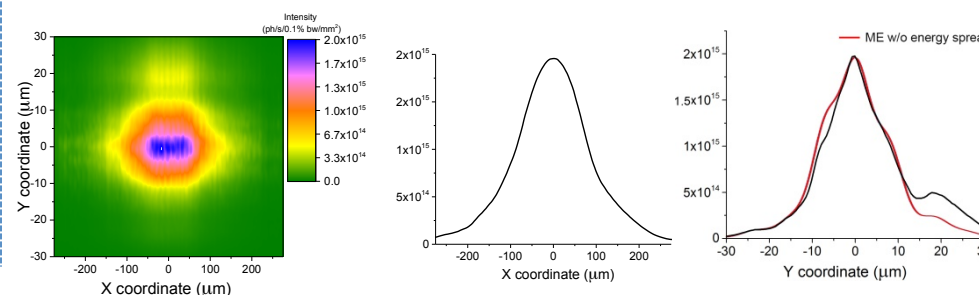
ES1 focus



ES2 focus with CRLs



ES2 focus no CRLs



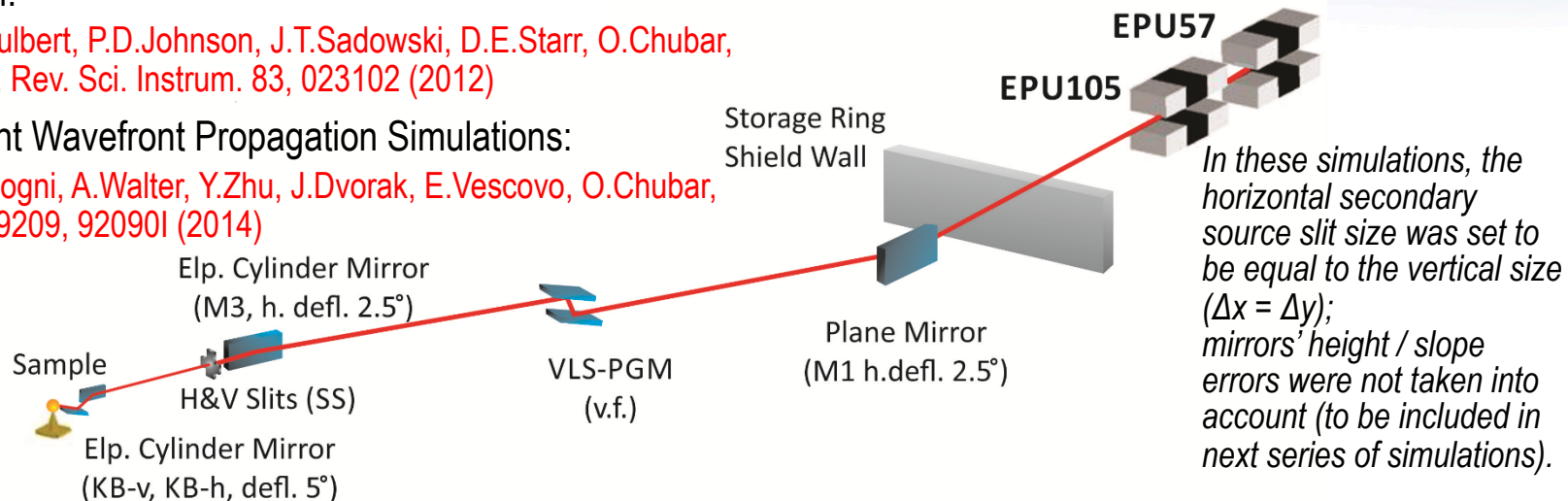
# Partially-Coherent Wavefront Propagation Simulations for a Soft X-ray Beamline with VLS grating (ESM @ NSLS-II)

## Beamline Design:

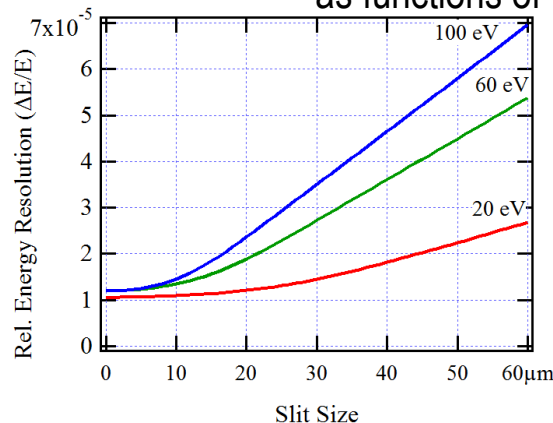
R.Reininger, S.L.Hulbert, P.D.Johnson, J.T.Sadowski, D.E.Starr, O.Chubar, T.Valla, E.Vescovo, Rev. Sci. Instrum. 83, 023102 (2012)

## Partially-Coherent Wavefront Propagation Simulations:

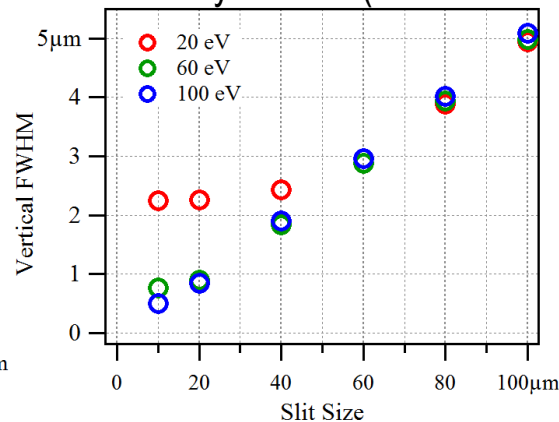
N.Canestrari, V.Bisogni, A.Walter, Y.Zhu, J.Dvorak, E.Vescovo, O.Chubar, Proc. of SPIE Vol. 9209, 92090I (2014)



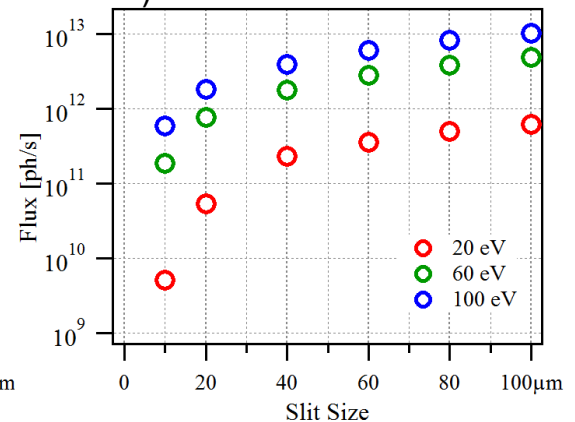
## Energy Resolution



## Spatial Resolution



## Flux (finite-bandwidth) at Sample



$$\Delta E/E > (mN) \uparrow - 1$$

Two different VLS Gratings (160 mm long) were used:

$\lambda/10 = 800$  lines/mm for  $E = 20$  eV;  $\lambda/10 = 600$  lines/mm for  $E = 60, 100$  eV

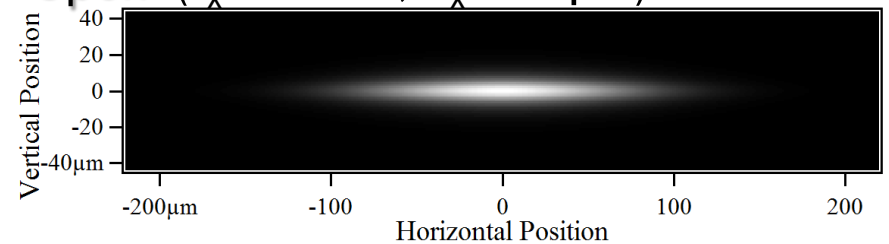
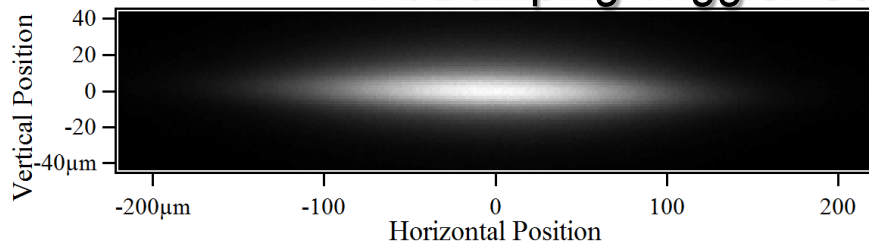


# NSLS-II Emittance Reduction by DWs Observed after Imperfect Optics at “Secondary Source” of HXN

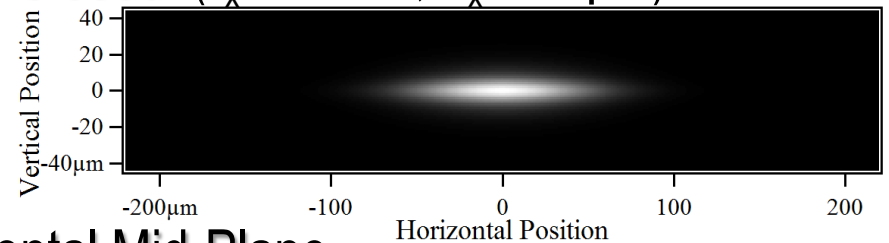
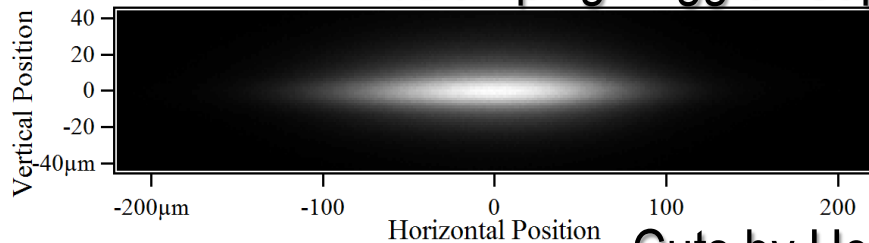
Intensity Distributions at 8.0 keV (5<sup>th</sup> UR Harmonic) at “Secondary Source”  
in Intermediate Hatch (Optical Magnification:  $\sim 0.93$ )

Measured At Damping Wiggler Gaps “Open” ( $\epsilon_x \approx 2.1$  nm,  $\sigma_x \approx 61$   $\mu$ m)

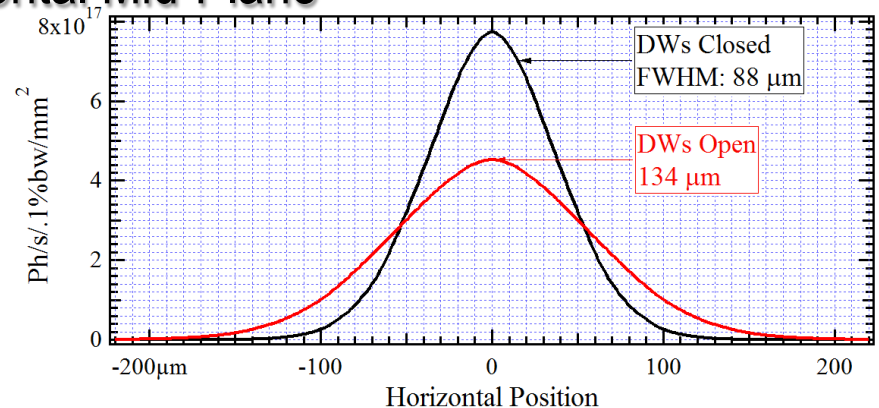
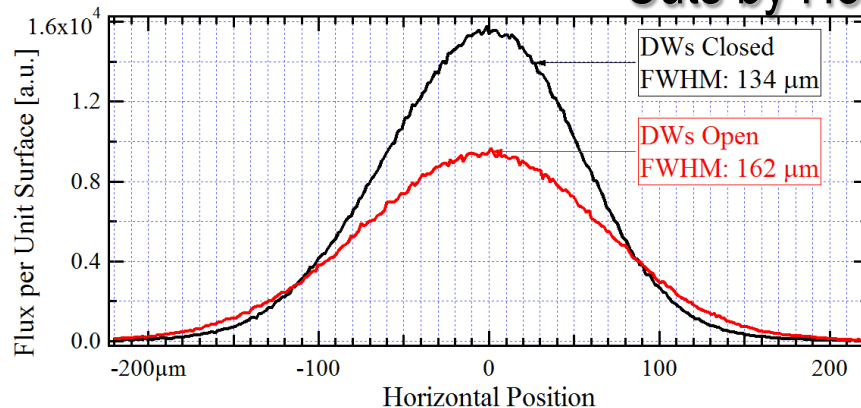
Calculated For perfect optical elements



At Damping Wiggler Gaps “Closed” ( $\epsilon_x \approx 0.9$  nm,  $\sigma_x \approx 40$   $\mu$ m)

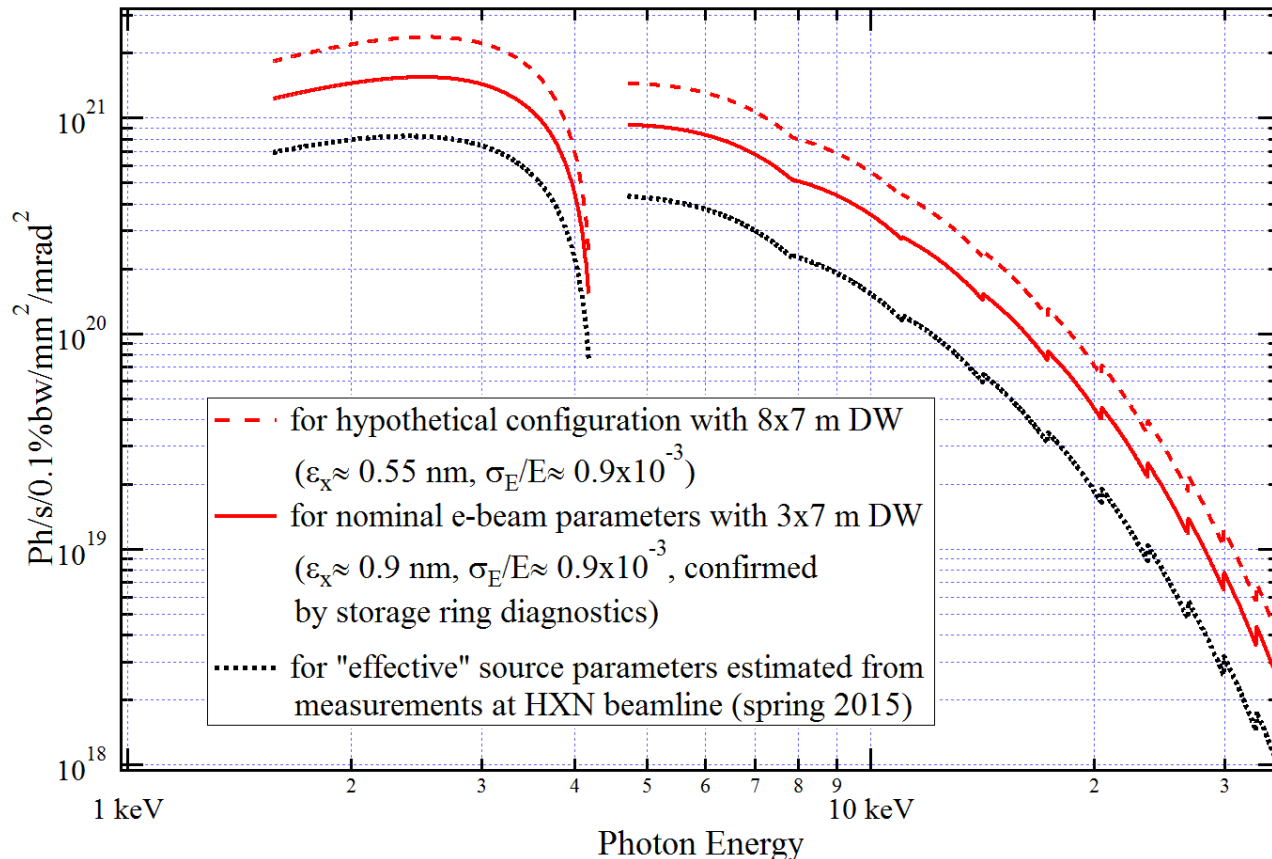


Cuts by Horizontal Mid-Plane



# NSLS-II Brightness: Nominal and Estimated from Measurements at HXN Beamline

Approximate Spectral Brightness of IVU20 in Low-Beta Straight Section of NSLS-II



All curves are scaled for 0.5 A e-beam current.

Note: absolute values of spectral brightness may not be very accurate, however, relative "locations" of the curves are credible.

The reduction of brightness "observed" at the beamline is attributed to imperfections of X-ray optics (horizontally-focusing bendable mirrors, monochromator, vertically-focusing CRL) and undulator magnetic field.

It will be possible to "restore" this "effective" brightness in the future (by further fine-tuning / processing / replacing of individual beamline components, identified from simulations and dedicated measurements).



U.S. DEPARTMENT OF  
**ENERGY**

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NATIONAL LABORATORY  
BROOKHAVEN SCIENCE ASSOCIATES



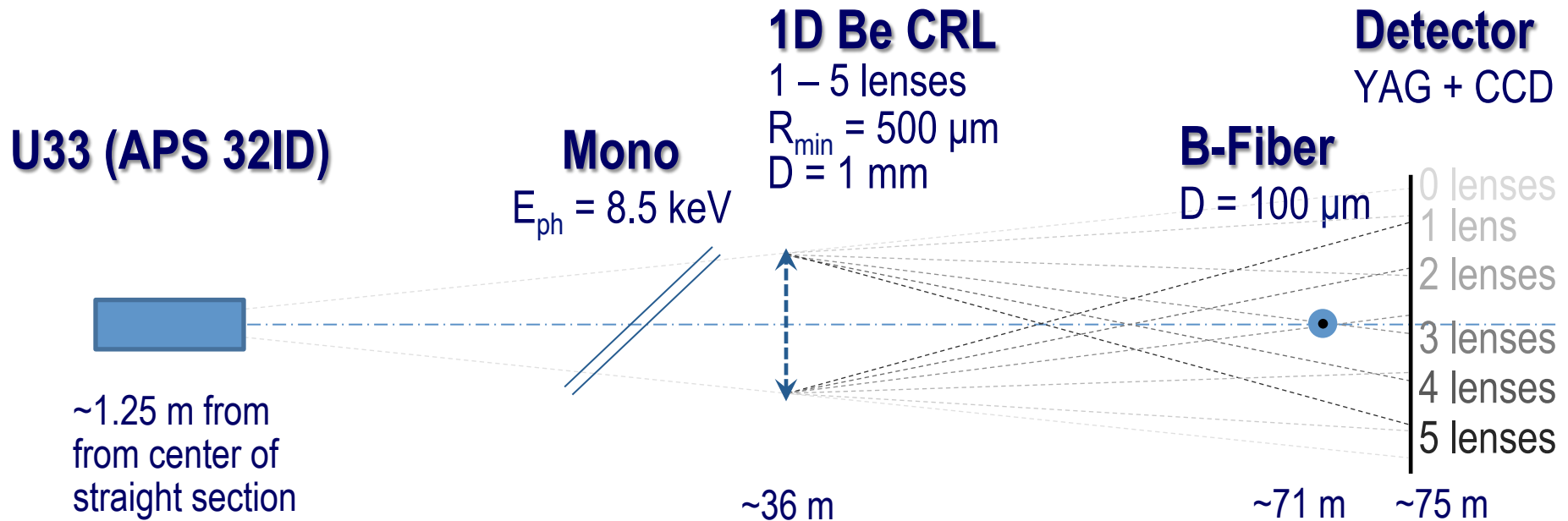
# Approach to Coherence Preservation Diagnostics Assisted by Simulations (Illustration)

V.Kohn, I.Snigireva and A.Snigirev, Phys. Rev. Lett., vol.85(13), p.2745 (2000)

A.Snigirev, V.Kohn, I.Snigireva, B.Lengeler, Nature, vol.384, p.49 (1996)

O.Chubar, A.Fluerasu, Y.S.Chu, L.Berman, L.Wiegart, W.-K.Lee, J.Baltser, J. Phys.: Conf. Ser. 425, 052028 (2013)

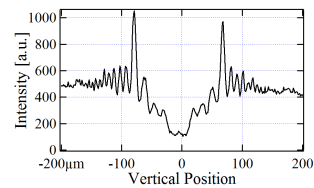
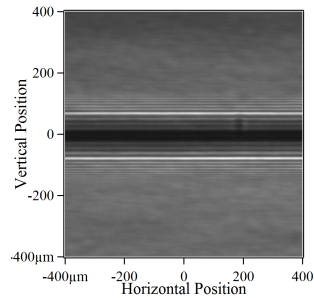
## Optical scheme of test experiments with CRL and a Boron fiber probe



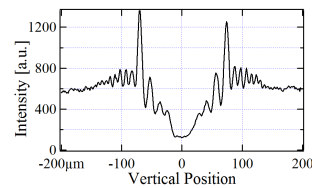
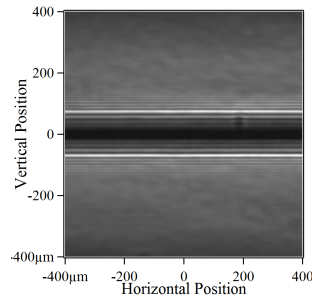
# Intensity Distributions in the B-fiber Based Interference Scheme for Different Numbers of CRL in Optical Path

Simulations allow to conclude about coherence preservation in presence of any beamline optics!

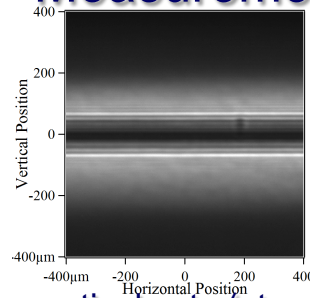
no lenses



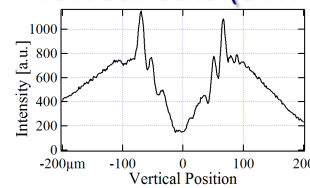
1 lens



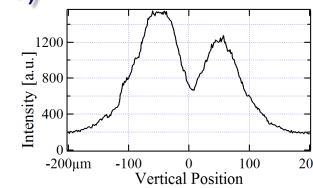
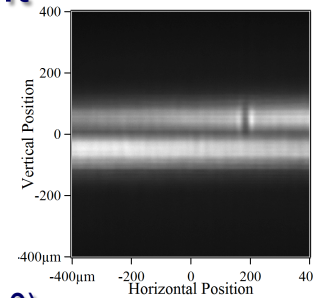
2 lenses  
Measurement



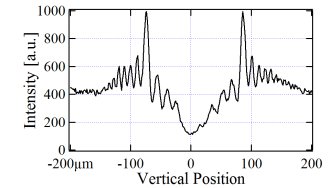
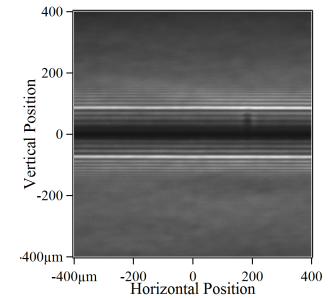
vertical cuts (at x = 0)



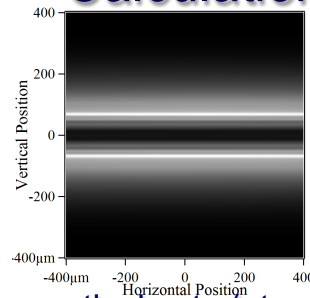
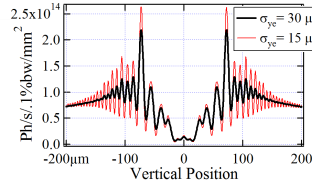
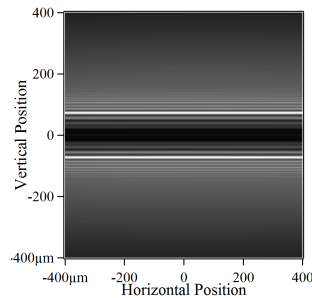
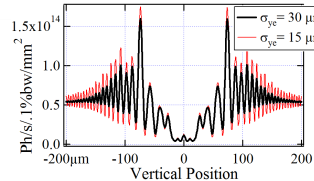
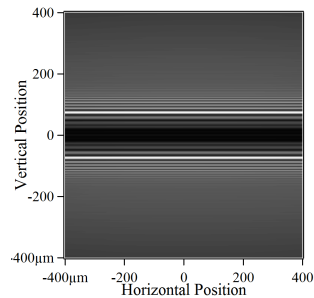
3 lenses



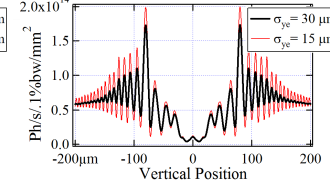
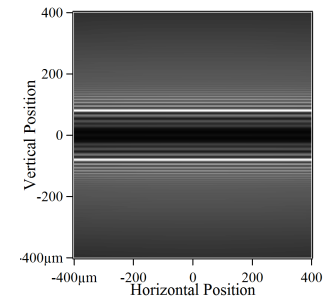
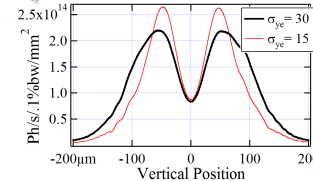
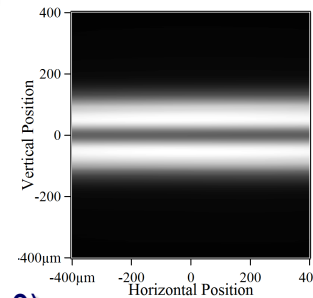
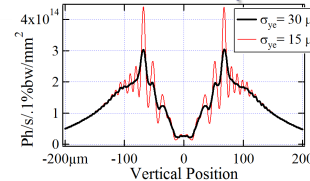
5 lenses



Calculation



vertical cuts (at x = 0)



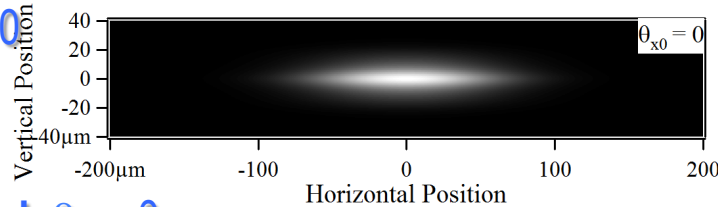
# Intensity Distributions of Focused Wiggler Radiation from Partially-Coherent Wavefront Propagation Calculations

On-Axis Collection:  $\theta_{x0} = 0$ ,  $\theta_{y0} = 0$

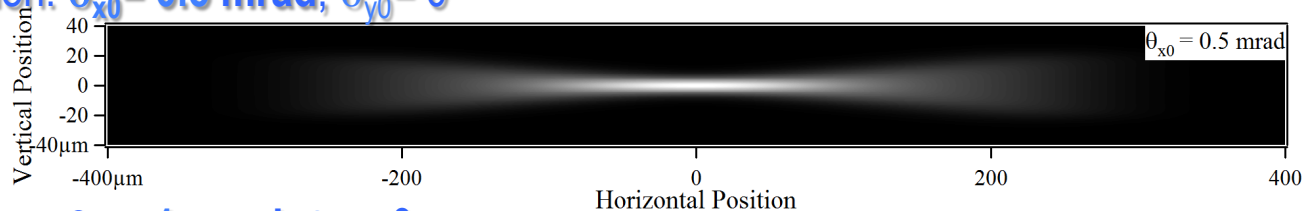
$|\theta_x - \theta_{x0}| < 0.1$  mrad

$|\theta_y - \theta_{y0}| < 0.1$  mrad

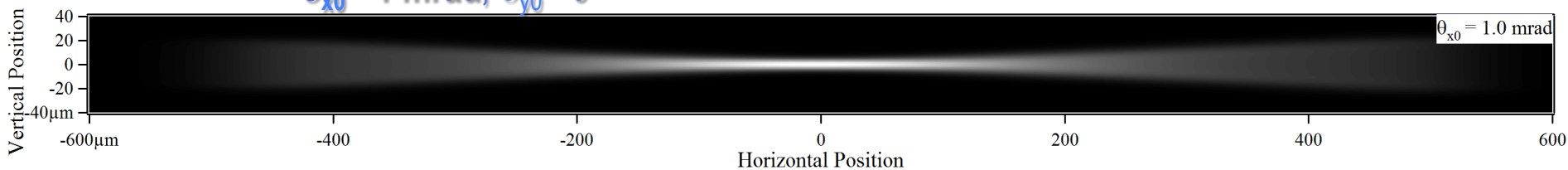
1 : 1 Imaging Scheme  
with "Ideal Lens"



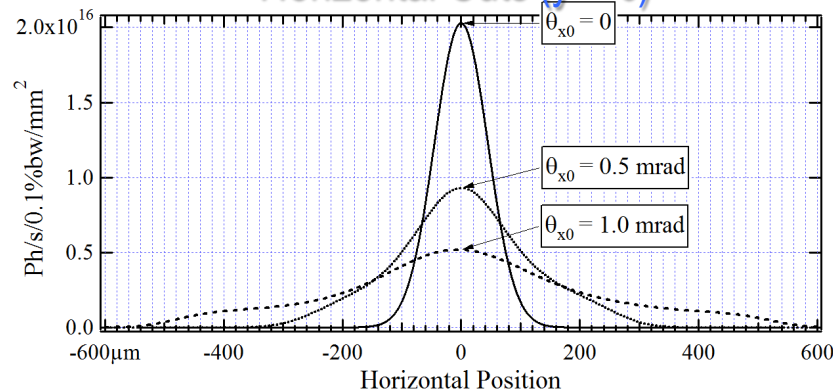
Off-Axis Collection:  $\theta_{x0} = 0.5$  mrad,  $\theta_{y0} = 0$



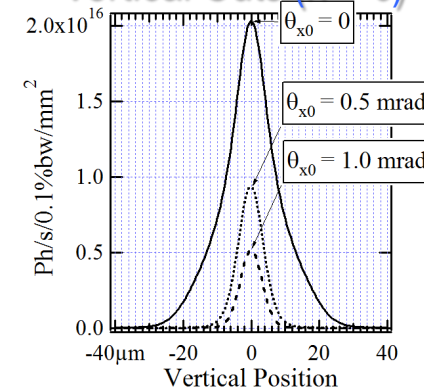
$\theta_{x0} = 1$  mrad,  $\theta_{y0} = 0$



Horizontal Cuts ( $y = 0$ )



Vertical Cuts ( $x = 0$ )



NSLS-II Low-Beta Straight Section  
 $I = 0.5$  A,  $\epsilon_x = 0.9$  nm,  $\epsilon_y = 8$  pm

SCW40:  $\lambda_u = 40$  mm,  $B_{\max} = 3$  T,  $L = 1$  m  
Photon Energy:  $E_{ph} = 10$  keV

# Wavefront Propagation Calculations for ROBL at ESRF

HZDR

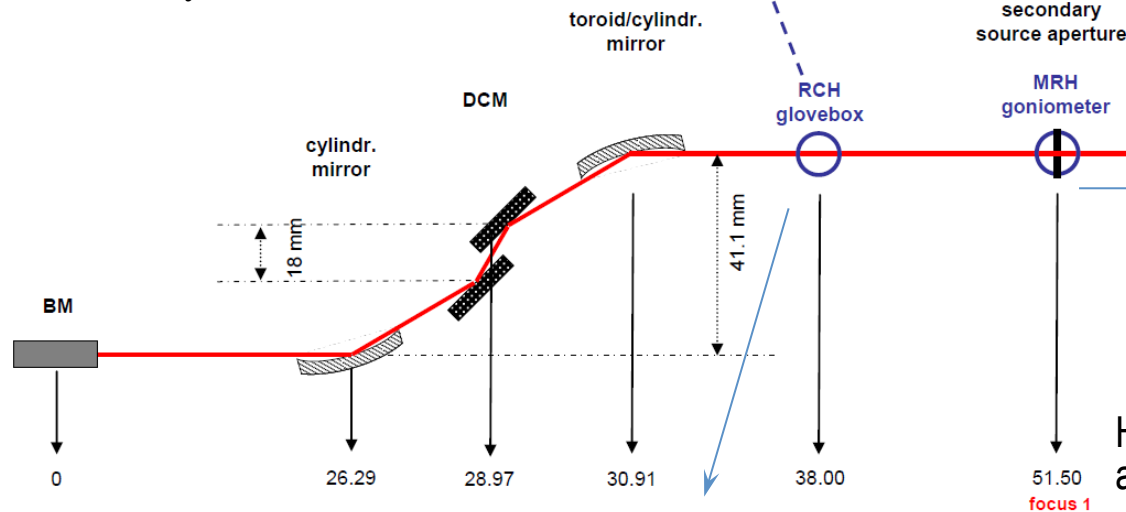
SHADOW:

$8.0 \times 1.0 \text{ mm}^2$   
 $1.4 \times 10^{12} \text{ ph/s (x2)}$

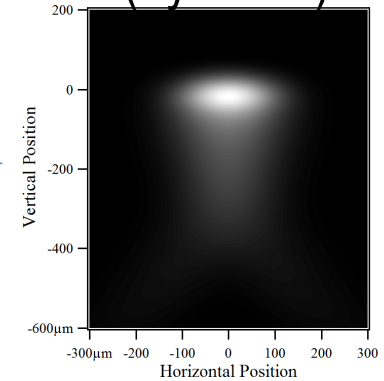
$130 \times 230 \text{ }\mu\text{m}^2$   
 $1.4 \times 10^{12} \text{ ph/s (x160)}$

$E = 18 \text{ keV}$

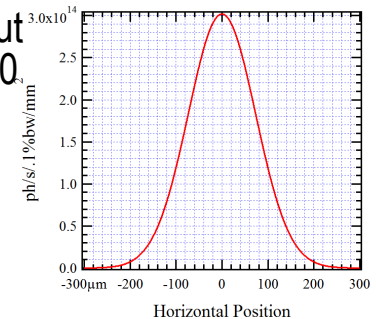
Figure courtesy A. Scheinost



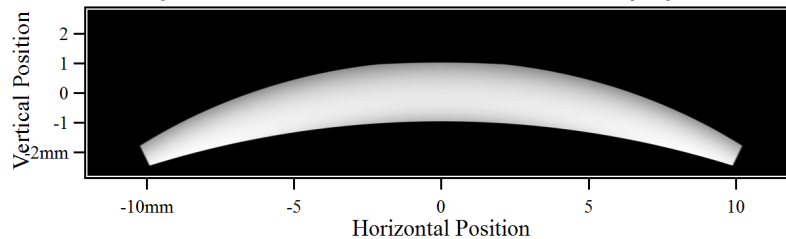
Intensity Distribution  
 at MRH / focus  
 (by SRW)



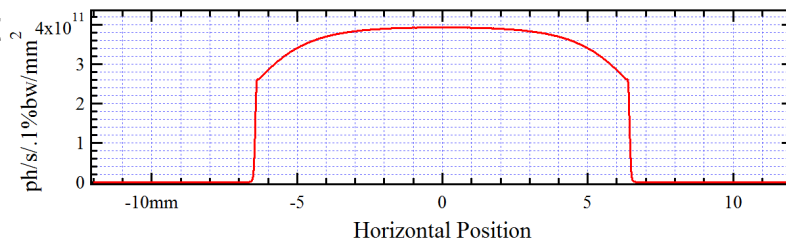
Hor. cut  
 at  $y = 0$



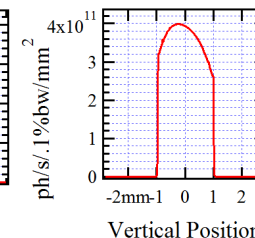
Intensity Distribution at RCH (by SRW)



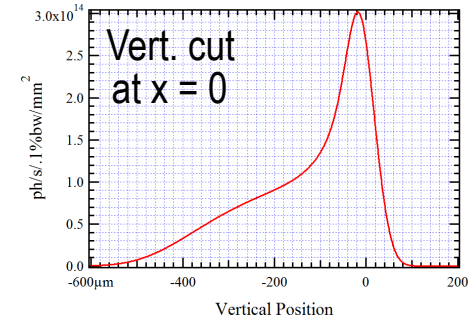
Hor. cut  
 at  $y = 0$



Vert. cut  
 at  $x = 0$



Vert. cut  
 at  $x = 0$

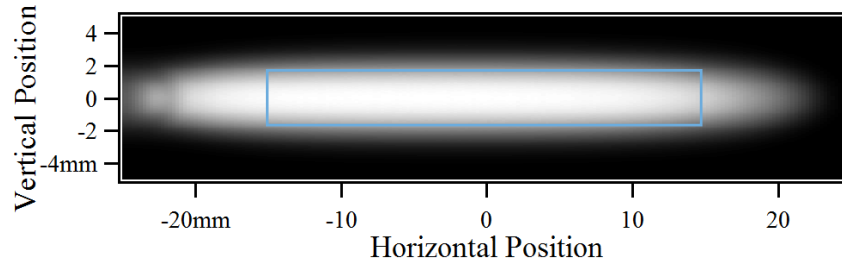


# 2PW-B Option for ROBL after ESRF Upgrade

Intensity Distribution at 18 keV at ~29.3 m from Source (assuming no apertures upstream)

*In this case, since the initial wavefront is very "spiky" (because of interference of several sources), the simulation was done in steps:*

- first, intensity in transverse plane before 1st aperture was calculated;
- second, electric field was instantiated from this intensity, assuming spher. wave, and propagated to final observation plane;
- finite e-beam size was taken into account by convolution.



## Spectral Flux

within  $|x| < 14.65$  mm,  $|y| < 1.625$  mm:  
 $\sim 4.0 \times 10^{13}$  ph/s/.1%bw

## Optical Scheme Parameters

Longitudinal Positions:

VCM: 29.3 m

TFM: 34.3 m

SSA: 54.5 m

Mirror Radii:

VCM:  $R = 20$  km

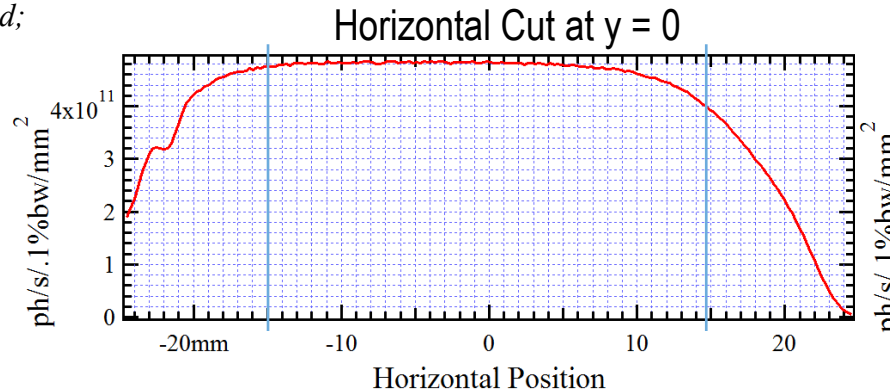
TFM:  $R_s = 61.8$  mm

$R_t = 18.0$  km

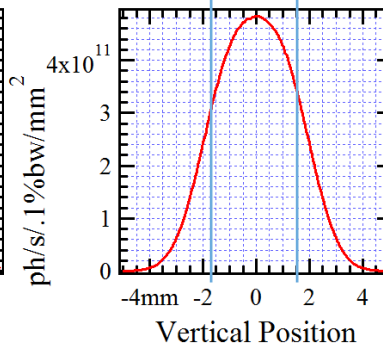
Incident Angles:

VCM: 2.5 mrad

TFM: 2.42 mrad



## Vertical Cut at $x = 0$

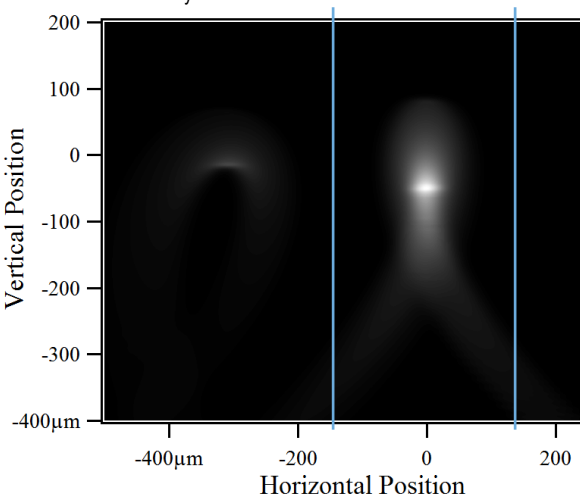


## e-Beam Parameters:

$E = 6$  GeV,  $I_e = 200$  mA

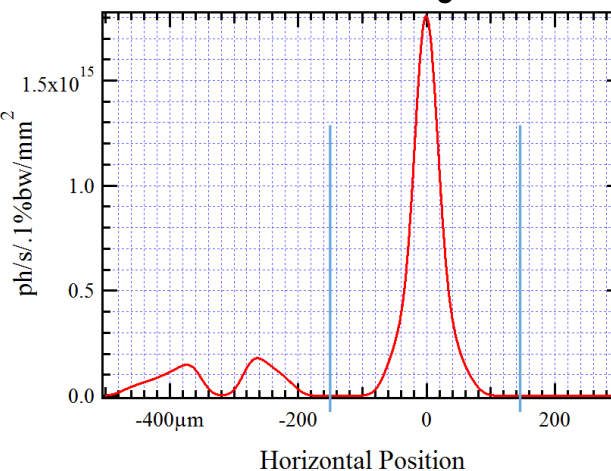
$\epsilon_x = 130$  pm,  $\epsilon_y = 5$  pm

$\beta_x = 1.81$  m,  $\beta_y = 2.57$  m

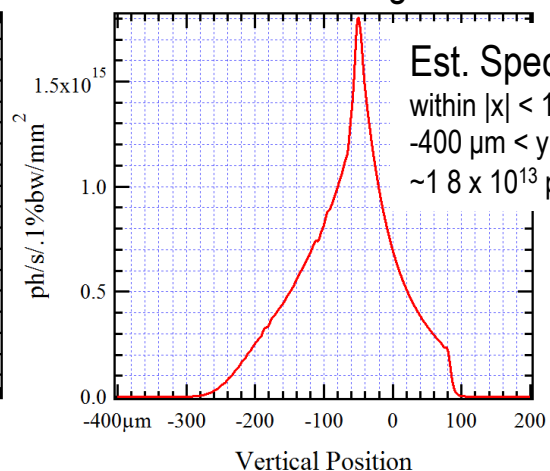


## Intensity Distribution at SSA

### Horizontal Cut through Max.



### Vertical Cut through Max.



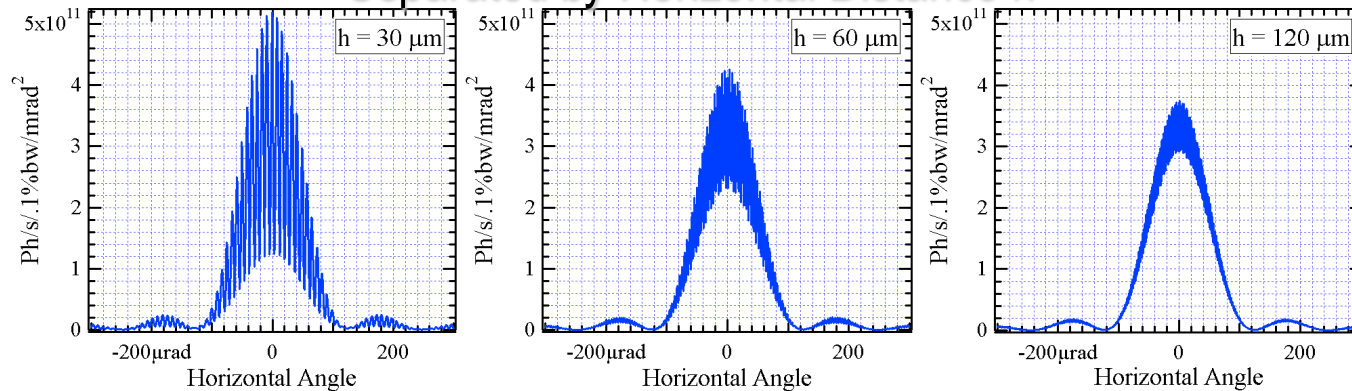
## Est. Spec. Flux

within  $|x| < 150$  μm,  
 $-400$  μm  $< y < 200$  μm:  
 $\sim 1.8 \times 10^{13}$  ph/s/.1%bw



# Estimating Degree of Coherence (/ Transverse Coherence Lengths) of Radiation from ESRF-U 2PW by Simulating Young's 2-Slit Interference Schemes

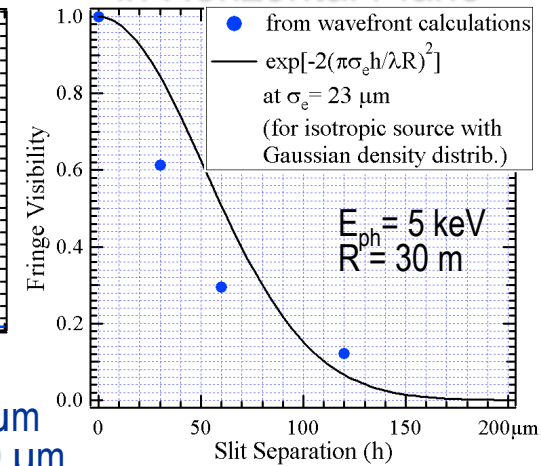
## Far-Field Interference Patterns from 2 Vertical Slits Separated by Horizontal Distance $h$



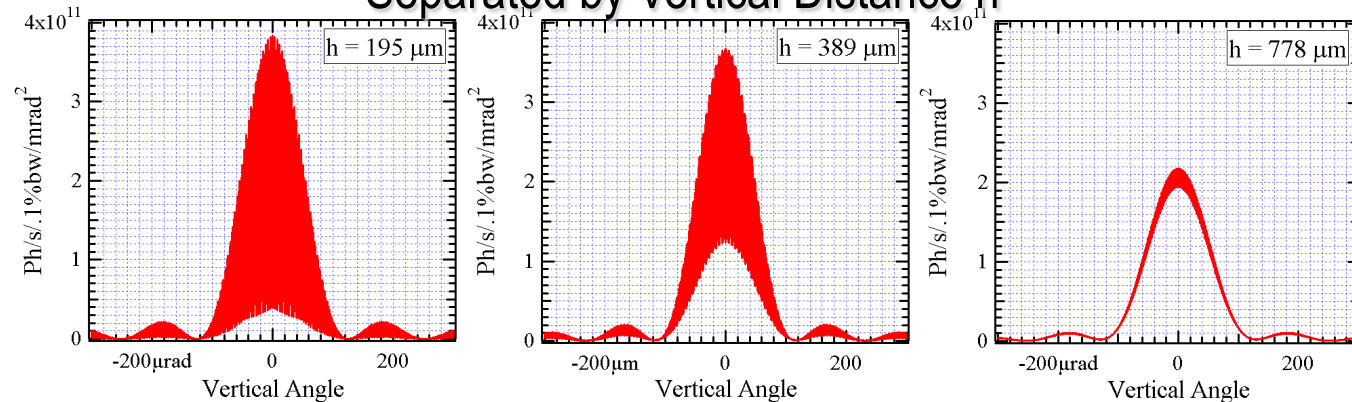
Vertical Aperture: 1 mm; Slit Size:  $2 \mu\text{m}$

Horizontal Coherence Length:  $\sim 40 \mu\text{m}$   
For a BM-like Source should be  $\sim 60 \mu\text{m}$

## Fringe Visibility vs $h$ in Horizontal Plane



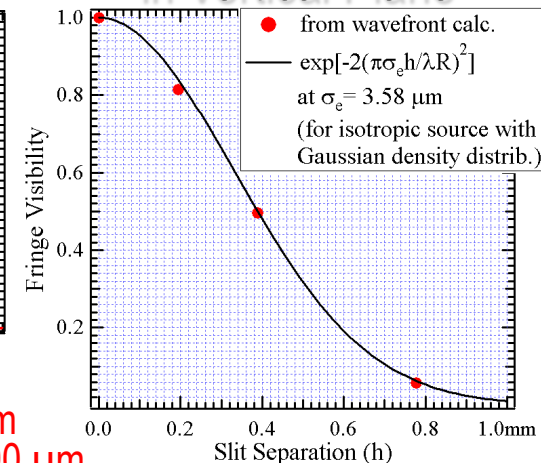
## Far-Field Interference Patterns from 2 Horizontal Slits Separated by Vertical Distance $h$



Horizontal Aperture: 1 mm; Slit Size:  $2 \mu\text{m}$

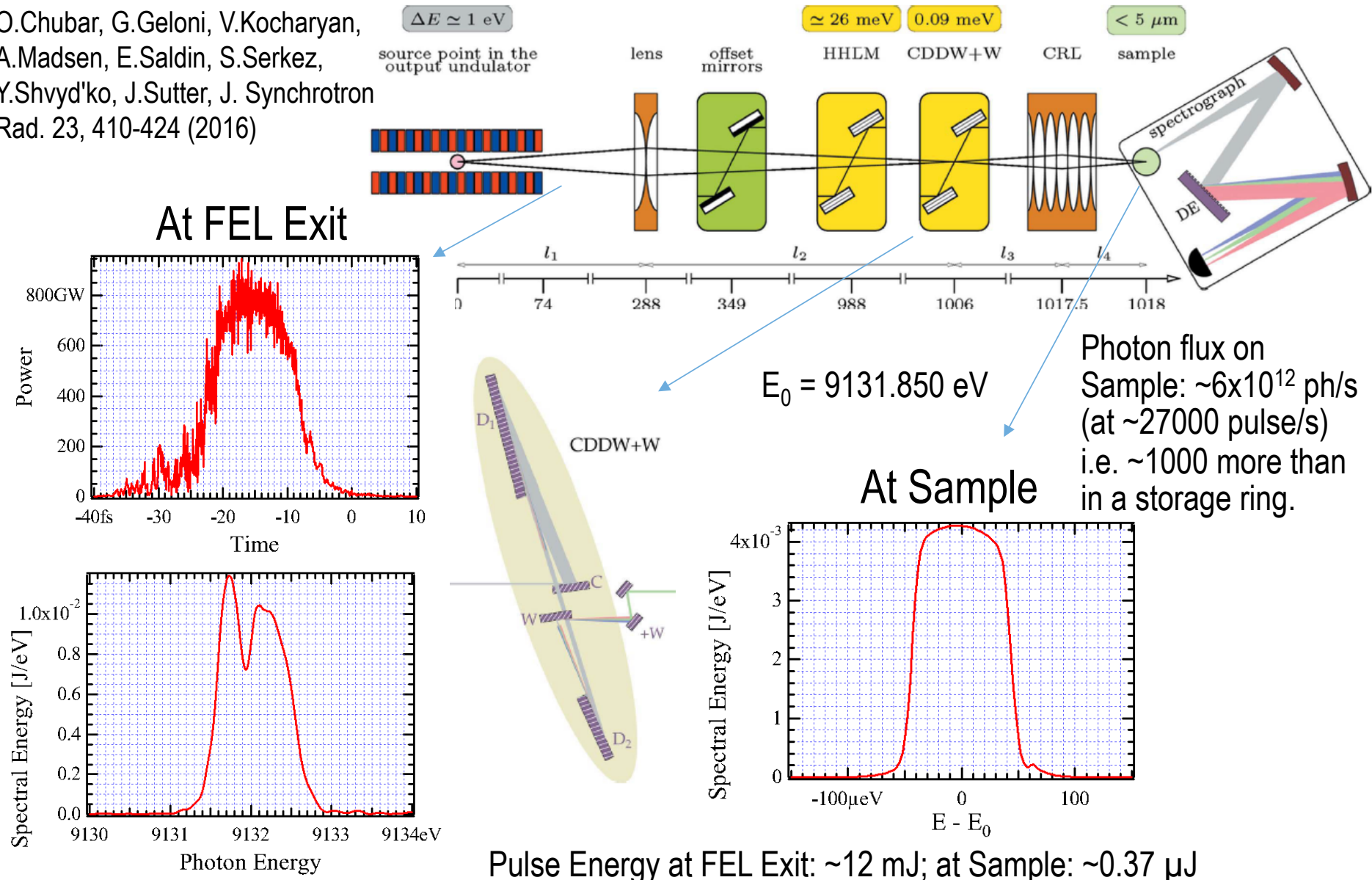
Vertical Coherence Length:  $\sim 390 \mu\text{m}$   
For a BM-like Source should be  $\sim 390 \mu\text{m}$

## Fringe Visibility vs $h$ in Vertical Plane



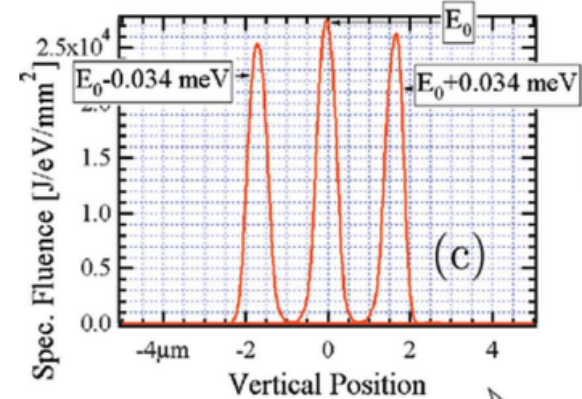
# Testing Ultra-High Resolution Inelastic X-ray Scattering Scheme at High-Rep-Rate Self-Seeded X-FEL

O.Chubar, G.Geloni, V.Kocharyan,  
A.Madsen, E.Saldin, S.Serkez,  
Y.Shvyd'ko, J.Sutter, J. Synchrotron  
Rad. 23, 410-424 (2016)

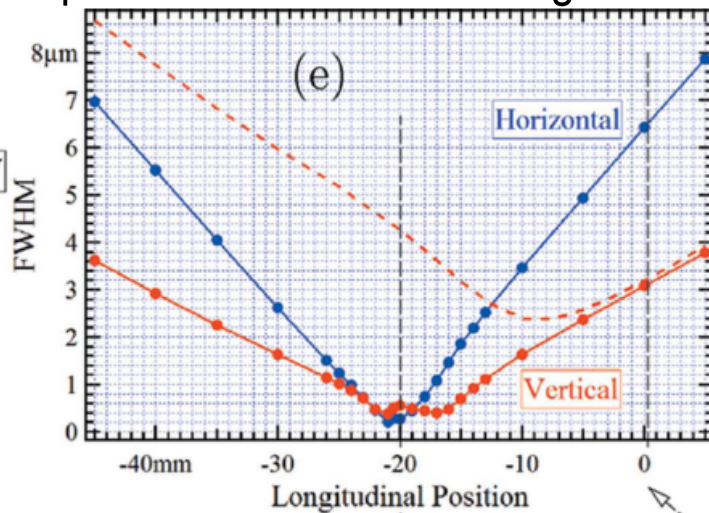


# IXS at X-FEL: Radiation Pulse Characteristics Near Sample

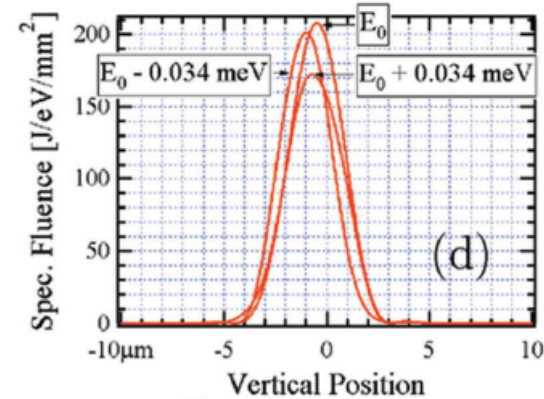
Spectral Fluence at Monochromatic Waist at  $x = 0$



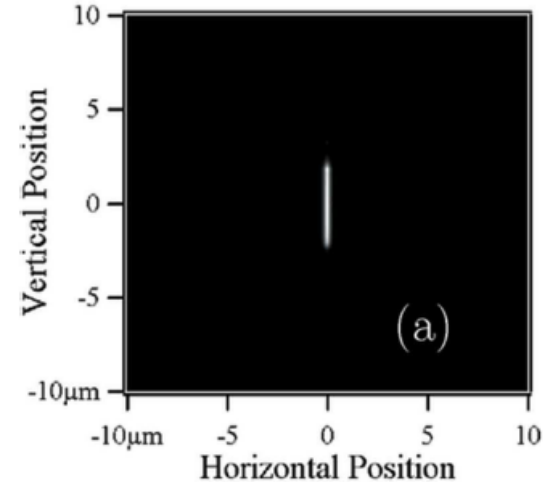
Spot Sizes at Different Long. Position



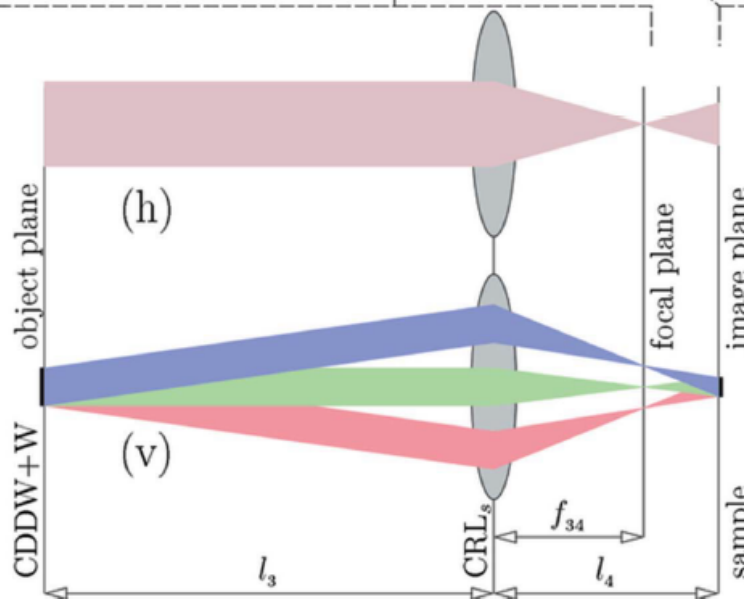
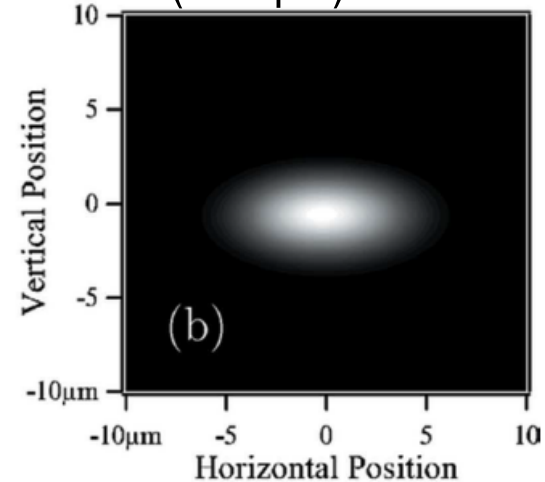
Spectral Fluence in Geom. Image (Sample) Plane at  $x = 0$



Fluence at Monochromatic Waist



Fluence in Geom. Image (Sample) Plane



# Summary and Comments

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- High-accuracy fully- and partially-coherent synchrotron emission and wavefront propagation calculations for sources and beamline optics are currently done routinely for beamlines at new storage rings and FEL (though performance can still be an issue in cases of low coherence).
- An advantage of high-accuracy wavefront calculations is very broad range of applications (because of their general electrodynamics basement): design of new sources and optics (maximizing performance of both), commissioning, diagnostics, simulation of user experiments, addressing misc. inverse problems of data processing, etc. Some interesting potential applications are not fully explored yet.
- Main disadvantage of these calculations is currently a ~low CPU performance in low-coherence cases compared to geometrical ray-tracing; however, it can be mitigated by parallelization, coherent mode decomposition and other methods.  
Note: the higher is the degree of coherence in a beamline, the easier is the treatment of partial coherence, which is very good for applications in FEL and MBA storage rings.  
Another “disadvantage” is higher complexity of these calculations compared to ray-tracing. It can be mitigated by programming more robust “propagators”, propagation “drivers”, as well as developing better user interfaces and writing better help.



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